# Online Vibration Signal Compensation with LSTM and Low-Rank Approximation

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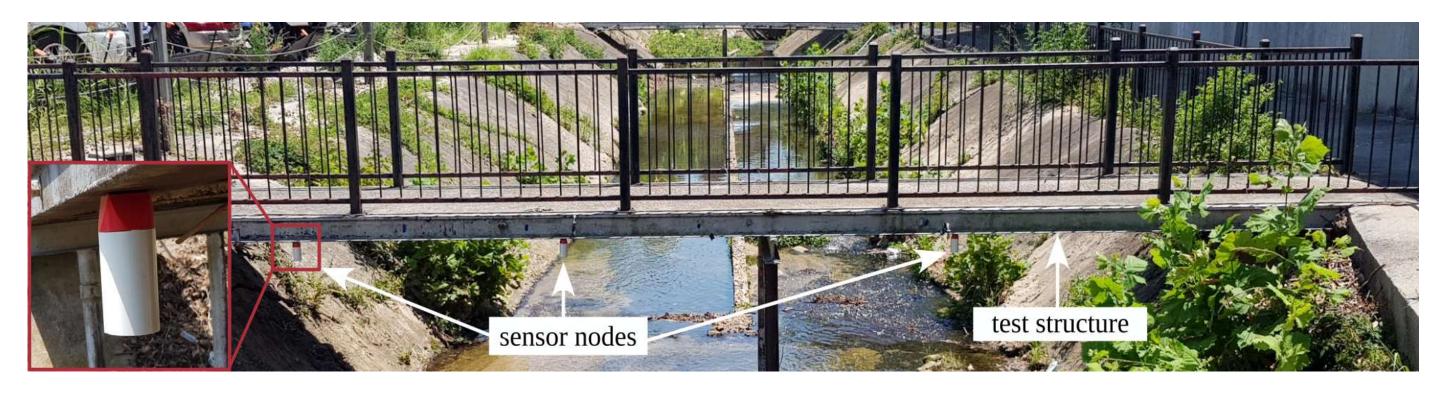
