



Recursion

Recursion

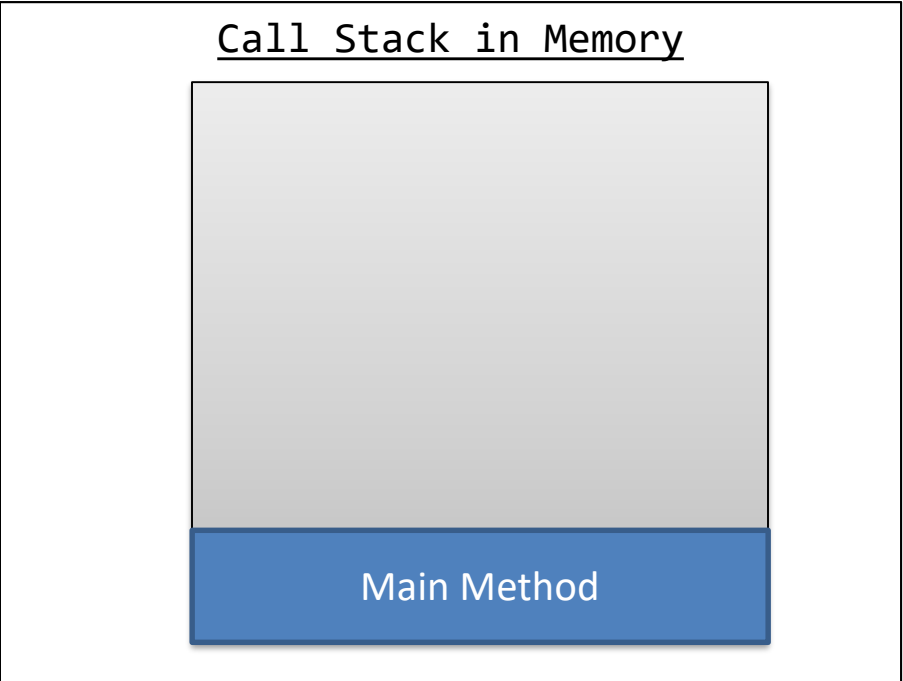
- Solve a problem by solving smaller versions of the same problem
 - Divide and Conquer Algorithms
 - Backtracking
- Recursive Method – a method that calls itself
 - “Loop-like”
 - Call stack
- Recursive Methods Required
 - Halting Condition
 - Recursive Call

Example

```
public static void countDown(int i)
{
    if(i < 0 )//Halting Condition
        return;
    System.out.println(i);
    countDown(i-1);//Recursive Call
}
```

