

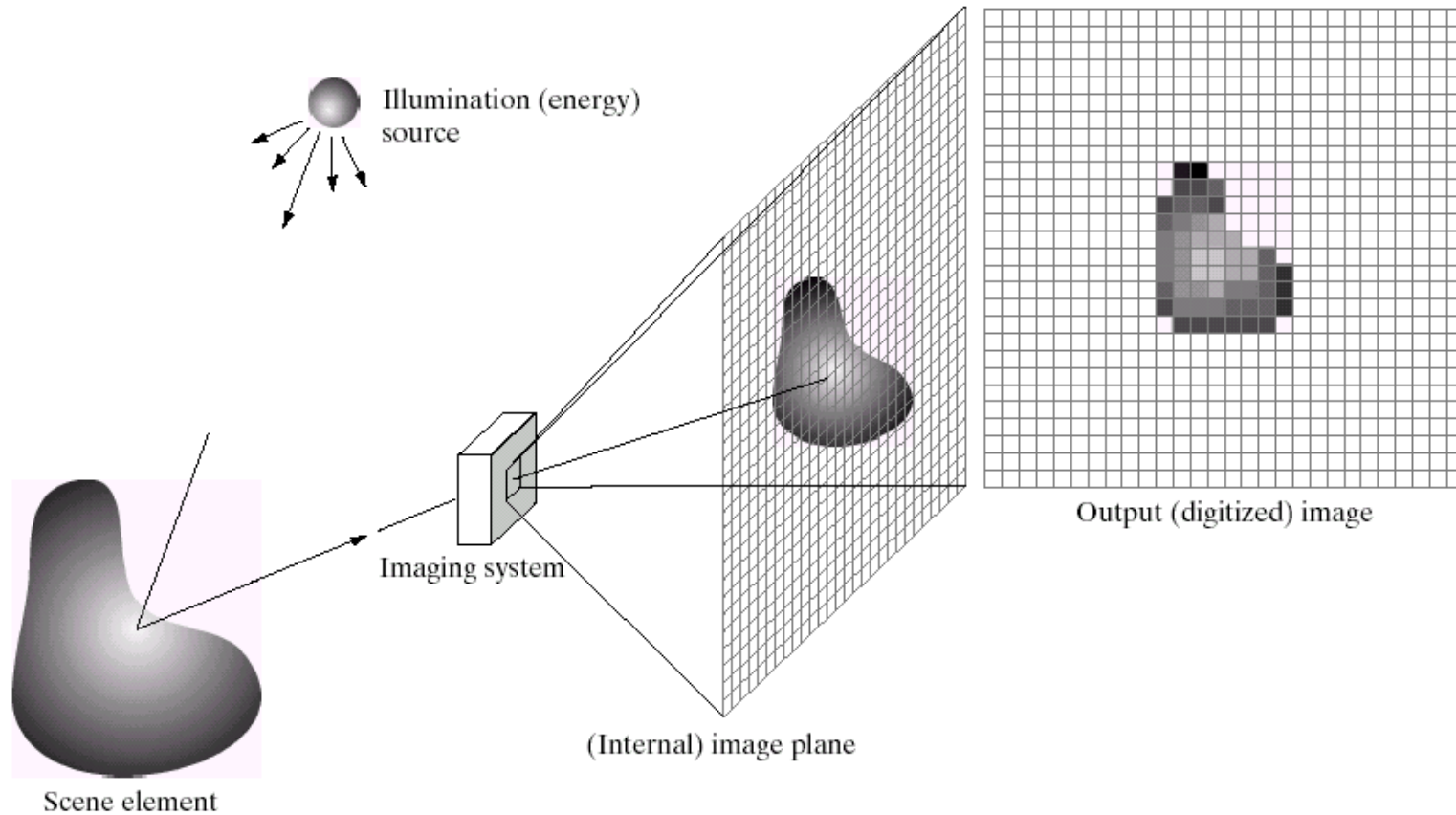


UNIVERSITY OF  
SOUTH CAROLINA

# CSCE 590 INTRODUCTION TO IMAGE PROCESSING

## Image Acquisition

# Image Acquisition and Representation

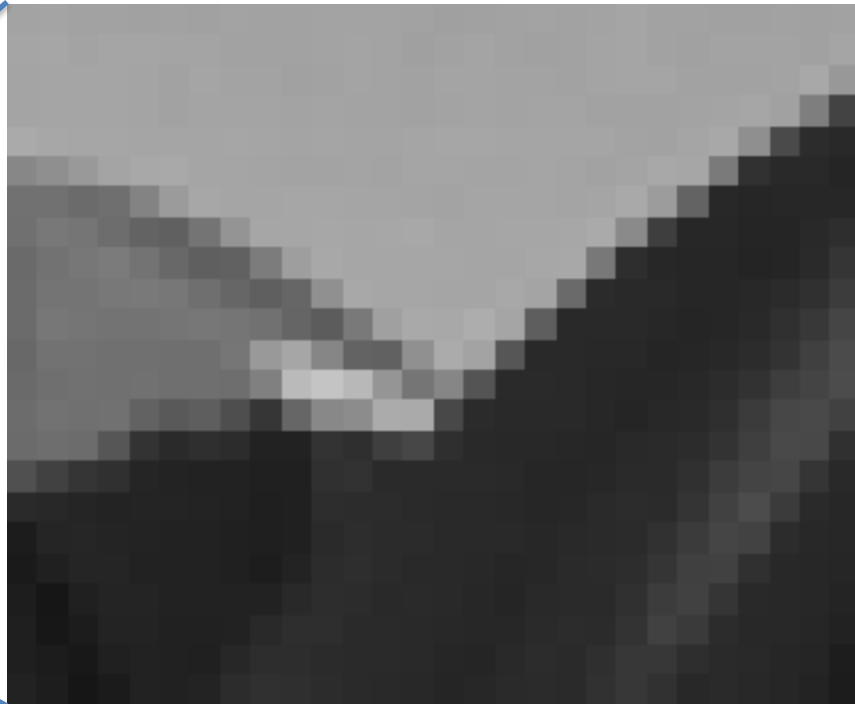
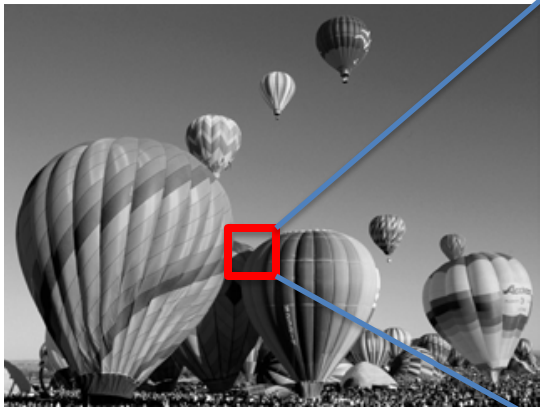


a b c d e

