

$S \rightarrow L = R \mid R$
 $L \rightarrow *R \mid \text{id}$
 $R \rightarrow L$

FIRST	FOLLOW
$S \mid *, \text{id}$	$S \mid \$, =$
$L \mid *, \text{id}$	$L \mid \$, =$
$R \mid *, \text{id}$	$R \mid \$, =$

SLR(1) states (sets of LR(0) items)

S_0 = start state
 $S \rightarrow \cdot L = R$
 $S \rightarrow \cdot R$
 $L \rightarrow \cdot *R$
 $L \rightarrow \cdot \text{id}$
 $R \rightarrow \cdot L$

$S_1 = \text{trans}(S_0, R) : S \rightarrow R \cdot$
 $S_2 = \text{trans}(S_0, *) : L \rightarrow * \cdot R$
 $R \rightarrow \cdot L$
 $L \rightarrow \cdot *R$
 $L \rightarrow \cdot \text{id}$

$\text{action}[S_1, =] = \text{"shift } S_1"$
 $\text{action}[S_2, =] = \text{"reduce } R \rightarrow L"$
 because $'=' \in \text{FOLLOW}(R)$
 shift-reduce conflict.

$\text{action}[S_2, \text{id}] = \text{"shift } S_3"$
 $S_3 = \text{trans}(S_2, \text{id}) : L \rightarrow * \text{id} \cdot$
 $R \rightarrow \cdot L$
 $L \rightarrow \cdot *R$
 $L \rightarrow \cdot \text{id}$

(Canonical) LR(1) parser:

state is a set of LR(1) items.

An LR(1) item is a pair:

$$\left[\frac{A \rightarrow \alpha \cdot \beta}{\text{LR(1) item}}, a \right]$$

"core" "lookahead"
 (or β)

Intuition:

If this item is in the current state, then that means that we could be working our way through $A \rightarrow \alpha \beta$ (as before) and we expect to see a as the lookahead when it is time to reduce.

If $[A \rightarrow \alpha \cdot, a]$ is in the current state, then only reduce if we see $\underline{a}$ on the lookahead.

Start state (if $S' \rightarrow S$ for augmenting grammar)

$\text{closure}(S' \rightarrow \cdot S, \$)$
 $\text{closure}(S)$ = set of LR(1) items:

if $[A \rightarrow \alpha \cdot B \beta, a] \in S$,
 then add $[B \rightarrow \cdot \gamma, b]$
 for all B -productions $B \rightarrow \gamma$
 and all $b \in \text{FIRST}(\beta a)$
 (apply repeatedly until can't add anything more)

$\text{trans}(S, X)$:
 For each item in S
 of the form $[A \rightarrow \alpha \cdot X \beta, a]$
 put $[A \rightarrow \alpha X \cdot \beta, a]$
 into $\text{trans}(S, X)$
 then take the closure

$\text{action}[S, a]$:
 if $[A \rightarrow \alpha \cdot a \beta, b] \in S$,
 then set $\text{action}[S, a] = \text{"shift } T"$
 where $T = \text{trans}(S, a)$
 (same as before)

If $[A \rightarrow \alpha \cdot, \underline{b}] \in S$,
 then set
 $\text{action}[S, \underline{b}] = \text{"reduce } A \rightarrow \alpha"$

$\text{goto}(S, A) := \text{trans}(S, A)$
 (same as before)

$S \rightarrow L = R \mid R$
 $L \rightarrow *R \mid id$
 $R \rightarrow L$

S_0 = start state:

$S \rightarrow \cdot L = R, \$$
 $S \rightarrow \cdot R, \$$
 $L \rightarrow \cdot *R, =$
 $L \rightarrow \cdot id, =$
 $R \rightarrow \cdot L, \$ \leftarrow \text{FIRST}(\$)$
 $L \rightarrow \cdot *R, \$$
 $L \rightarrow \cdot id, \$$

$S_1 = \text{trans}(S_0, L):$

$S \rightarrow L \cdot = R, \$$
 $R \rightarrow L \cdot, \$$

no conflict!

$\text{action}[S_1, =] = \text{"shift T"}$
 $T = \text{trans}(S_1, =)$
 $\text{action}[S_1, \$] = \text{"reduce } R \rightarrow L"$

$S_2 = \text{trans}(S_0, R): S \rightarrow R \cdot, \$$

$S_3 = \text{trans}(S_0, *):$

$L \rightarrow * \cdot R, =$
 $L \rightarrow * \cdot R, \$$

$R \rightarrow \cdot L, =$
 $R \rightarrow \cdot L, \$$
 $L \rightarrow \cdot *R, =$
 $L \rightarrow \cdot *R, \$$
 $L \rightarrow \cdot id, =$
 $L \rightarrow \cdot id, \$$

etc.

LALR(1) parser

canonical LR(1) often produces too many states

Notice: cores of each

LR(1) parser state are same as for SLR - (indep of lookahead)

State of LALR(1) parser is a set of LR(1) items.

Easy description:

Start with an (canonical) LR(1) parser,

merge states with the same set of cores

union

goto & action tables constructed similarly

(Time & space inefficient)

efficient methods exist to construct an LALR(1) parser.

[no further details — not on the test]

Code generation & optimization

generic low-level target language: three-address code

$L: x := y \text{ op } z$

$x := \text{op } y$

goto L

if $x \text{ cmp } y$ then goto L