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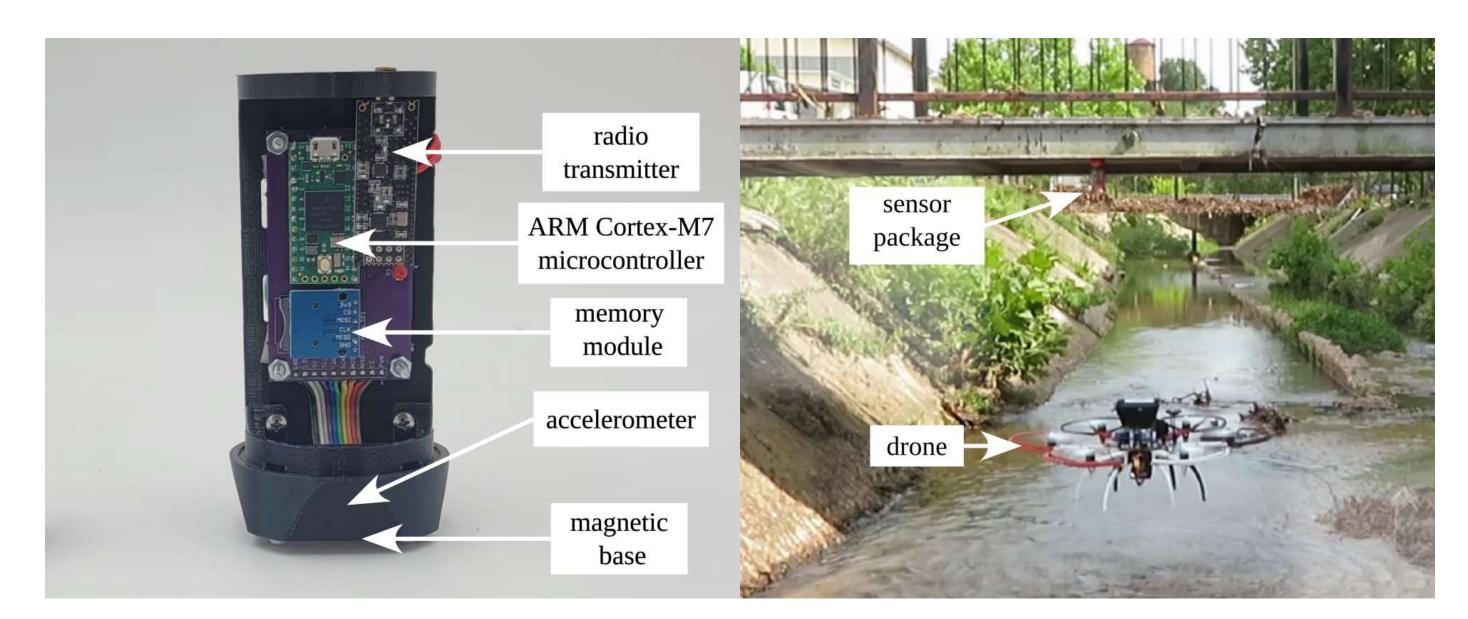
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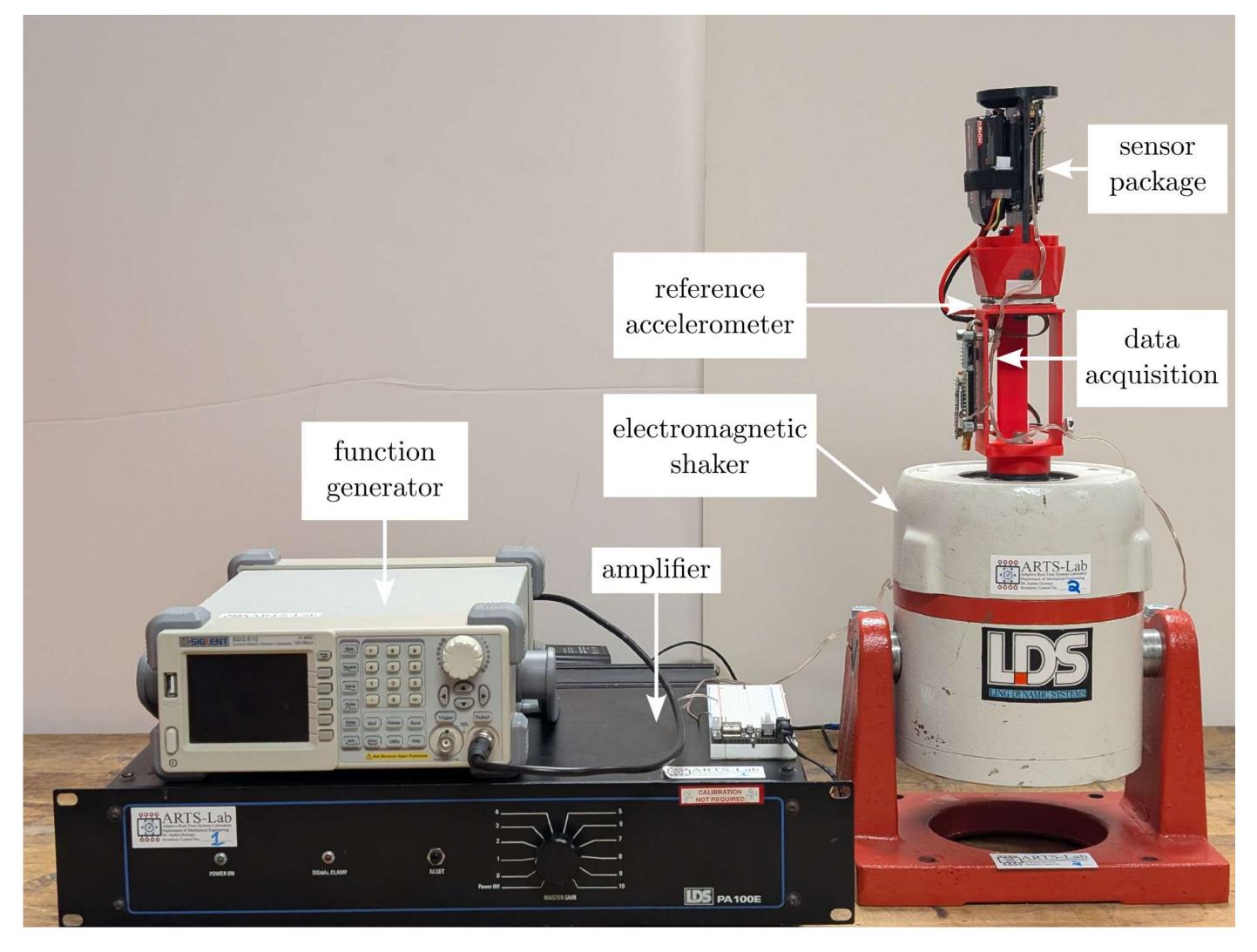
## Background



