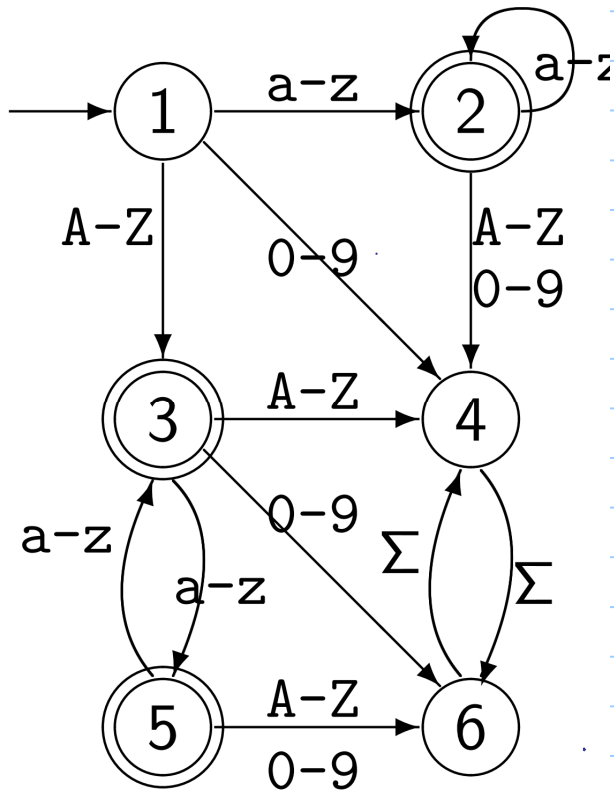


Details of minimization example from slide 31 Lex J. Berthold



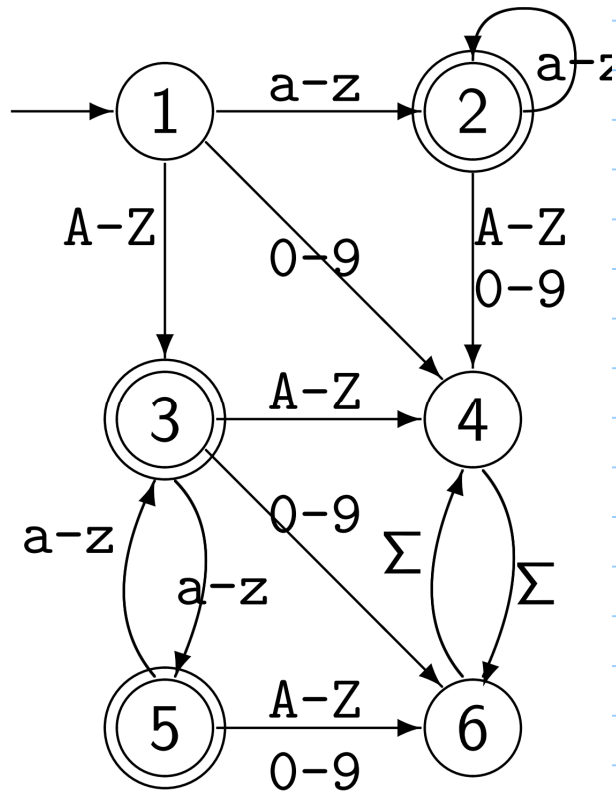
$$G_1 = F = \{2, 3, 5\}$$

$$G_2 = S \setminus F = \{1, 4, 6\}$$

Both unmarked. Pick one, say G_1 .
 Compute transition table:

G_1	a-z	A-Z	0-9
2	G_1	G_2	G_2
3	G_1	G_2	G_2
5	G_1	G_2	G_2

consistent: mark &
 do not split



Select the remaining unmarked group,
 $G_2 = \{1, 4, 6\}$

G_2 a-z A-Z 0-9

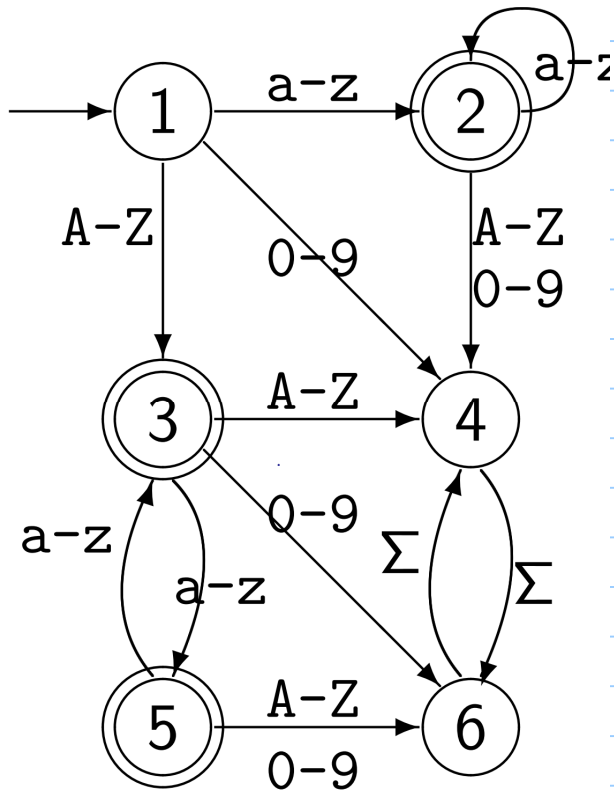
1	G_1	G_1	G_2
4	G_2	G_2	G_2
6	G_2	G_2	G_2

not consistent;
 split into maximal
 consistent subgroups
 and unmark all groups

$G_3 = \{1\}$

(A singleton: cannot be split)

$G_4 = \{4, 6\}$



Consider $G_4 = \{4, 6\}$. Compute its transition table

G_4	a-z	A-Z	0-9
-------	-----	-----	-----

4	G_4	G_4	G_4
6	G_4	G_4	G_4

consistent:
mark it.

Check G_1 for consistency.

(Recall that groups are now:

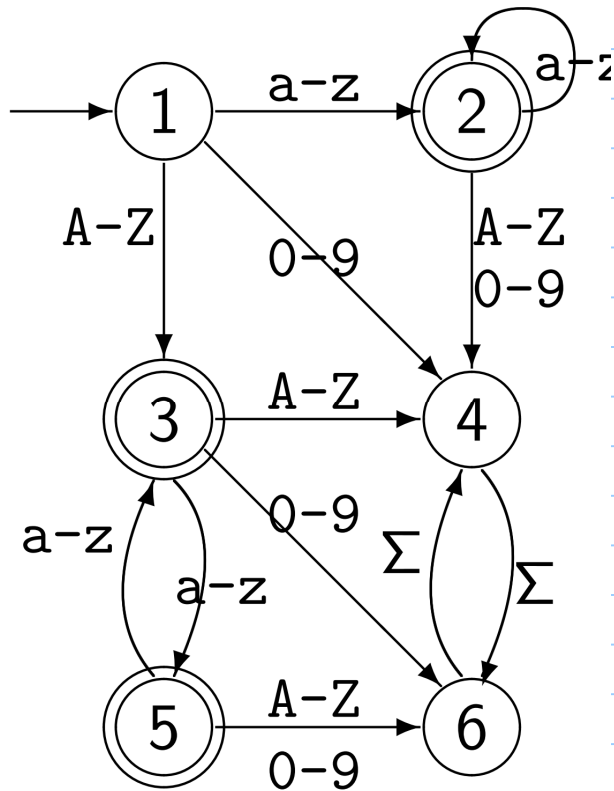
$G_1 = \{2, 3, 5\}$, $G_2 = \{1\}$, $G_4 = \{4, 6\}$, and G_1 is unmarked)

G_1	a-z	A-Z	0-9
-------	-----	-----	-----

2	G_1	G_4	G_4
3	G_1	G_4	G_4
5	G_1	G_4	G_4

consistent:

mark it.



All groups are either marked or singletons
 So, there is a minimal equivalent DFA
 with states $q_3 (\{1\})$, $q_4 (\{4,6\})$, $q_1 (\{2,3,5\})$:

