

**Errata**  
**Robust Process Control**  
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- p. i "Department of Chemical and Nuclear Engineering" should be "Chemical Engineering"
- p. 55 Line-3 "Frank (1984)" should be "Frank (1974)"
- p. 58 Thm. 4.1-2 and all of p. 59

**Theorem 4.1-2.** *The  $H_2$ -optimal complementary sensitivity function*

$$\bar{\eta} = \tilde{p}\tilde{q} = \tilde{p}_A v_M^{-1} \{\tilde{p}_A^{-1} v_M\}_* \quad (4.1 - 8)$$

*has the following properties:*

1. *The poles of  $\bar{\eta}$  are among the mirror images of the plant RHP zeros and among the zeros of  $v_M$ .*
2.  *$\bar{\eta}$  has RHP zeros at the plant RHP zeros.  $\bar{\eta}$  can have additional RHP zeros.*

*Proof.*

1. The potential poles of  $\bar{\eta}$  are the poles of  $\tilde{p}_A$ , the zeros of  $v_M$  and the poles of  $\{\tilde{p}_A^{-1} v_M\}_*$ , which are the poles of  $v_M$ . However, the poles of  $v_M$  are cancelled by zeros of  $v_M^{-1}$  premultiplying  $\{\cdot\}_*$ .
2.  $\bar{\eta}$  has RHP zeros at  $\tilde{p}_A$ . Additional RHP zeros can arise from  $\{\tilde{p}_A^{-1} v_M\}_*$ . □

RHP zeros are generally considered as "bad" for performance. However, 2. implies that depending on the input  $v_M$  the optimal controller  $\tilde{q}$  can sometimes *add* RHP zeros.

**Example 4.4-1.**

$$\tilde{p} = \tilde{p}_A = \frac{-s+2}{s+2}, v_M = \frac{s+1}{s} \quad (4.1 - 9)$$

$$\tilde{q} = \frac{s}{s+1} \left\{ \frac{s+2}{-s+2} \frac{s+1}{s} \right\}_* = \frac{s}{s+1} \left\{ -1 + \frac{1}{s} + \frac{6}{-s+2} \right\}_* = \frac{-s+1}{s+1} \quad (4.1 - 10)$$

$$\bar{\eta} = \frac{(-s+2)(-s+1)}{(s+2)(s+1)} \quad (4.1 - 11)$$

The controller  $\tilde{q}$  added a RHP zero at  $(+1,0)$ . □

p. 64 Proof.

Proof. Assume  $p_A = \frac{-s+\zeta}{s+\zeta^H} \cdot \frac{-s+\zeta^H}{s+\zeta}$ .

$$\begin{aligned} \|e\|_2^2 &= \frac{1}{2\pi i} \int_{-i\infty}^{+i\infty} |(1-p_A)s^{-1}|^2 ds \\ &= \frac{1}{2\pi i} \int_{-i\infty}^{+i\infty} \left[ 2 - \frac{-s+\zeta}{s+\zeta^H} \cdot \frac{-s+\zeta^H}{s+\zeta} - \frac{s+\zeta^H}{-s+\zeta} \cdot \frac{s+\zeta}{-s+\zeta^H} \right] |s^{-1}|^2 ds \\ &= \text{Res}_{s=\zeta} \left[ -\frac{s+\zeta^H}{-s+\zeta} \cdot \frac{s+\zeta}{-s+\zeta^H} \cdot \frac{1}{s^2} \right] + \text{Res}_{s=\zeta^H} \left[ -\frac{s+\zeta^H}{-s+\zeta} \cdot \frac{s+\zeta}{-s+\zeta^H} \cdot \frac{1}{s^2} \right] \\ &= \frac{4\text{Re}(\zeta)}{|\zeta|^2} \quad \square \end{aligned}$$

p. 68 Fig. 4.3-2

“1:  $\lambda = 10$ ” should be “1:  $\lambda = 0.1$ ”  
 “3:  $\lambda = 0.1$ ” should be “3:  $\lambda = 10$ ”

p. 75 (4.5-1)

“ $|\tilde{p}\tilde{q}f\bar{\ell}_m|$ ” should read “ $|\tilde{p}\tilde{q}\bar{\ell}_m|$ ”

p. 86 Line-5

“unstable systems the sensitivity function” should be  
 “unstable systems the complementary sensitivity function”

p. 91 Middle

“ $\|(1-p\tilde{q}v)\|_2^2$ ” should be “ $\|(1-p\tilde{q}v)\|_2^2$ ”

p. 116-117

Table should be moved down on page  
 (placement same as pages 62, 63)

p. 122 Fig. 6.1-4

“ $\lambda$ ” should be “ $\lambda/\Theta$ ”  
 “TIME” should be “TIME/ $\Theta$ ”

p. 143 2nd par.