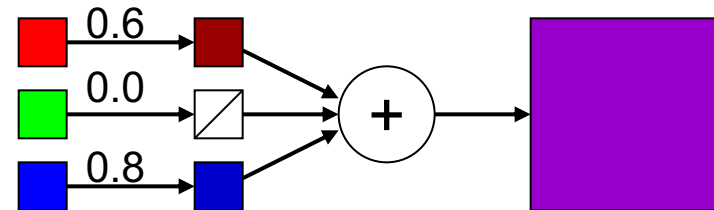
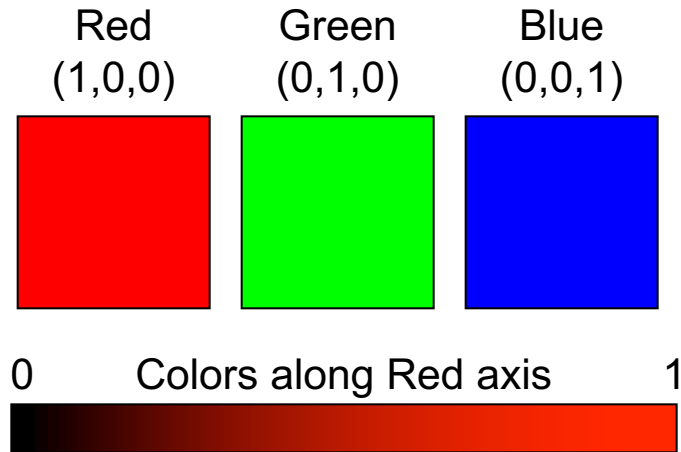
**FIGURE 2.15** An example of the digital image acquisition process. (a) Energy (“illumination”) source. (b) An element of a scene. (c) Imaging system. (d) Projection of the scene onto the image plane. (e) Digitized image.

# Image Representation

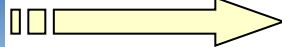
- **Discrete representation of images**
  - we'll carve up image into a rectangular grid of pixels  $P[x,y]$
  - • each pixel  $p$  will store an intensity value in  $[0\ 1]$
  - •  $0 \rightarrow$ black;  $1 \rightarrow$ white; in-between  $\rightarrow$ gray
  - • Image size  $m$  by  $n \rightarrow (mn)$  pixels



# Color Image



RGB channels



A yellow arrow pointing from the original image to the decomposed channels.



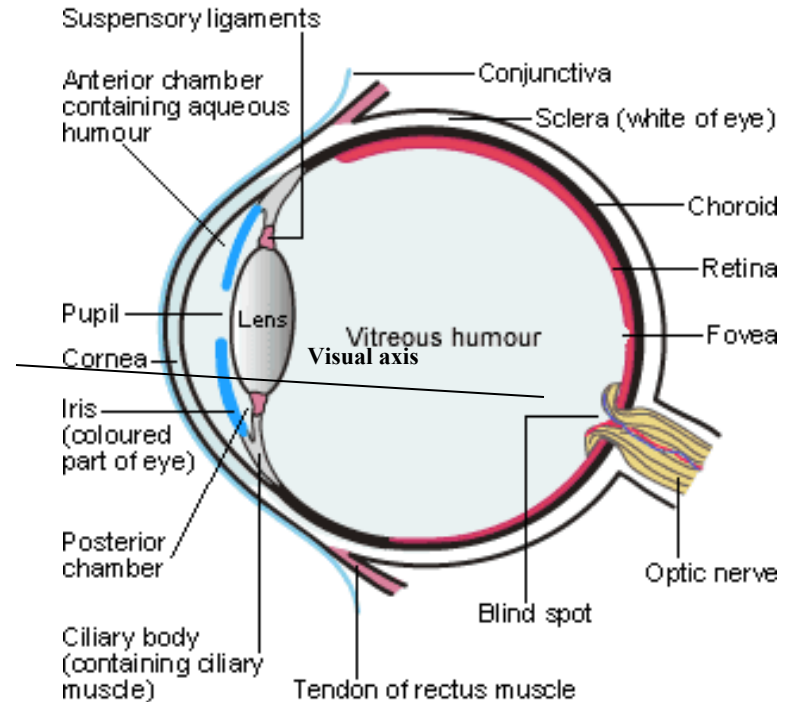
# Elements of Human Visual Perception

**Human visual perception plays a key role in selecting a technique**