Recursion Count Down

```
public static void countDown(int i)
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Recursion Count Down

5

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Call Stack in Memory

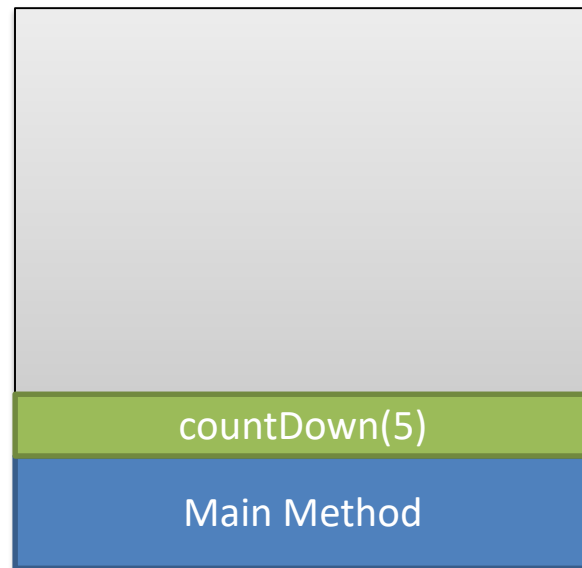


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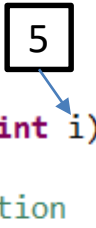
5

Call Stack in Memory



Recursion Count Down

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Call Stack in Memory



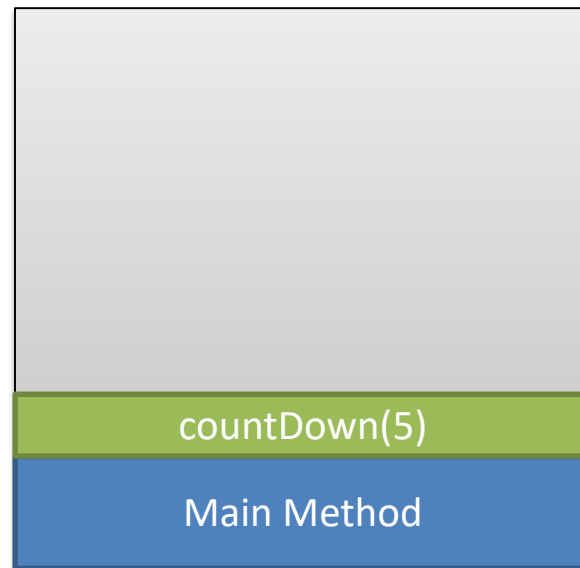
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Console
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Call Stack in Memory

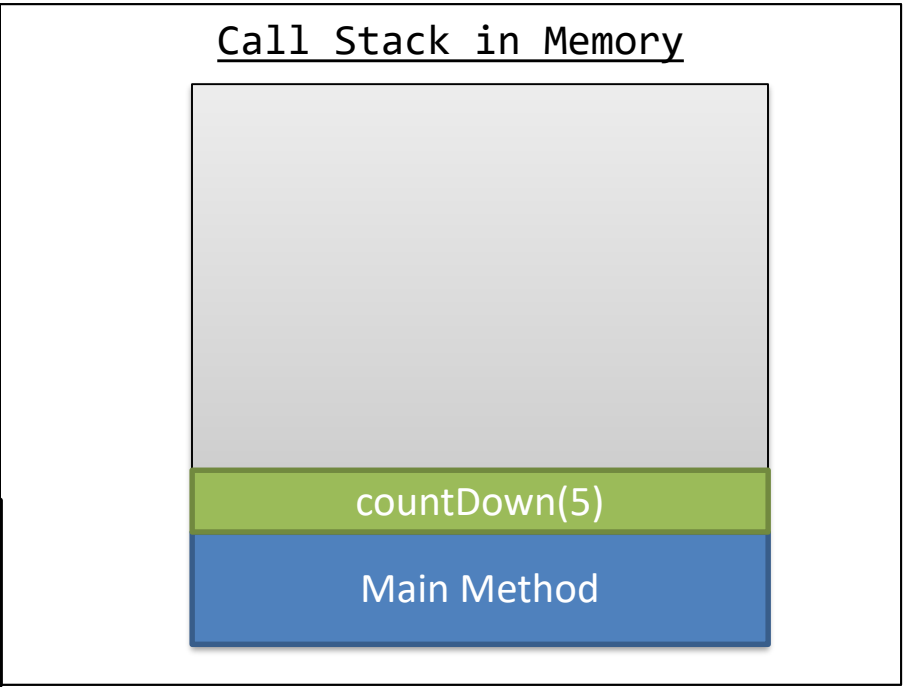


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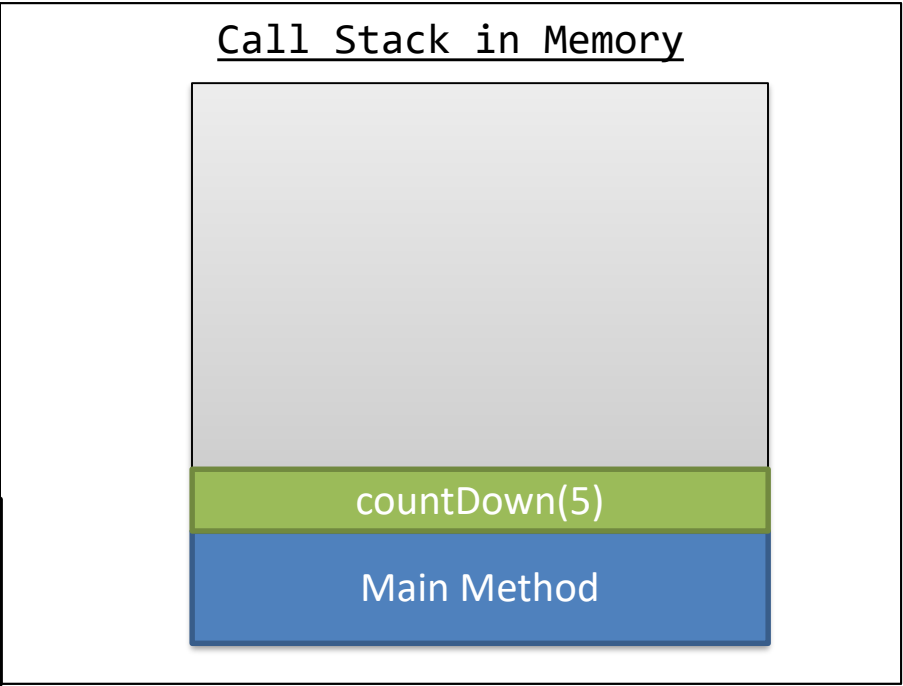


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Console
5



Recursion Count Down

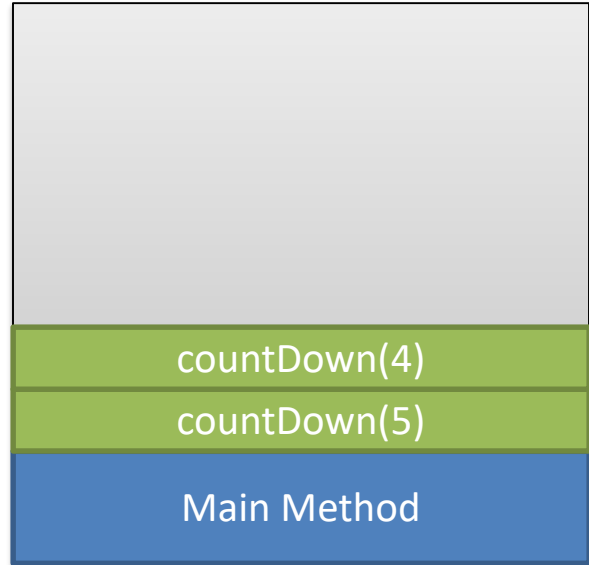
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Console
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Call Stack in Memory



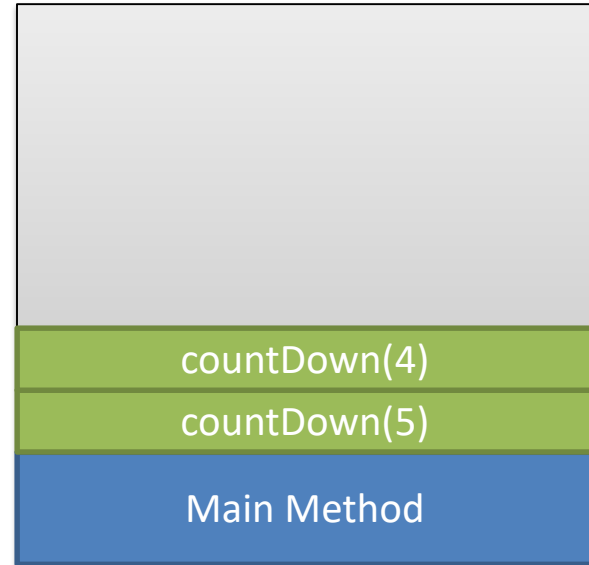
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Console
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Call Stack in Memory



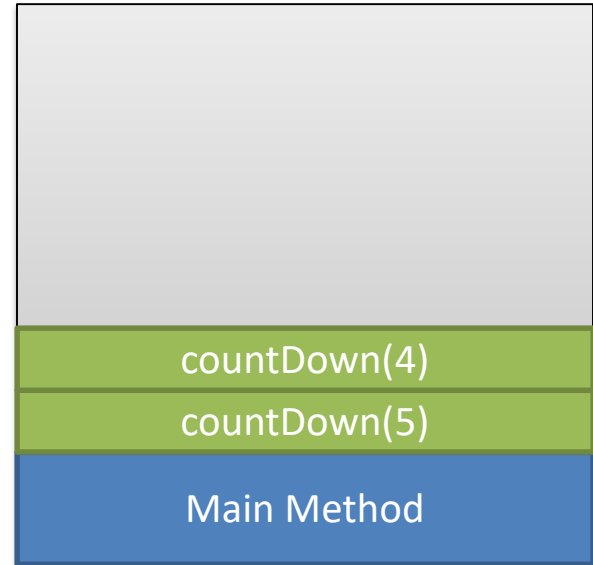
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Console
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4

Call Stack in Memory

