CSCE 355, Fall 2022, Assignment 3 Due September 20, 2022

August 24, 2022

Team homework submissions are now accepted! Starting with this homework, you are encouraged to form a team of up to four (4) people for a single joint homework submission. Benefits include sharing ideas with other people, reduced workload, and faster feedback (due to less grading). This is purely optional. If you do form a team, then elect one member of the team to submit the homework, and be sure all your names are on the submission.

1. For the ϵ -NFA of textbook Exercise 2.5.2,

	ϵ	a	b	c
$\rightarrow p$	$\begin{cases} q,r \end{cases}$	Ø	$\{q\}$	$\{r\}$
$q \\ *r$	Ø	{ <i>p</i> }	$\{r\}$	$\{p,q\}$
*r	Ø	Ø	Ø	Ø

find an equivalent NFA (without ϵ -moves) using the method explained in class. This is also Method 2 described in the COURSE NOTES (link from the course homepage) in Section 10.4.

- 2. Do Exercise 2.5.3(a): Design an ϵ -NFA for the following language: the set of all strings consisting of zero or more a's followed by zero or more b's, followed by zero or more c's. Try to use ϵ -transitions to simplify your design.
- 3. Do Problem 2.3 (pp. 81–82). This illustrates a proof by string induction.
- 4. (a) Show that every regular language is recognized by an ϵ -NFA where out of each state there is no more than one ϵ -transition and no more than one non- ϵ -transition (i.e., a transition on a symbol from the alphabet).
 - (b) Show that every regular language is recognized by an ϵ -NFA where out of each state there is exactly one ϵ -transition and exactly one non- ϵ -transition (i.e., a transition on a symbol from the alphabet). (A solution to this part is obviously also a solution to the previous part.)
- 5. Do Exercise 3.1.1(b,c): Write regexes for the following languages:
 - b) The set of strings of 0's and 1's whose tenth symbol from the right end is 1.
 - c) The set of strings of 0's and 1's with at most one pair of consecutive 1's.
- 6. (Optional) Do Exercises 3.1.2(b,c) and 3.1.3(a,b,c)

- 7. Write a regular expression for the language of strings over $\{a, b, c\}$ where no a appears after any b or c.
- 8. Do Exercise 3.2.3: Convert the following DFA to a regular expression, using the state-elimination technique of Section 3.2.2.

$$\begin{array}{c|cccc} & 0 & 1 \\ \hline \rightarrow *p & s & p \\ q & p & s \\ r & r & q \\ s & q & r \end{array}$$

- 9. Do Exercise 3.2.4(c): Convert the following regex to an ϵ -NFA: $\mathbf{00}(\mathbf{0}+\mathbf{1})^*$.
- 10. Recall the DFA D we constructed that accepts a binary string iff it has an odd number of 1's:

$$\begin{array}{c|cccc}
 & 0 & 1 \\
\hline
 \rightarrow A & A & B \\
 *B & B & A
\end{array}$$

- (a) Convert D into an equivalent clean ϵ -NFA using the clean-up procedure in class (add a new start state, a new final state, and some ϵ -transitions).
- (b) Use the state elimination method to convert D to a regular expression. Eliminate state A first, then B.
- 11. Same exercise as before, except make A the final state (so that D accepts a string iff it has an *even* number of 1's).
- 12. (Optional) Recall the product DFA P that counts an even number of zeros and an odd number of ones:

$$\begin{array}{c|c|c|c} & & 0 & 1 \\ \hline \rightarrow EE & OE & EO \\ OE & EE & OO \\ *EO & OO & EE \\ OO & EO & OE \\ \end{array}$$

Use the state elimination method to convert P to a regular expression. (To control the complexity, you may wish to define names for intermediate regexes.)

- 13. Draw the transition diagram of an ϵ -NFA equivalent to the regex $(a + bc)^*aa$. You may (but are not required to) contract ϵ -transitions provided it is safe to do so.
- 14. Write a regular expression for the language of strings over $\{a, b, c\}$ where no a appears after any b or c.