**Lens and Cornea: focusing on the objects**

**Two receptors in the retina:**

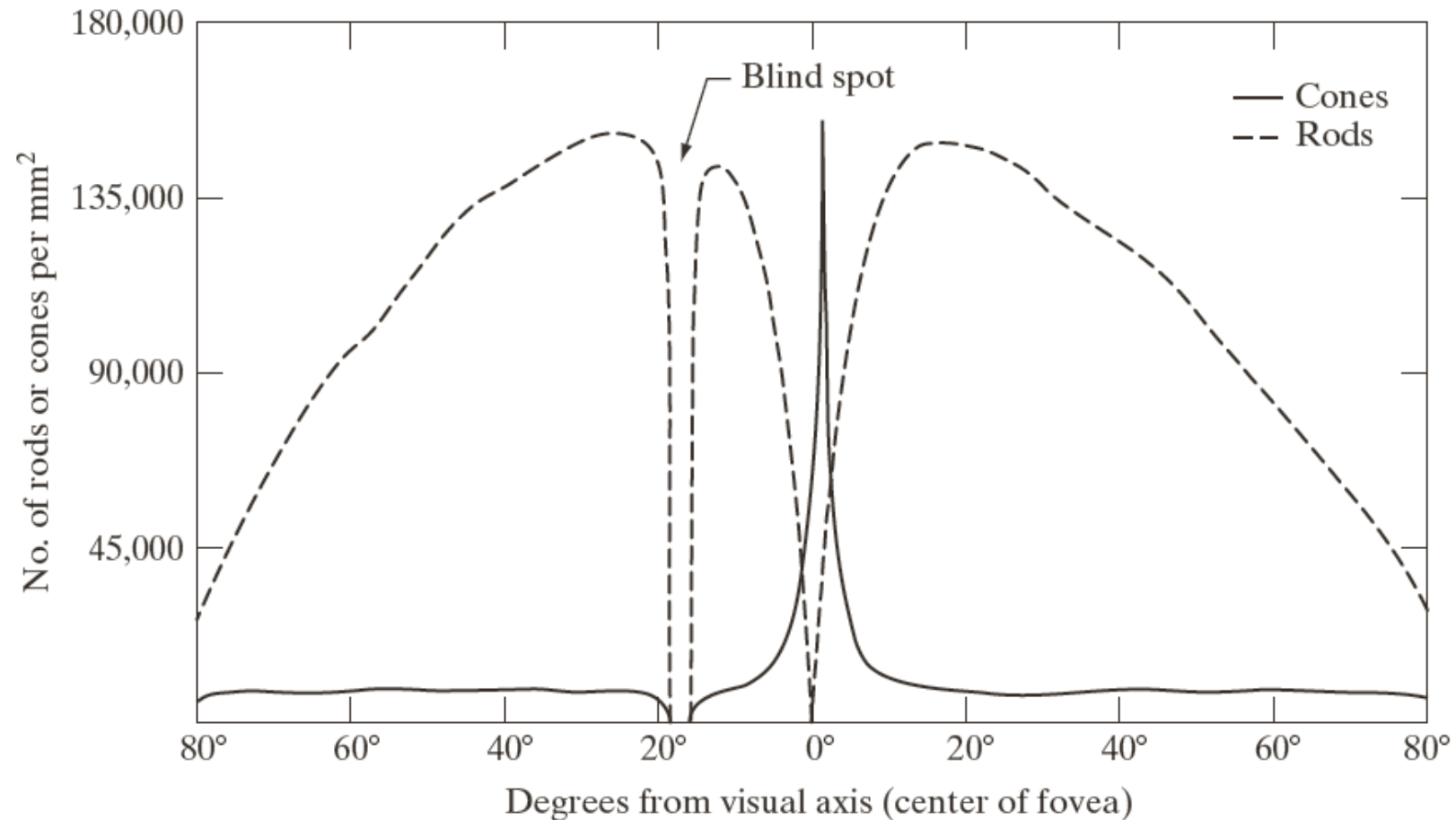
- Cones and rods
- Cones located in fovea and are highly sensitive to color
- Rods give a general overall picture of view, are insensitive to color and are sensitive to low level of illumination



<http://www.mydr.com.au/eye-health/eye-anatomy>



# Distribution of Rods and Cones in the Retina



**FIGURE 2.2**  
Distribution of  
rods and cones  
in the retina.



# Brightness Adaptation: Subjective Brightness

## Scotopic:

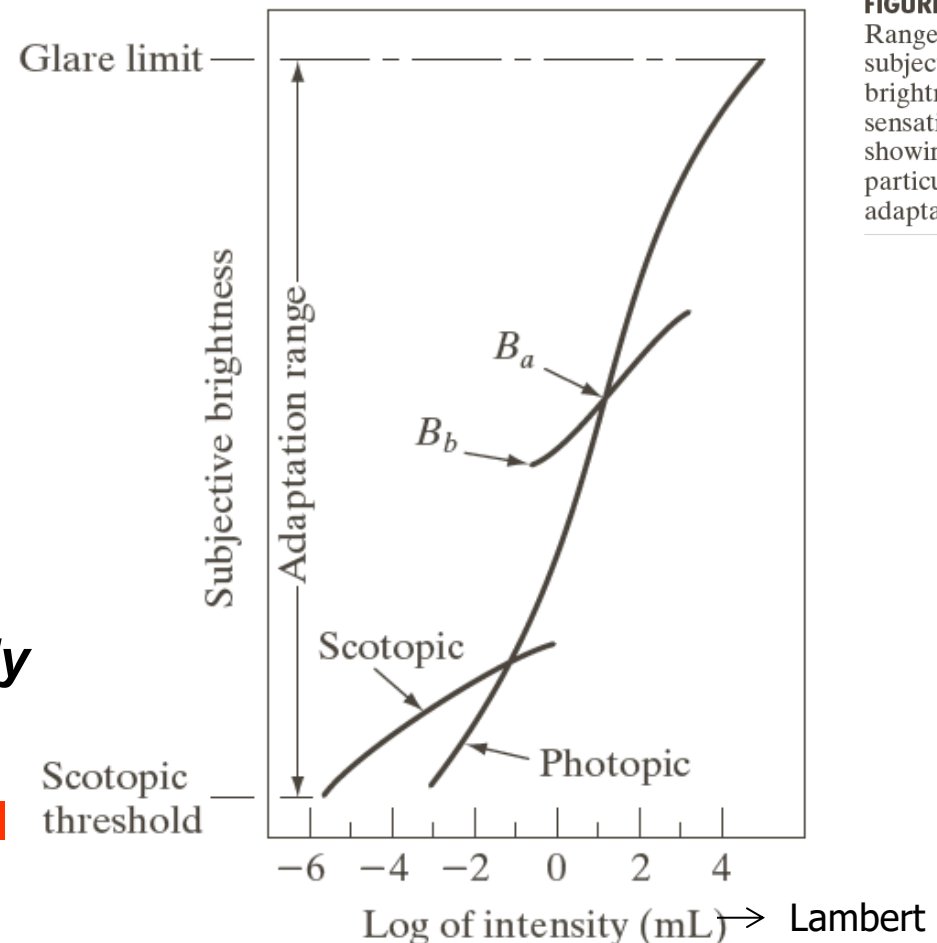
- Vision under low illumination
- rod cells are dominant