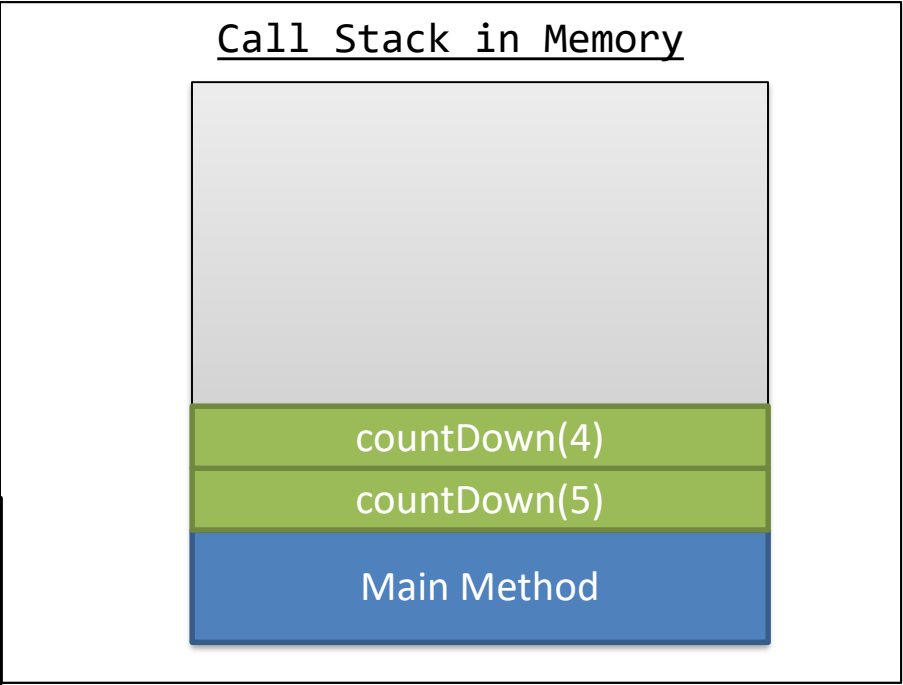


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Console
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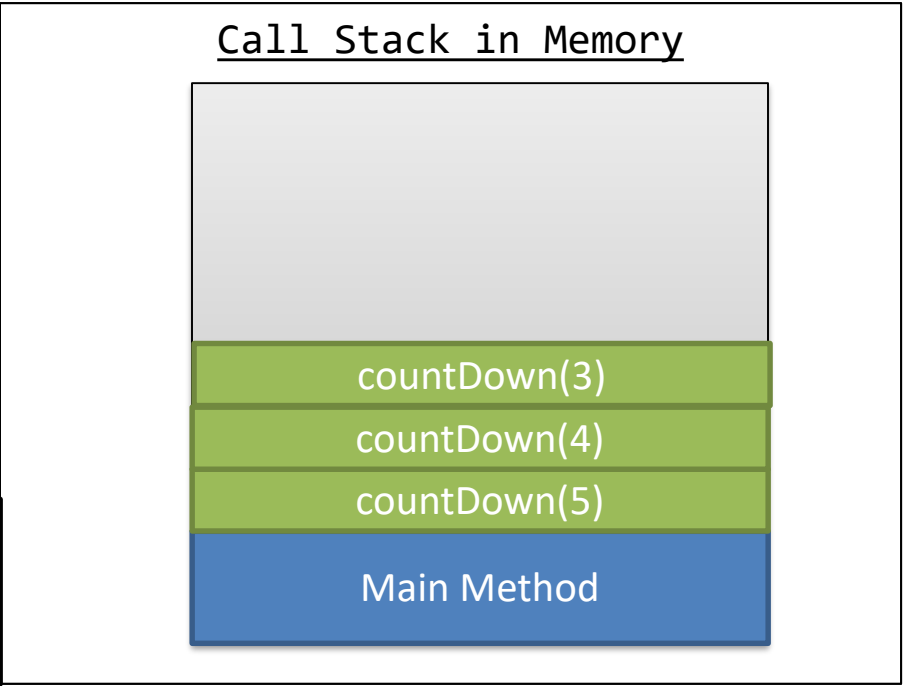


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3

Console
5
4



A Few Recursive Steps
Later...

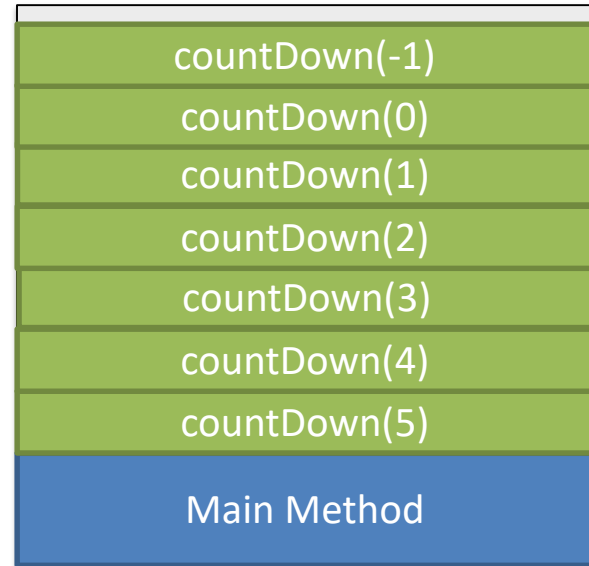
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-1

Console
5
4
3
2
1
0

Call Stack in Memory



Recursion Count Down

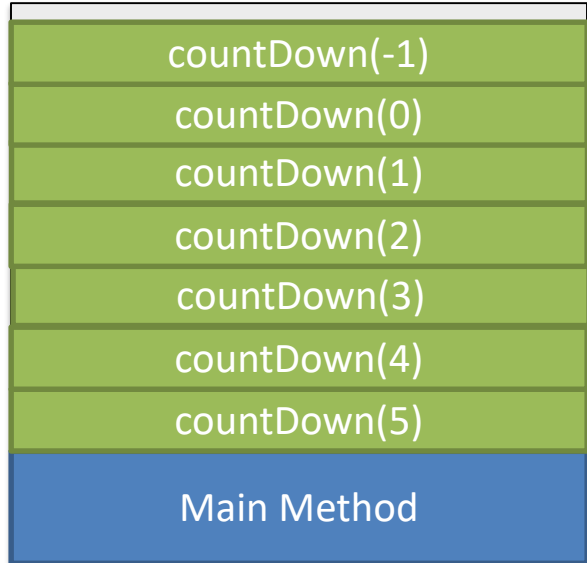
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Console
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Call Stack in Memory



Recursion Count Down

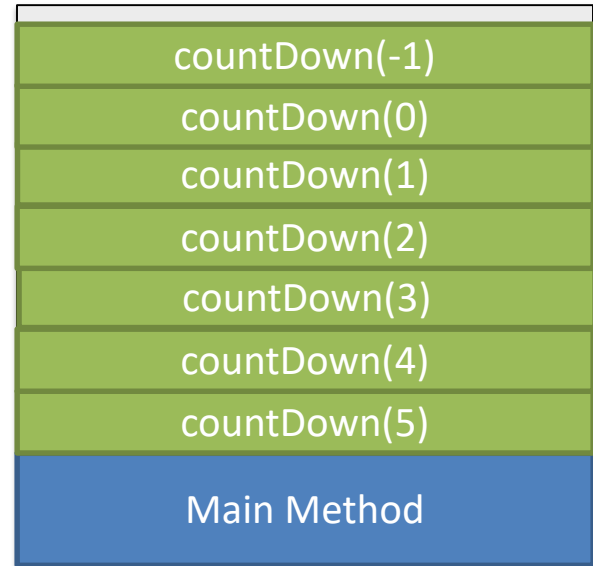
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Console

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Call Stack in Memory



Recursion Count Down

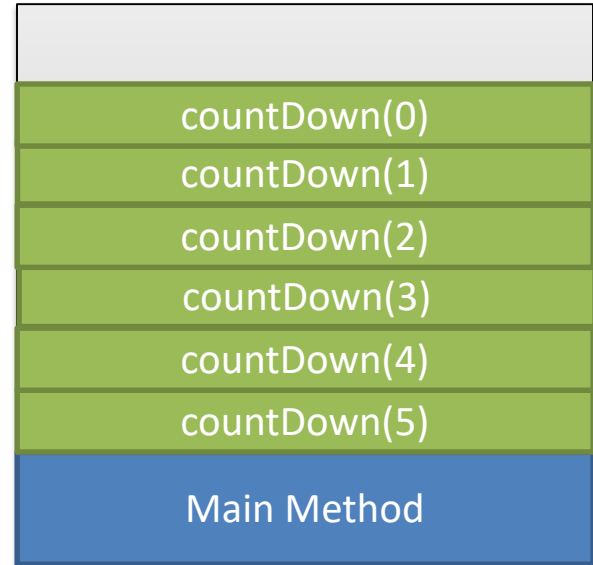
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0

Console

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4
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Call Stack in Memory



Recursion Count Down

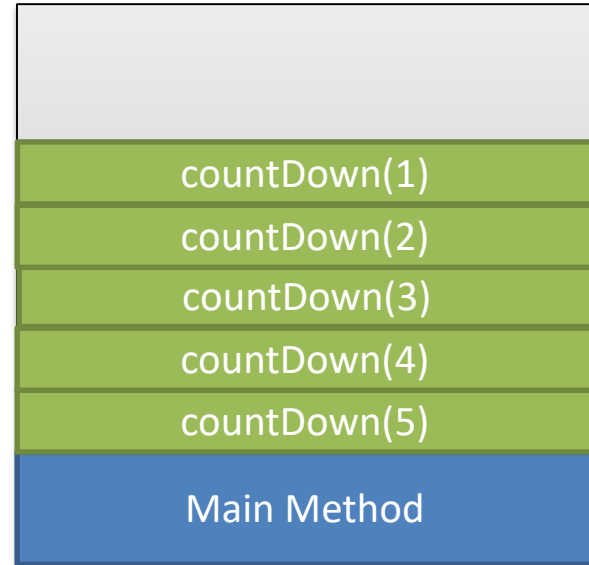
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Console

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Call Stack in Memory



Recursion Count Down

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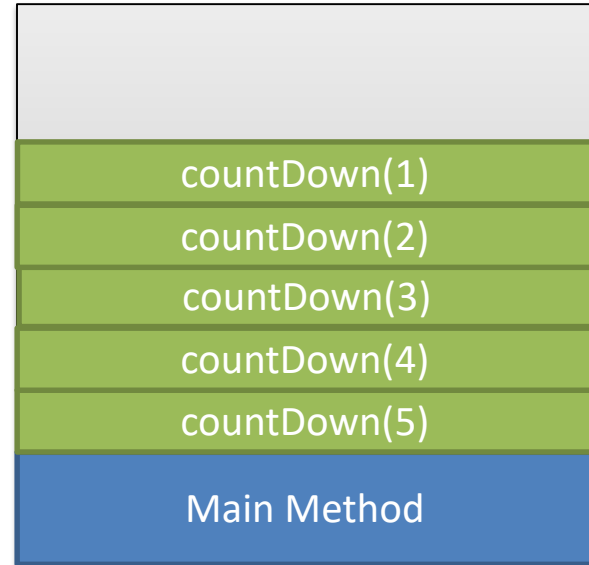
1



Console