SHM sensing node deployment



Drone-deployable sensor package



Experimental setup

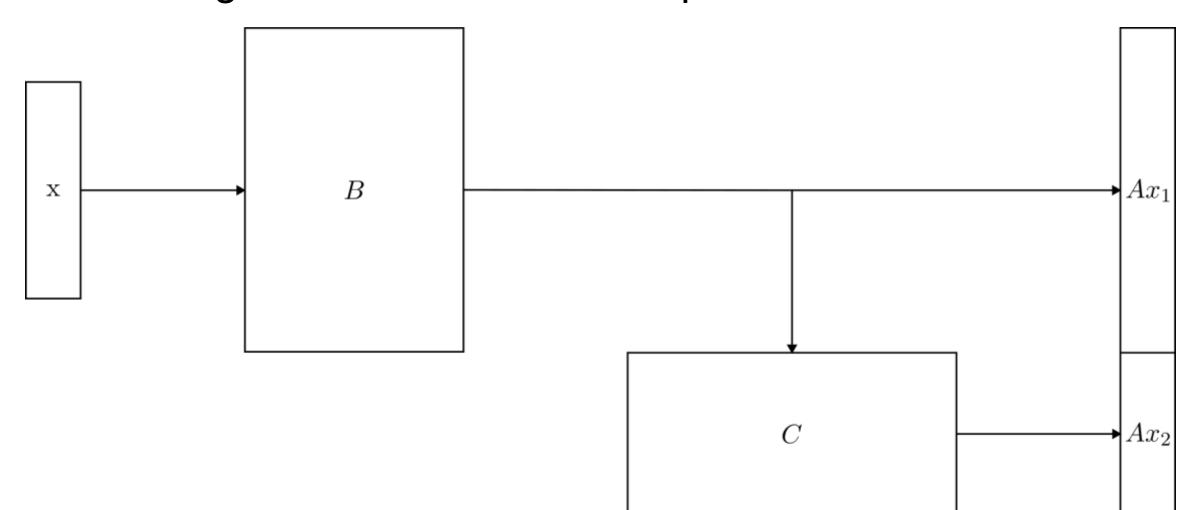
# Degrees-of-Freedom Decomposition

$$Ax_1 = Bx$$
  $Ax_2 = Cx_1$   $Ax = P\begin{bmatrix} Ax_1 \\ Ax_2 \end{bmatrix}$ 

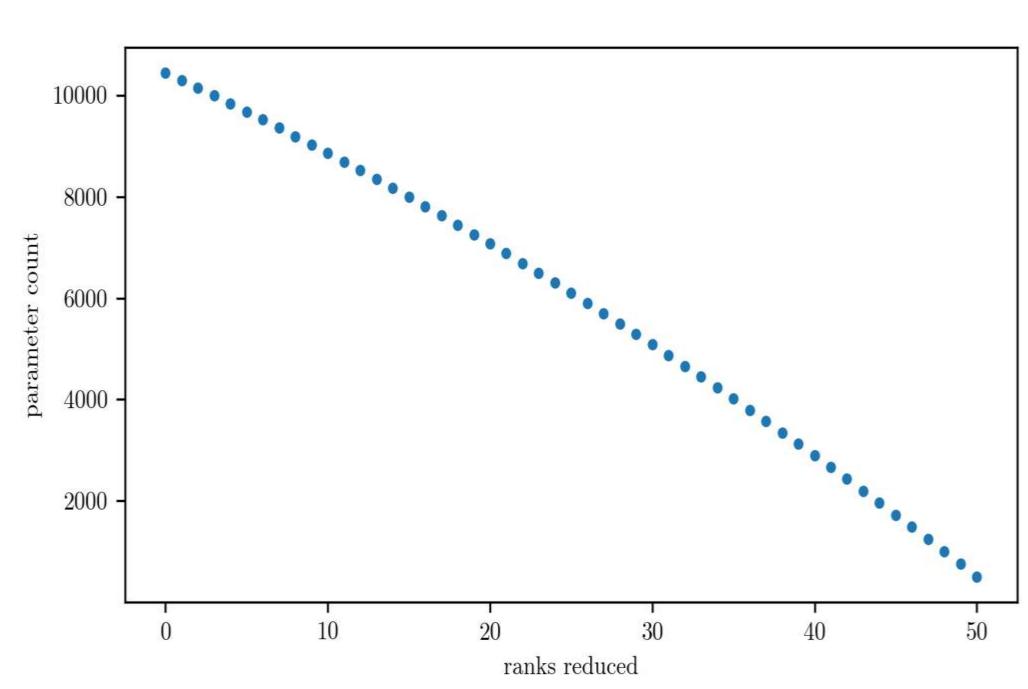
$$U = \begin{bmatrix} U_1 \\ U_2 \end{bmatrix} \qquad B = U_1 \Sigma V^{\mathrm{T}} \qquad C = U_2 U_1^{-1}$$

