

Example for bucket elimination algorithm

What is the probability that a person has tuberculosis, given that he/she has dyspnoea and has visited Asia recently?

$$P(\alpha=T) = 0.01$$

$$H_{\alpha}(\tau) = P(\tau|\alpha=T)*P(\alpha=T) = (0.0005, 0.0095)$$

ϵ	ξ	$P(\xi \epsilon)$	$H_{\xi}(\epsilon)$
T	T	0.98	1
T	F	0.02	
F	T	0.05	1
F	F	0.95	

τ	β	λ	ϵ	$P(\epsilon \tau,\lambda)$	$H_{\delta}(\epsilon,\beta)$	$H_{\xi}(\epsilon)$	$H_{\epsilon}(\tau,\beta,\lambda)$
T	T	T	T	1	0.9	1	0.9
T	T	T	F	0	0.8	1	
T	T	F	T	1	0.9	1	0.9
T	T	F	F	0	0.8	1	
T	F	T	T	1	0.7	1	0.7
T	F	T	F	0	0.1	1	
T	F	F	T	1	0.7	1	0.7
T	F	F	F	0	0.1	1	
F	T	T	T	1	0.9	1	0.9
F	T	T	F	0	0.8	1	
F	T	F	T	0	0.9	1	0.8
F	T	F	F	1	0.8	1	
F	F	T	T	1	0.7	1	0.7
F	F	T	F	0	0.1	1	
F	F	F	T	0	0.7	1	0.1
F	F	F	F	1	0.1	1	

$\delta=T$	ϵ	β	$H_{\delta}(\epsilon,\beta)=P(\delta=T \epsilon,\beta)$
T	T	T	0.9
T	T	F	0.7
T	F	T	0.8
T	F	F	0.1

τ	β	σ	λ	$P(\lambda \sigma)$	$H_{\epsilon}(\tau,\beta,\lambda)$	$H_{\lambda}(\tau,\beta,\sigma)$
T	T	T	T	0.1	0.9	0.9
T	T	T	F	0.9	0.9	
T	T	F	T	0.01	0.9	0.9
T	T	F	F	0.99	0.9	
T	F	T	T	0.1	0.7	0.7
T	F	T	F	0.9	0.7	
T	F	F	T	0.01	0.7	0.7
T	F	F	F	0.99	0.7	
F	T	T	T	0.1	0.9	0.81
F	T	T	F	0.9	0.8	
F	T	F	T	0.01	0.9	0.801
F	T	F	F	0.99	0.8	
F	F	T	T	0.1	0.7	0.16
F	F	T	F	0.9	0.1	
F	F	F	T	0.01	0.7	0.106
F	F	F	F	0.99	0.1	

τ	β	σ	$P(\beta \sigma)$	$P(\sigma)$	$H_{\lambda}(\tau,\beta,\sigma)$	$H_{\sigma}(\tau,\beta)$
T	T	T	0.6	0.5	0.9	0.405
T	T	F	0.3	0.5	0.9	
T	F	T	0.4	0.5	0.7	0.385
T	F	F	0.7	0.5	0.7	
F	T	T	0.6	0.5	0.81	0.36315
F	T	F	0.3	0.5	0.801	
F	F	T	0.4	0.5	0.16	0.0691
F	F	F	0.7	0.5	0.106	

τ	β	$H_{\sigma}(\tau,\beta)$	$H_{\beta}(\tau)$
T	T	0.405	0.79
T	F	0.385	
F	T	0.36315	0.43225
F	F	0.0691	

τ	$H_{\alpha}(\tau)$	$H_{\beta}(\tau)$	$H_{\alpha}(\tau)*H_{\beta}(\tau)$	$P(\tau \alpha=T, \delta=T)$
T	0.0005	0.79	0.000395	0.088
F	0.0095	0.43225	0.004106375	0.912