```
5
4
3
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```

Call Stack in Memory



Recursion Count Down

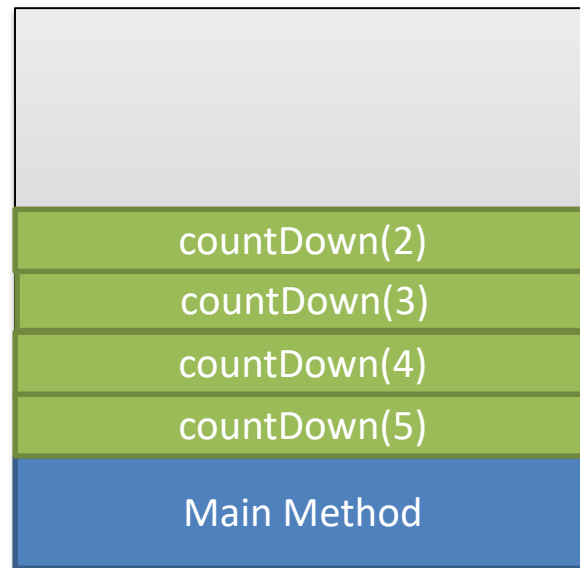
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Call Stack in Memory



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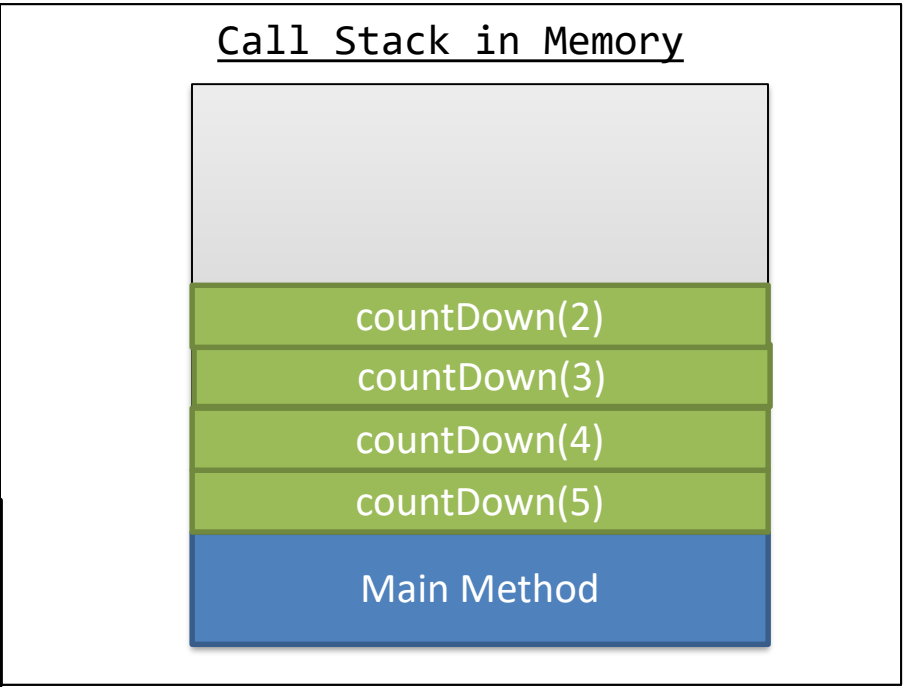
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→

Console

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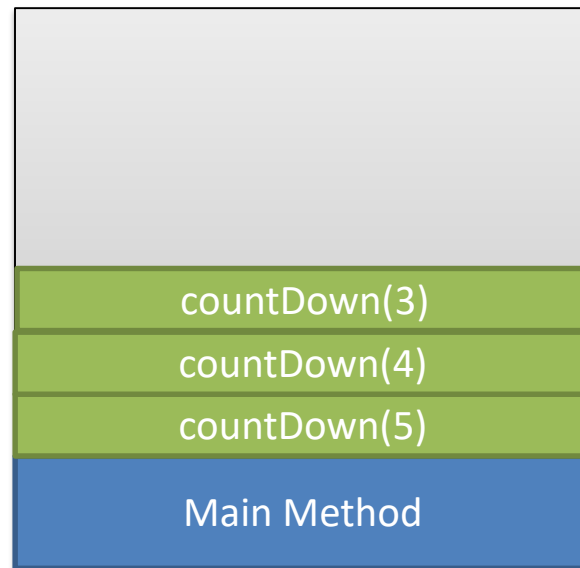
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Console

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Call Stack in Memory



A Few Returns Later...

Recursion Count Down

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Console

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Call Stack in Memory



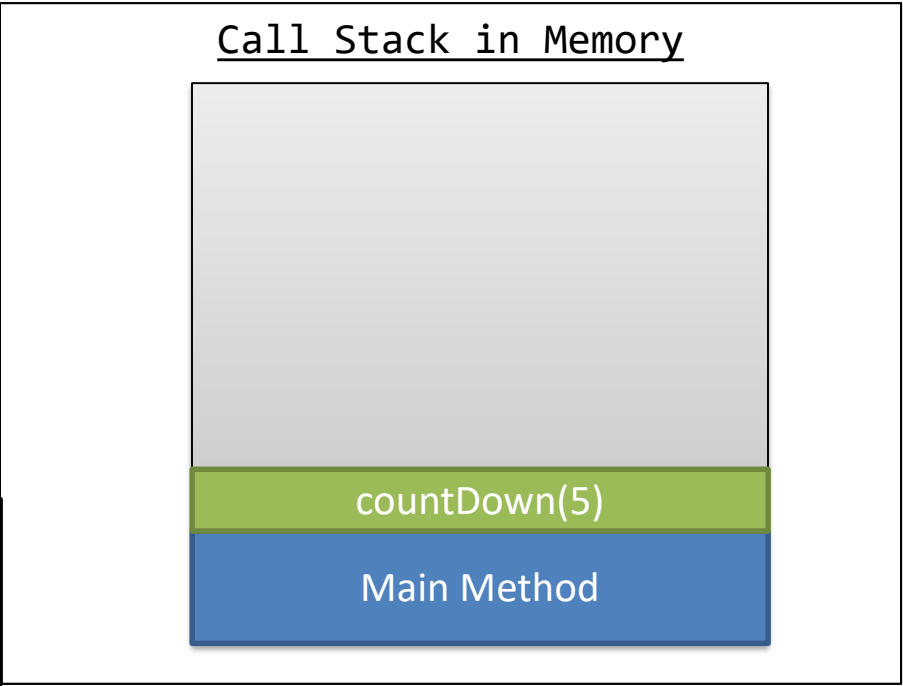
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Console