## Photopic:

- Vision under good illumination
- cone cells are dominant

The total range of distinct intensity levels the eye can discriminate *simultaneously* is rather small

**Brightness adaptation level**



**FIGURE 2.4** Range of subjective brightness sensations showing a particular adaptation level.



# Brightness Discrimination

**Weber Ratio/Fraction**

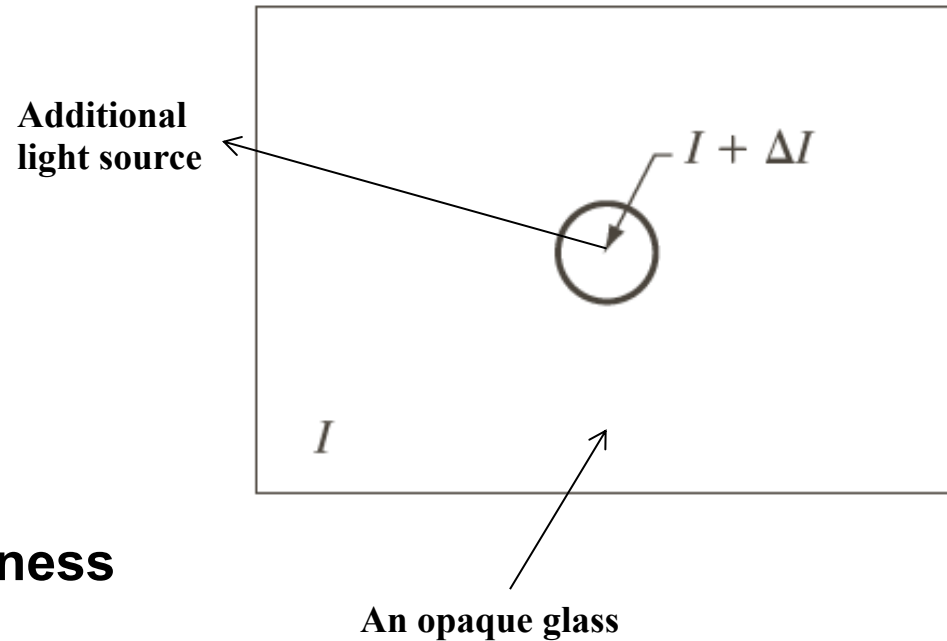
$$\frac{\Delta I_c}{I}$$

$I + \Delta I_c$  :