“Out” should be “Our”

p. 206 (10.1-8)

$$\pi(s) = \prod_{i=1}^{n_p} (s - \pi_i) = \det(sI - A)$$

p. 220 Line-2

“Let the number of open-loop unstable poles of  $PC$ ”  
 should read “Let the total number of open-loop unstable  
 poles of  $P$  and  $C$ ”

p. 225 (10.3-13)

$$“= \int_{-\infty}^{\infty}” \text{ should be } “= \frac{1}{2\pi} \int_{-\infty}^{\infty}”$$

p. 229 Line-14

“certainty” should be “certainly”

p. 239 2nd par. from bottom

replace all “ $\| \|$ ” by “ $\| \|_\nu$ ”

p. 240	Middle	“frequencies where $\ell_O(\omega) \geq 1$ ” should be “frequencies where $\bar{\ell}_O(\omega) \geq 1$ ”
p. 241	Eqn. above (11.1-15)	“ $\sigma(\tilde{P})$ ” should be “ $\bar{\sigma}(\tilde{P})$ ”
p. 244	Last line	“ $W_2 = \tilde{P}\ell_I$ ” should be “ $W_2 = \tilde{P}\bar{\ell}_I$ ”
p. 250	Line-5	“that the optimization problem is convex” should be “that after a nonlinear variable transformation the optimization problem is convex”
p. 272	Table 11.3-1	“-538.2” should be “-583.8”
p. 280	(11.4-12)	$G = \begin{pmatrix} 0 & 0 & -I \\ P & 0 & -P \\ P & I & -P \end{pmatrix}$ should be $G = \begin{pmatrix} 0 & 0 & -I \\ \tilde{P} & 0 & -\tilde{P} \\ \tilde{P} & I & -\tilde{P} \end{pmatrix}$
p. 280	Example 11.4-1	With the exception of (11.4-11) we assume $w = 1$ .
p. 283	Last line of Proof	“=” should be “<”
p. 284	Table 11.4-1 Case 1	“ $\bar{\sigma}B$ ” should be “ $\bar{\sigma}(B)$ ”
p. 284	(11.4-23) (11.4-24) Eq. after (11.4-24)	“ $\leq$ ” should be “<” second “<” should be “ $\leq$ ” “ $\leq$ ” should be “<”
p. 285	Proof on top half of page	for consistency with the rest of the other theorems replace “ $k$ ” by “ $1/k$ ”

- p. 286 Top “(ii)  $H = hI : \mu^2 \begin{pmatrix} 0 & P^{-1} \\ P & P \end{pmatrix} = 1$ ”  
should read  
“(ii)  $H = hI : \mu^2 \begin{pmatrix} 0 & \tilde{P}^{-1} \\ \tilde{P} & \tilde{P} \end{pmatrix} = 1$ ”
- p. 286 Just before (11.4-32) “Theorem 12.4-1” should be “Theorem 11.4-1”
- p. 346 par. preceding  
(13.3-8) “ $P$ ” should be “ $\tilde{P}$ ”
- p. 357 Line-4 “Palozoglu” should be “Palazoglu”
- p. 365 Middle  
(14.3-2) “Corollary 14.3-4” should be “Corollary 14.3-5”  
“ $sd(s)$ ” should be “ $s^n d^n(s)$ ”
- p. 366 top part of page

Because  $G(s)$  is stable the closed-loop system will be stable only if all the coefficients of

$$\det(sd(s)I + kN(s)) = s^n d^n(s) + \dots + k^n \det N(0) = 0 \quad (14.3 - 3)$$

are positive. If  $G(s)$  is proper, the coefficient of the highest power of  $s$  in (14.3-3) will be the coefficient of the highest power of  $s$  in  $d(s)$ . This coefficient will be positive because of the stability assumption. The constant coefficient is  $\det(kN(0))$  and therefore for closed-loop stability it is required that  $\det(N(0)) > 0$  and  $\det(G(0)) > 0$ .  $\square$

- p. 371 Corollary 14.4-2 “The stable system  $P$  is DIC if”  
should read “The stable system  $P$  is IC if”
- p. 377 Table 14.4-1  $p_{12}$  “ $e^{-3.70s}$ ” should be “ $e^{-3.79s}$ ”  
 $p_{23}(0)$  “5.94” should be “5.984”  
 $p_{31}(0)$  “0.204” should be “0.0204”  
 $p_{32}(0)$  “0.33” should be “-0.33”
- p. 377 Fig. 14.4-2 “ $E$ ” should be “ $L_H$ ”
- p. 385 (14.5-22) “ $= I$ ” should be “ $= 1$ ”
- p. 397 Line 5 “Let the number of open-loop unstable poles of  
 $P_\gamma^* C$ ” should read “Let the total number of open-loop

		unstable poles of $P_\gamma^*$ and $C$ "
p. 466	Table A.4-1, Column "C", 2nd row	"16.023" should be "-16.023"
p. 473	Line 5	"M. Latchman" should be "H. Latchman"
Back cover		" $H_\infty$ optional" should be " $H_\infty$ optimal"