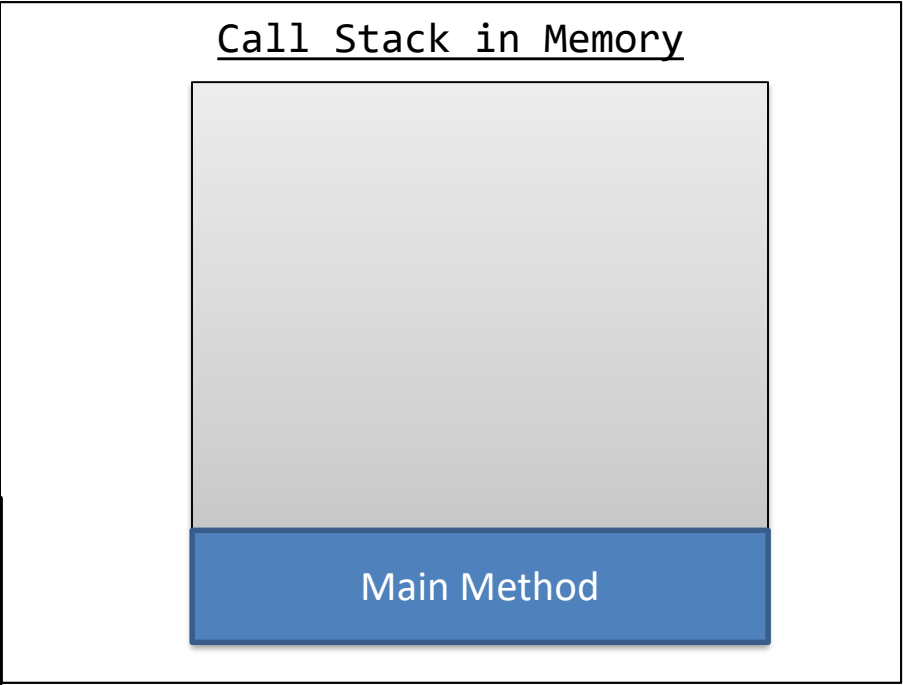
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Console
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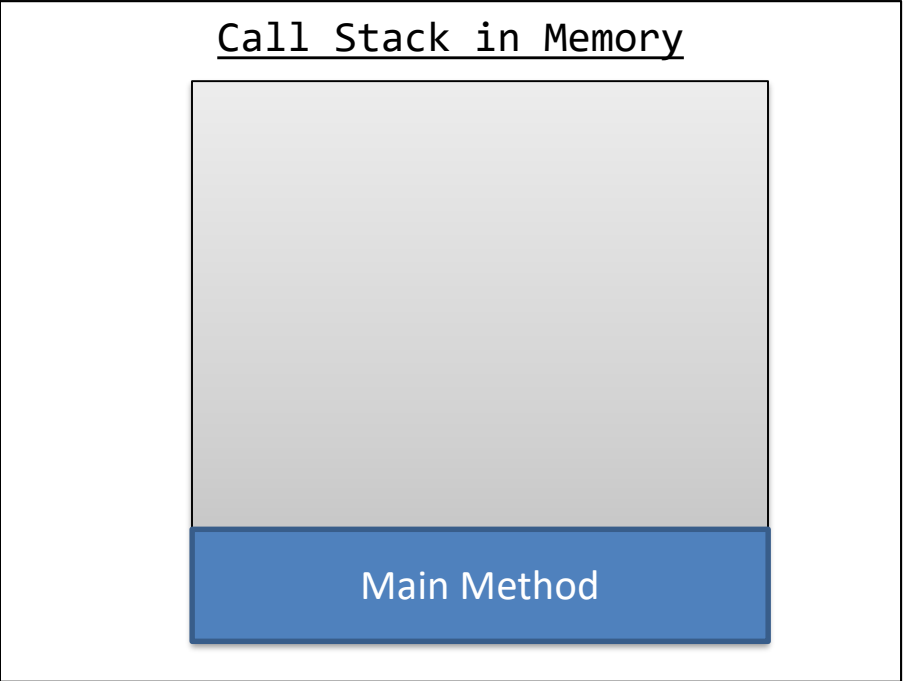


Recursion Factorial

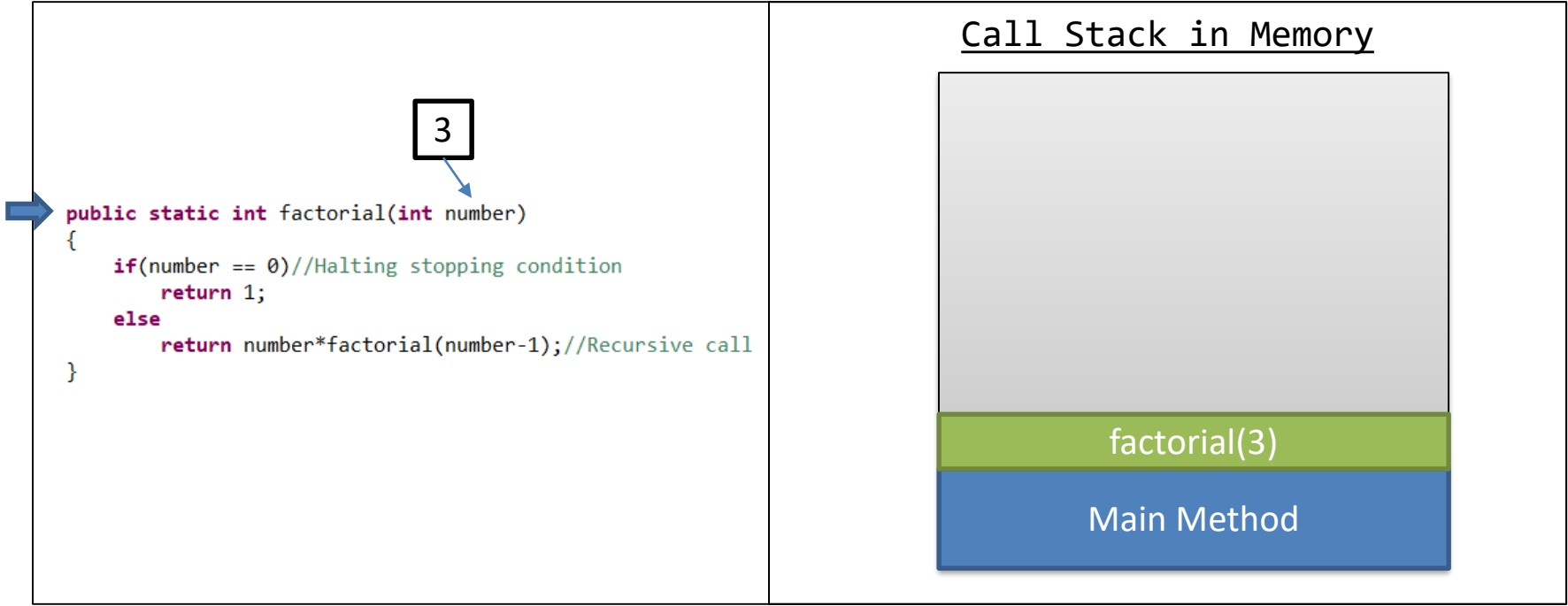
$$n! = \begin{cases} 1 & \text{if } n = 0 \\ (n - 1)! \times n & \text{if } n > 0 \end{cases}$$