$$B: r \times n$$
  $C: (m-r) \times r$ 

Degrees-of-freedom decomposition definition



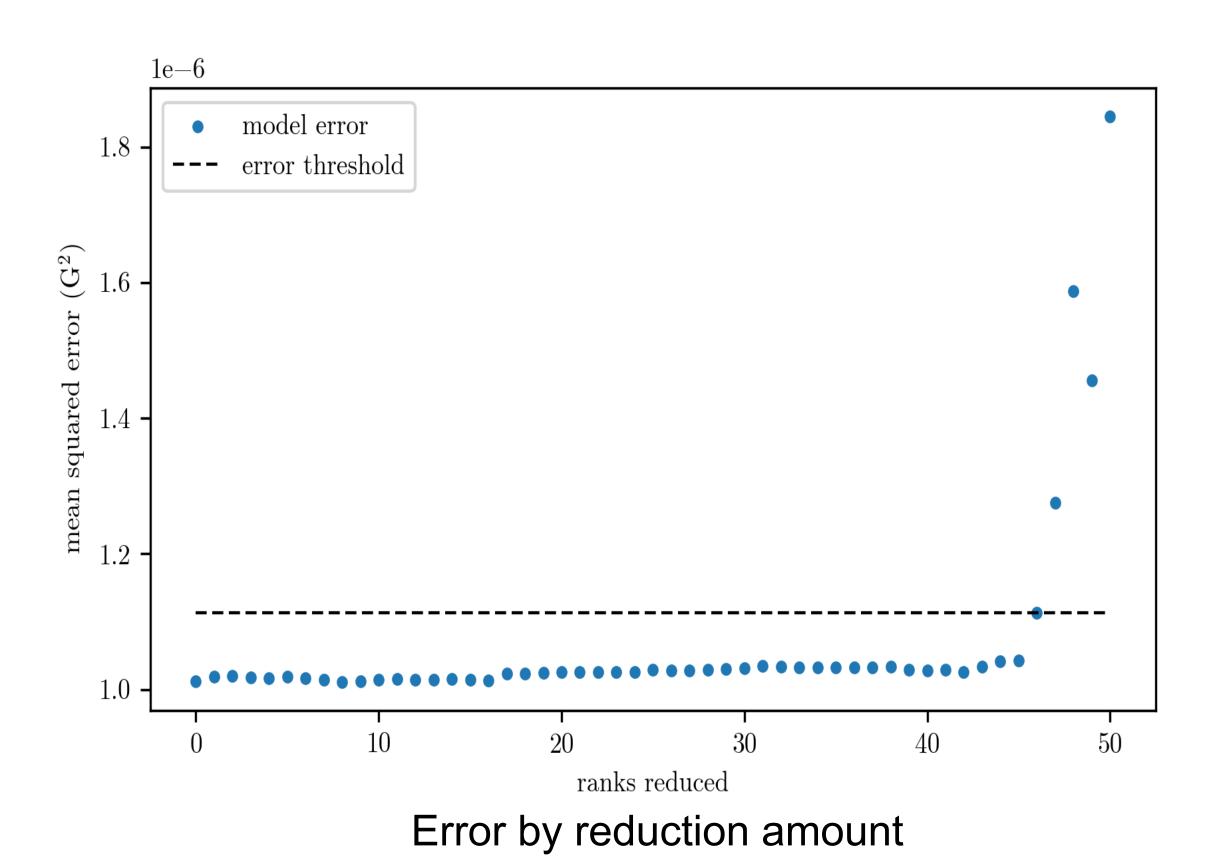
Degrees-of-freedom matrix-vector multiplication

