

$\text{FIRST}(\beta)$  set of terminals and/or  $\epsilon$

$\beta$  is any string of grammar symbols.

$\text{FOLLOW}(A)$

$A$  is a nonterminal set of all tokens that could come right after  $A$  in some sentential form

Assume, from now on, that the start symbol does not appear in the body of any production.

Easy to convert any grammar into an equivalent one of this form

$G$  grammar with start symbol  $S$ .

$G'$  is same grammar, except, new, fresh nonterminal  $S'$  is new start symbol, then add a single production  $S' \rightarrow S$

to  $G$ . [ $G'$  is an augmented grammar]

Given  $G'$  augmented grammar with start symbol  $S'$

Construct FOLLOW sets as follows:

1. put  $\$$  into  $\text{FOLLOW}(S')$
2. If  $A \rightarrow \alpha B \gamma$  is a production, where  $A, B$  nonterminals,  $\alpha, \gamma$  are strings of grammar symbols:
  - a) But every token in  $\text{FIRST}(\gamma)$  into  $\text{FOLLOW}(B)$
  - b) If  $\epsilon \in \text{FIRST}(\gamma)$  [e.g.,  $A \rightarrow \alpha B$ ] put all of  $\text{FOLLOW}(A)$  into  $\text{FOLLOW}(B)$

Starting with all FOLLOW sets empty, apply rules 1, 2a, 2b repeatedly until nothing else can get in.

|                                   | A | Follow(A)     |
|-----------------------------------|---|---------------|
| $S \rightarrow E$                 | S | \$            |
| $E \rightarrow E + T \mid T$      | E | $\$, +, )$    |
| $T \rightarrow T * F \mid F$      | T | $\$, +, *, )$ |
| $F \rightarrow c \mid v \mid (E)$ | F | $\$, +, *, )$ |

Building an SLR(0) parser.

Items: An item (LR(0) item)

is an expression of the form

$$A \rightarrow \alpha \cdot \beta$$

where  $A \rightarrow \alpha \beta$  is a production of the grammar.

Eg.  $E \rightarrow E + T$

gives 4 possible items:

$$\begin{aligned} E &\rightarrow \cdot E + T \\ E &\rightarrow E \cdot + T \\ E &\rightarrow E + \cdot T \\ E &\rightarrow E + T \cdot \end{aligned}$$

$A \rightarrow \epsilon$  yields  $A \rightarrow \cdot$  as only item

A state of an SLR parser is a set of items. We build states starting the start state and following transitions.

Closure: Let  $S$  be a set of items. Compute the closure of  $S$ :

$\text{Closure}(S)$ :

$T := S$

repeat

let  $A \rightarrow \alpha \cdot B \gamma$  be some item in  $T$ , where  $A, B$  nonterminals,  $\alpha, \gamma$  are strings of grammar symbols  
For each production with head  $B$

$$B \rightarrow \delta,$$

add  $B \rightarrow \cdot \delta$  to  $T$ .

until nothing more gets added

return  $T$

Now we define the transition function  $\text{trans}(s, x)$   $s$  is a state  $x$  is symbol

$\text{trans}(S, X) = t$  (state)

where:

$t := \emptyset$

repeat

if  $A \rightarrow \alpha.X\beta$  is in  $S$ ,

where  $A$  nonterminal,

$\alpha, \beta$  strings of grammar symbols,

$X$  is a grammar symbol

add  $A \rightarrow \alpha.X\beta$  to  $t$

//  $A \rightarrow \alpha.X\beta$

until all such items are added to  $t$

return  $\text{closure}(t)$

Start state:

$S_0 = \text{closure}(\{S' \rightarrow \cdot S\})$

where  $S'$  is the start symbol of the augmented grammar

$S_0 = \text{start state:}$

|                             |                                                    |                              |
|-----------------------------|----------------------------------------------------|------------------------------|
| $S \rightarrow \cdot E$     | } normal items                                     | $S \rightarrow E$            |
| $E \rightarrow \cdot E + T$ |                                                    | $E \rightarrow E + T \mid T$ |
| $E \rightarrow \cdot T$     | } non-terminal items<br>those added by closure op. | $T \rightarrow T * F \mid F$ |
| $T \rightarrow \cdot T * F$ |                                                    | $F \rightarrow c \mid (E)$   |
| $T \rightarrow \cdot F$     |                                                    |                              |
| $F \rightarrow \cdot c$     |                                                    |                              |
| $F \rightarrow \cdot (E)$   |                                                    |                              |

$S_1 = \text{trans}(S_0, E):$

$S \rightarrow E \cdot$

$E \rightarrow E \cdot + T$

$S_2 = \text{trans}(S_0, T):$

$E \rightarrow T \cdot$

$T \rightarrow T \cdot * F$

$S_3 = \text{trans}(S_0, F):$

$T \rightarrow F \cdot$

$S_4 = \text{trans}(S_0, c):$

$F \rightarrow c \cdot$

$S_5 = \text{trans}(S_0, '('):$

$F \rightarrow ( \cdot E$

$E \rightarrow \cdot E + T$

$E \rightarrow \cdot T$

$T \rightarrow \cdot T * F$

$T \rightarrow \cdot F$

$F \rightarrow \cdot c$

$F \rightarrow \cdot (E)$

$S_6 = \text{trans}(S_1, +):$

$E \rightarrow E + \cdot T$

$T \rightarrow \cdot T * F$

$T \rightarrow \cdot F$

$F \rightarrow \cdot c$

$F \rightarrow \cdot (E)$

ETC.

Construct the goto and action tables for the SLR(1) parser.

For every nonterminal  $A$  and state  $S$ , define

$\text{goto}[S, A] := \text{trans}(S, A)$

For every state  $S$  containing the item  $S' \rightarrow \cdot S$ . (exactly one such state)

set  $\text{action}[S, \$] := \text{"accept"}$

For every state  $S$  containing an item of the form  $A \rightarrow \alpha \cdot b \beta$

where  $A$  nonterminal

$b$  is a token

$\alpha, \beta$  strings

set  $\text{action}[S, b] = \text{"shift } t"$ ,

where  $t = \text{trans}(S, b)$

[ $t$  contains  $A \rightarrow \alpha b \beta$ ]

For every state  $S$  containing

$A \rightarrow \alpha \cdot$ ,

set  $\text{action}[S, a] = \text{"reduce } A \rightarrow \alpha"$

for each token  $a \in \text{FOLLOW}(A)$ .