Recursion Factorial

```
public static int factorial(int number)
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    if(number == 0)//Halting stopping condition
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Recursion Factorial

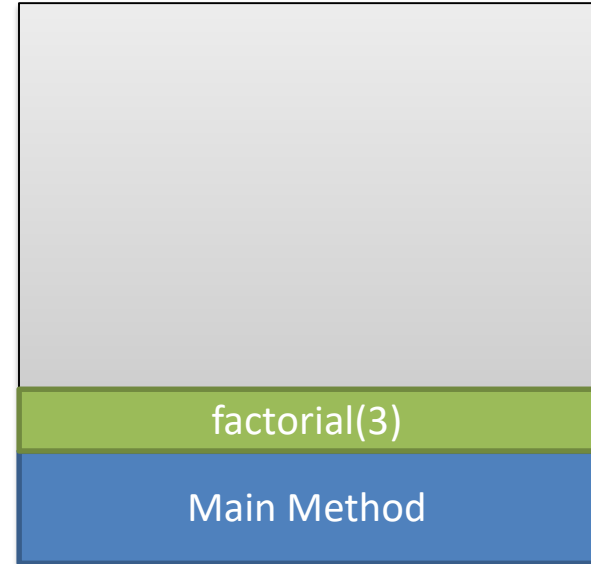


Recursion Factorial

3

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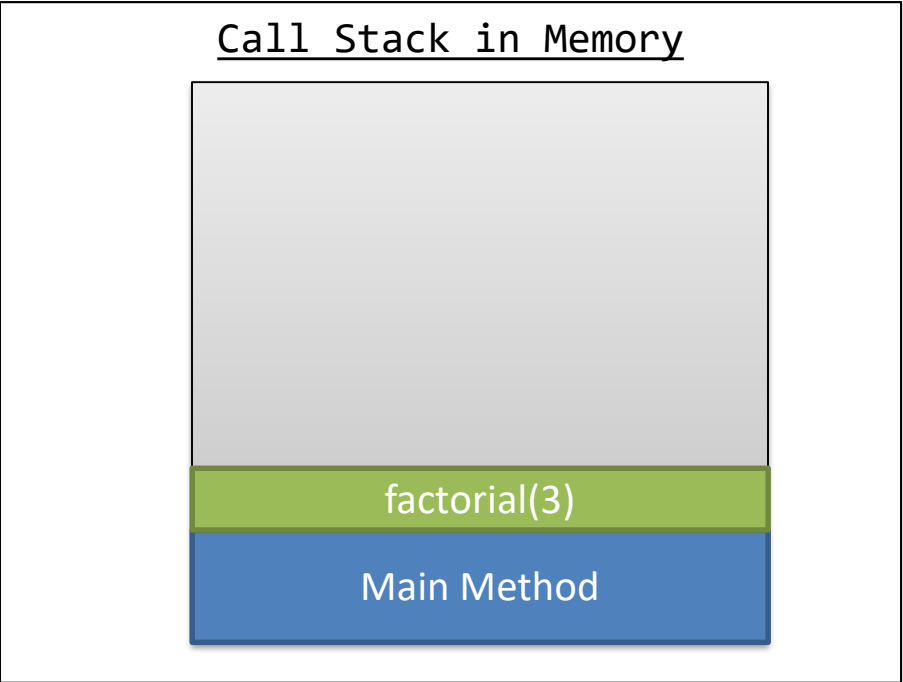
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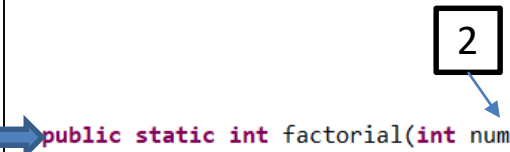
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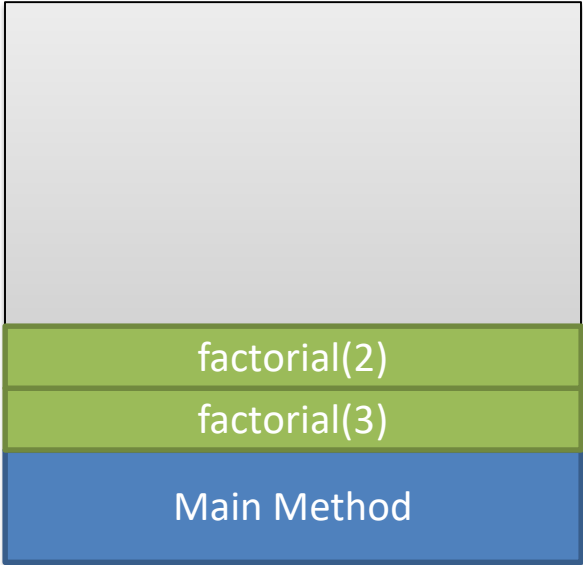


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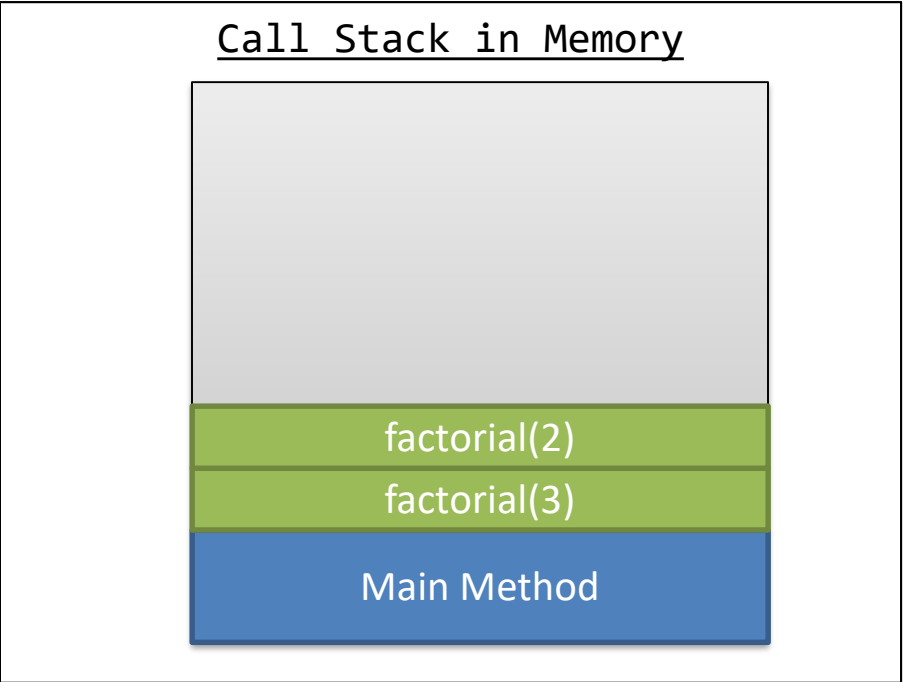
Call Stack in Memory



Recursion Factorial

2

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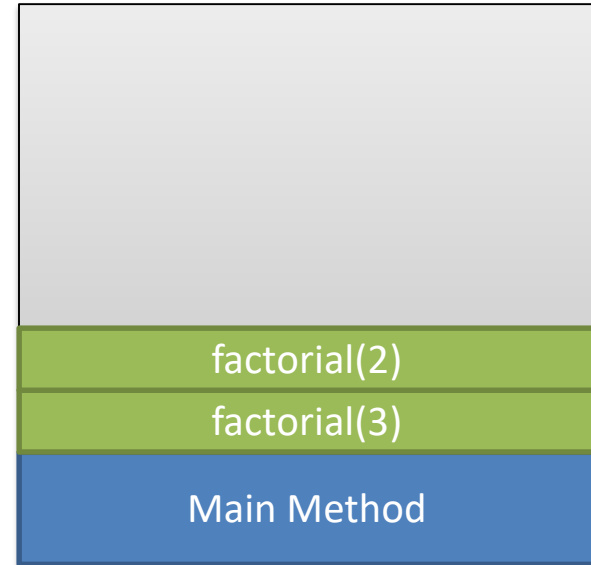


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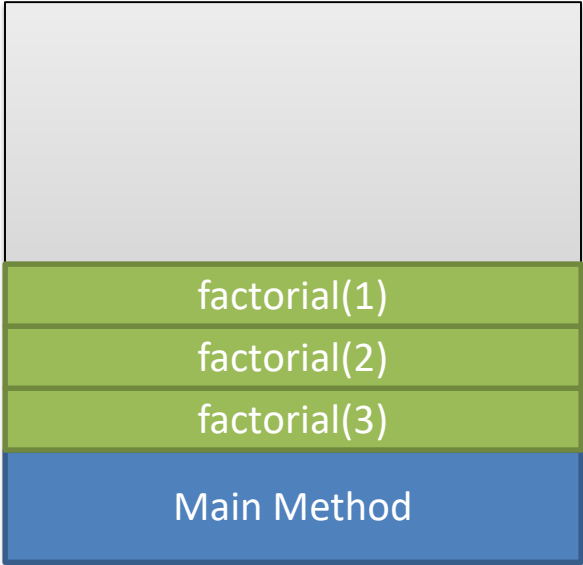