**Short-duration flash**

**Small ratio: good brightness discrimination**

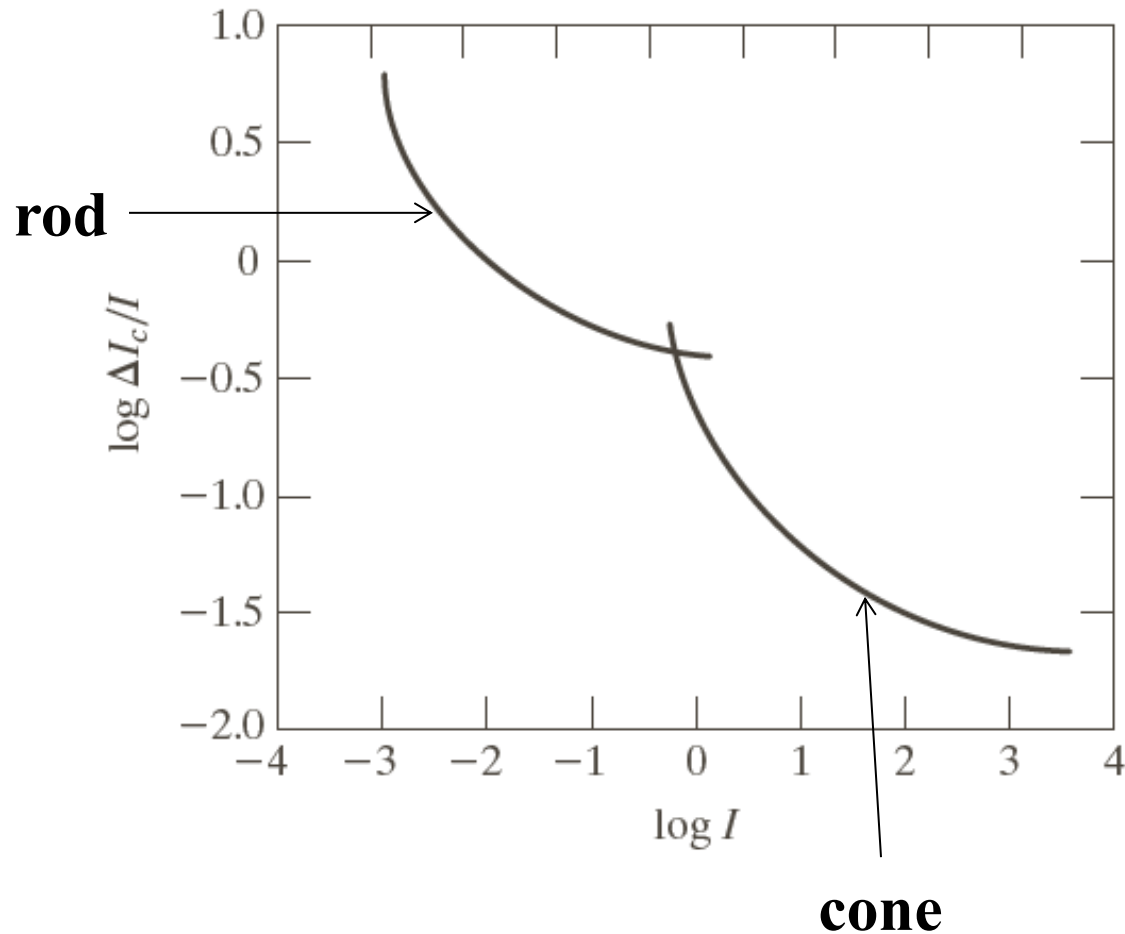
**Large ratio: poor brightness discrimination**