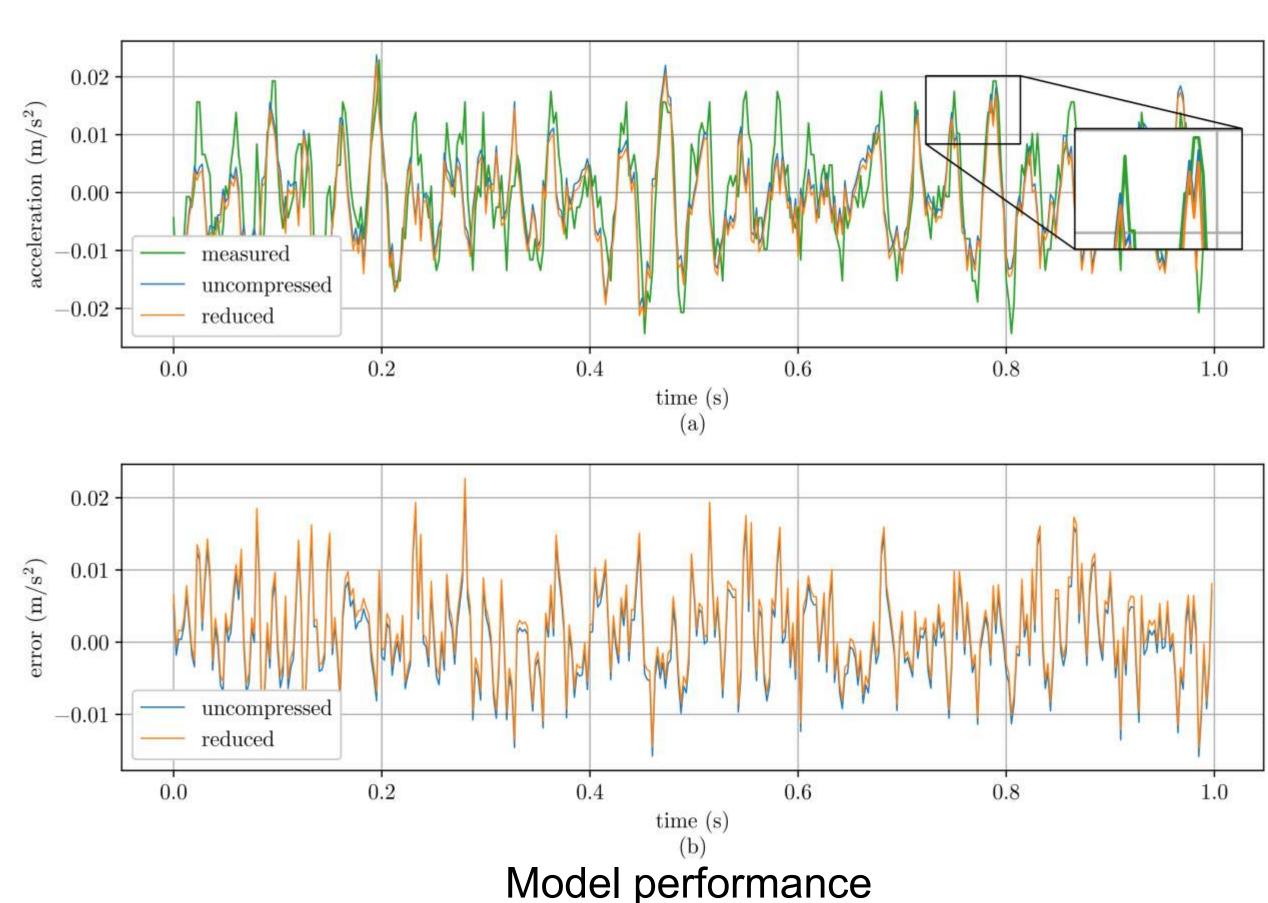


Compensation model parameter count

- Reduces the number of parameters and operations required for inference
- Removes barrier-to-entry associated with direct use of SVD
- Generalizable to any application requiring matrix-vector multiplication

### Performance





#### Conclusion

- LSTM is shown to be an effective non-linear compensator
- The LSTM weight matrix was reduced from rank 51 to rank 6 using truncated SVD
- Degrees-of-freedom decomposition allowed for significant spatial and computational savings
- Memory footprint improved to 6,884B from 41,804B
- Inference latency improved to 40µs from 201µs