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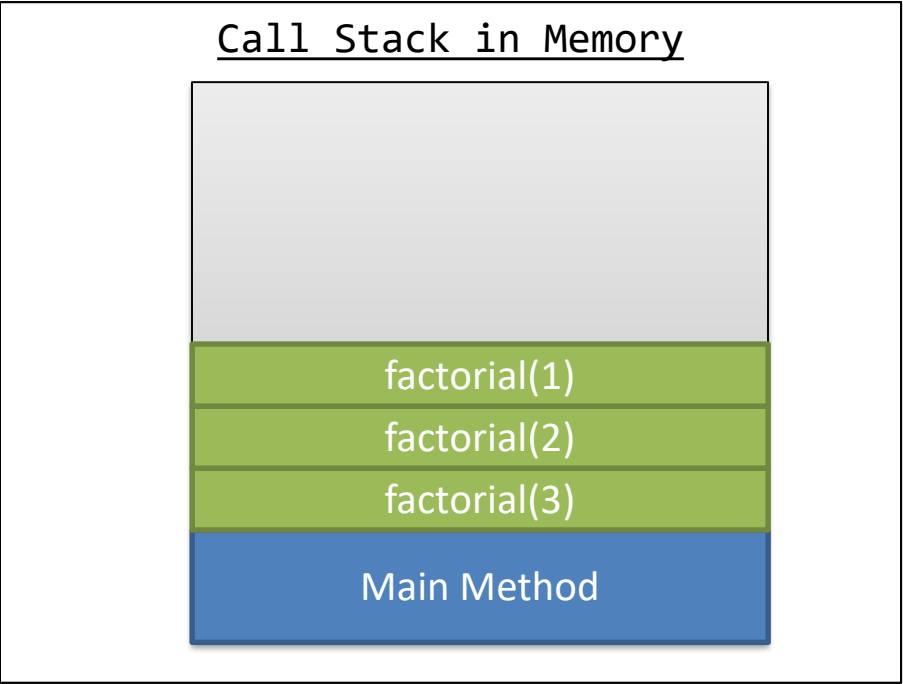
Call Stack in Memory



Recursion Factorial

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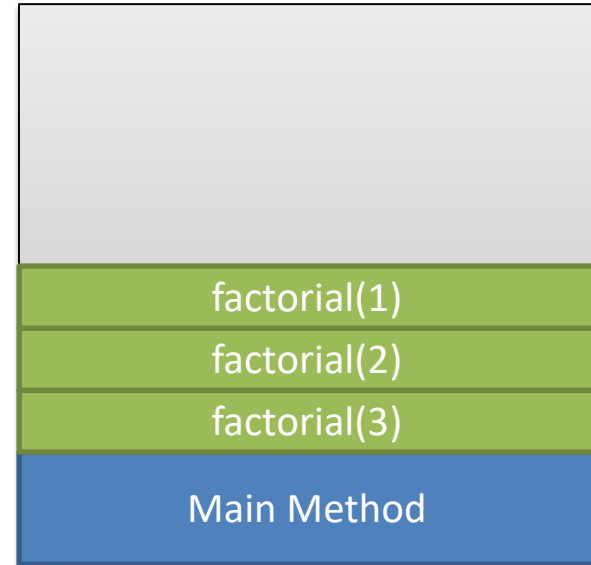


Recursion Factorial


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Call Stack in Memory

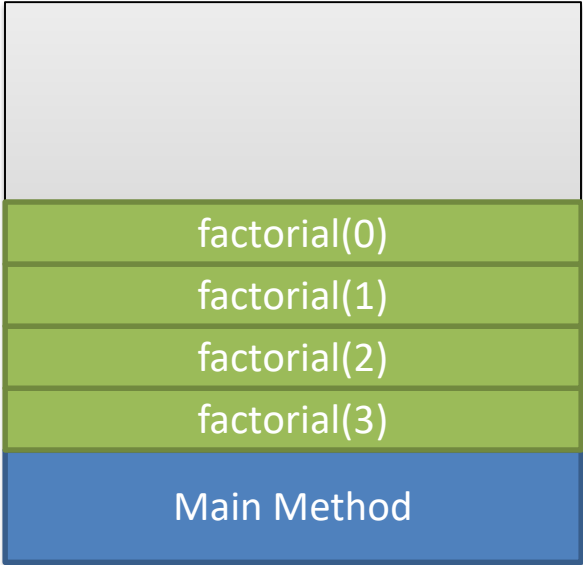


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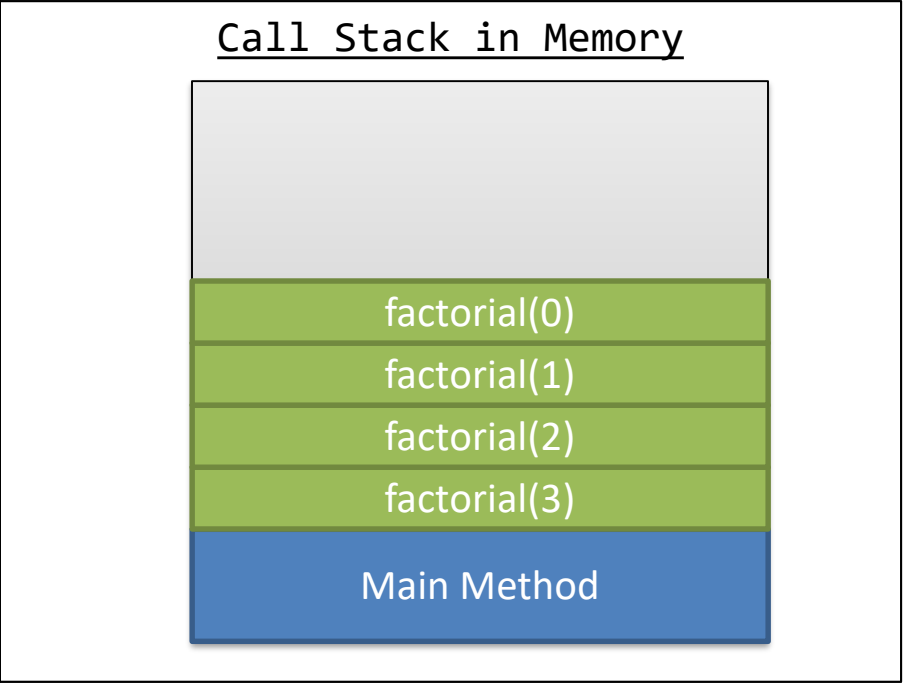
Call Stack in Memory




Recursion Factorial



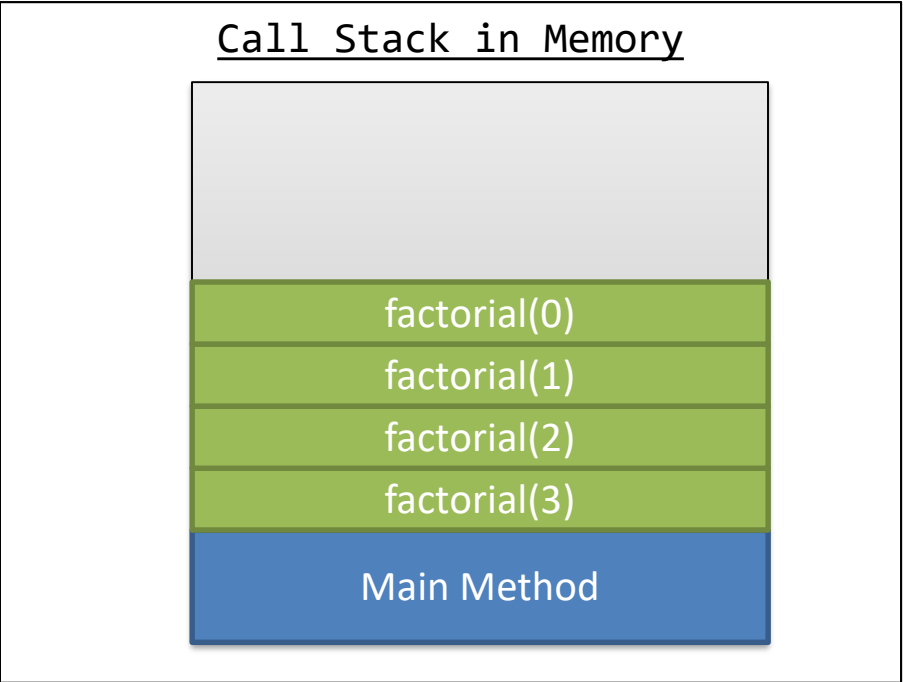
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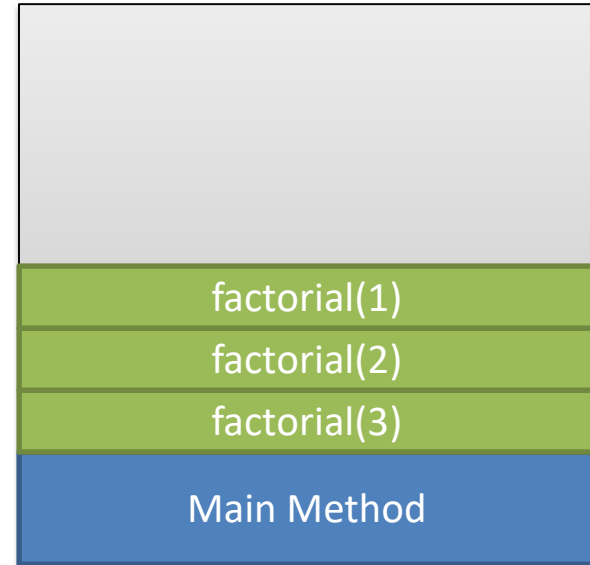


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The diagram illustrates the recursive call process. A box containing the number '1' has an arrow pointing to the recursive call `factorial(number-1)` in the code. Another box containing the number '1' has a bracket pointing to the return value of the recursive call, indicating that the function returns 1 for the base case.

Call Stack in Memory



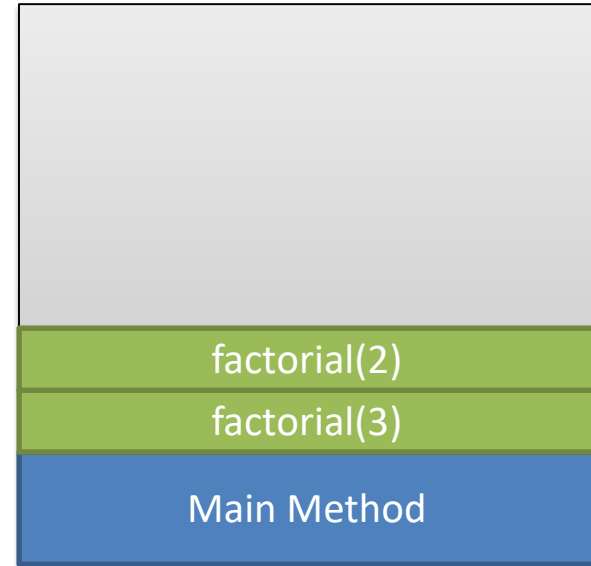
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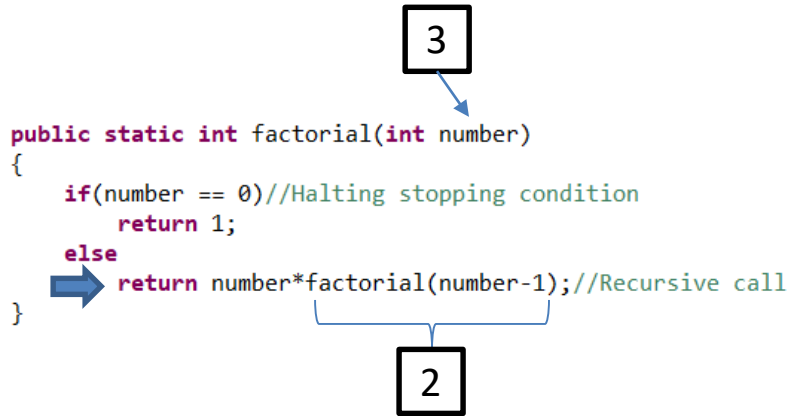
2

1

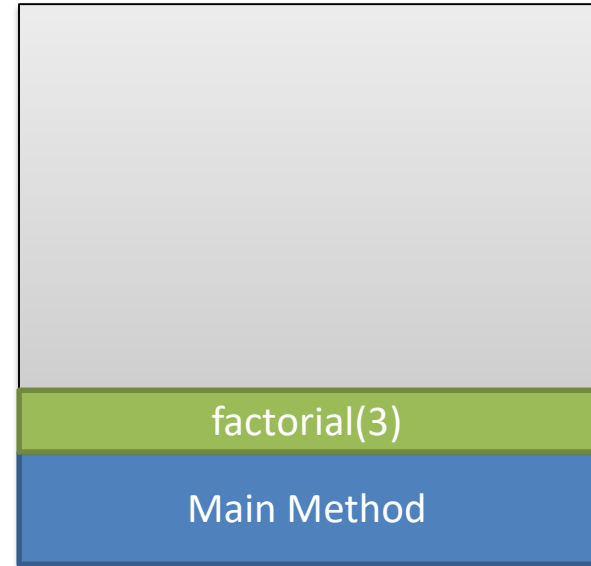
Call Stack in Memory



Recursion Factorial



Call Stack in Memory



Recursion Factorial

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```

Return Value = 6

Call Stack in Memory



Recursion

GCD

$$\text{gcd}(a, 0) = a$$

$$\text{gcd}(a, b) = \text{gcd}(b, a \text{ MOD } b)$$

Recursion Fibonacci

$$F_n = F_{n-1} + F_{n-2}$$

$$F_1 = 1$$

$$F_2 = 1$$

Fibonacci Number (n)	1	2	3	4	5	6	7	8	...
Value	1	1	2	3	5	8	13	21	...

Sierpinski's Carpet

Concept

- Cut area in to 9 equal squares
 - 3 Horizontal
 - 3 Vertical
- Fill in the Center Square
- Repeat this process for the 8 surrounding squares until a limit has been reached
 - Recursive Depth
 - Pixel Limit

Example