**FIGURE 2.5** Basic experimental setup used to characterize brightness discrimination.

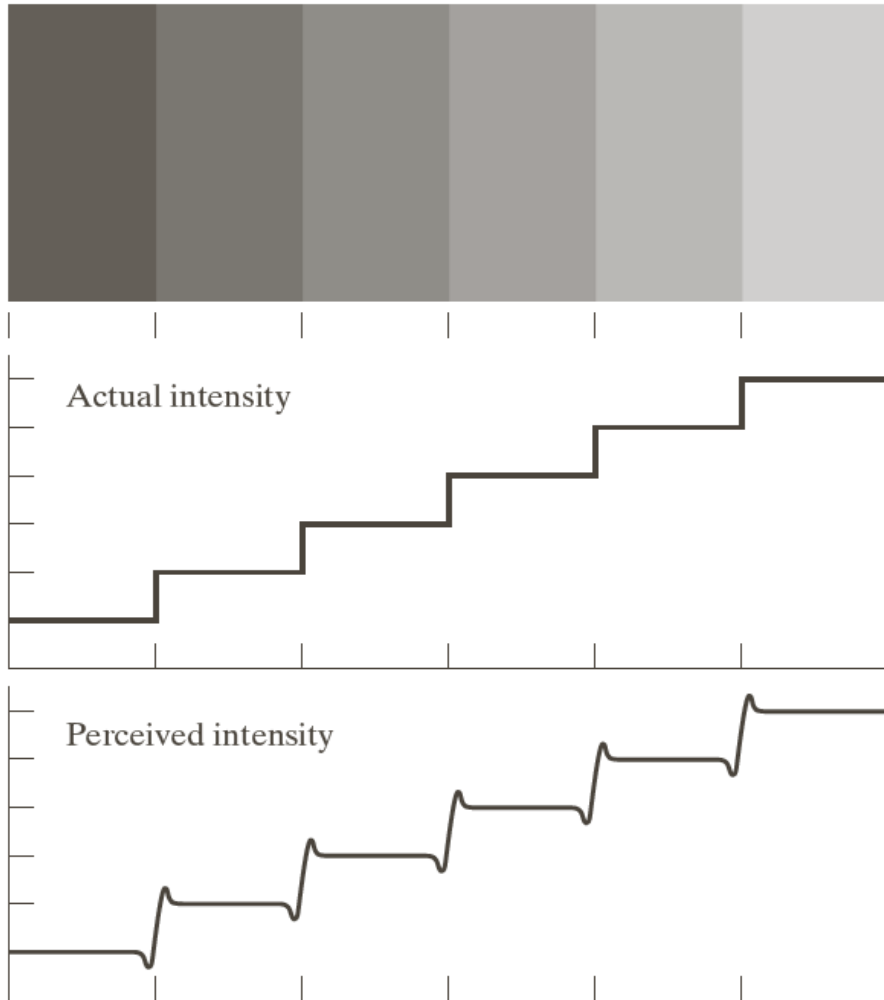


# Brightness Discrimination at Different Intensity Levels



**FIGURE 2.6**  
Typical Weber  
ratio as a function  
of intensity.

# Perceived Intensity is Not a Simple Function of the Actual Intensity (1)



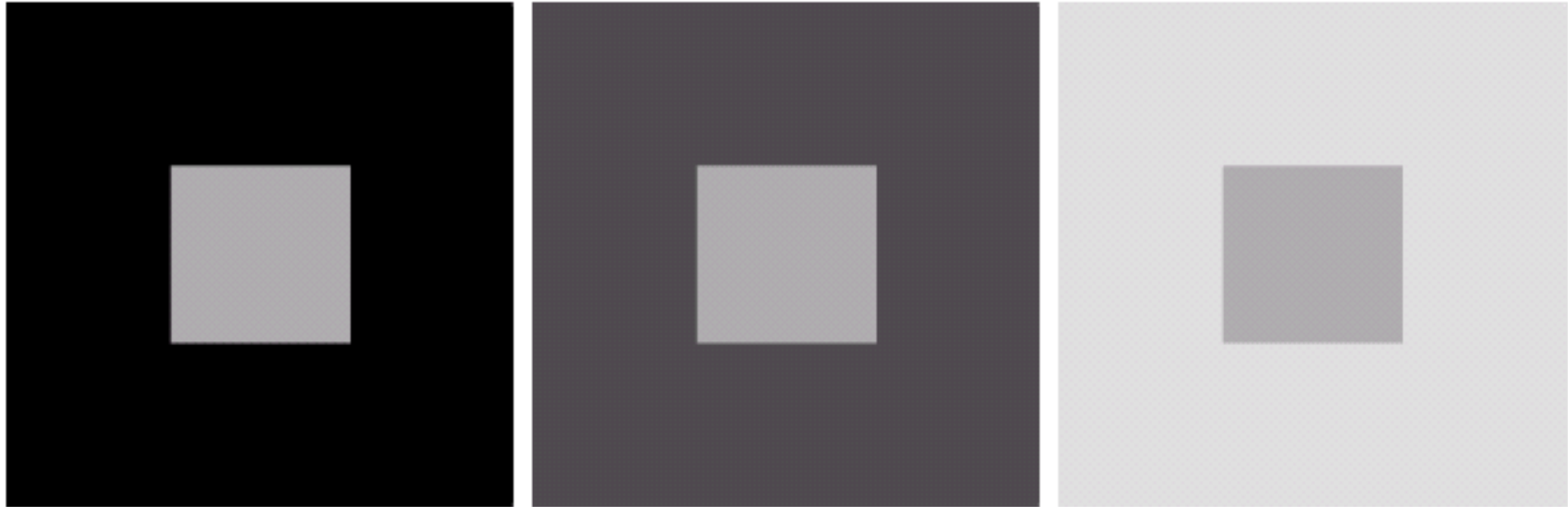
a  
b  
c

**FIGURE 2.7**  
Illustration of the Mach band effect. Perceived intensity is not a simple function of actual intensity.



# Perceived Intensity is Not a Simple Function of the Actual Intensity (2) – Simultaneous Contrast

---



a b c

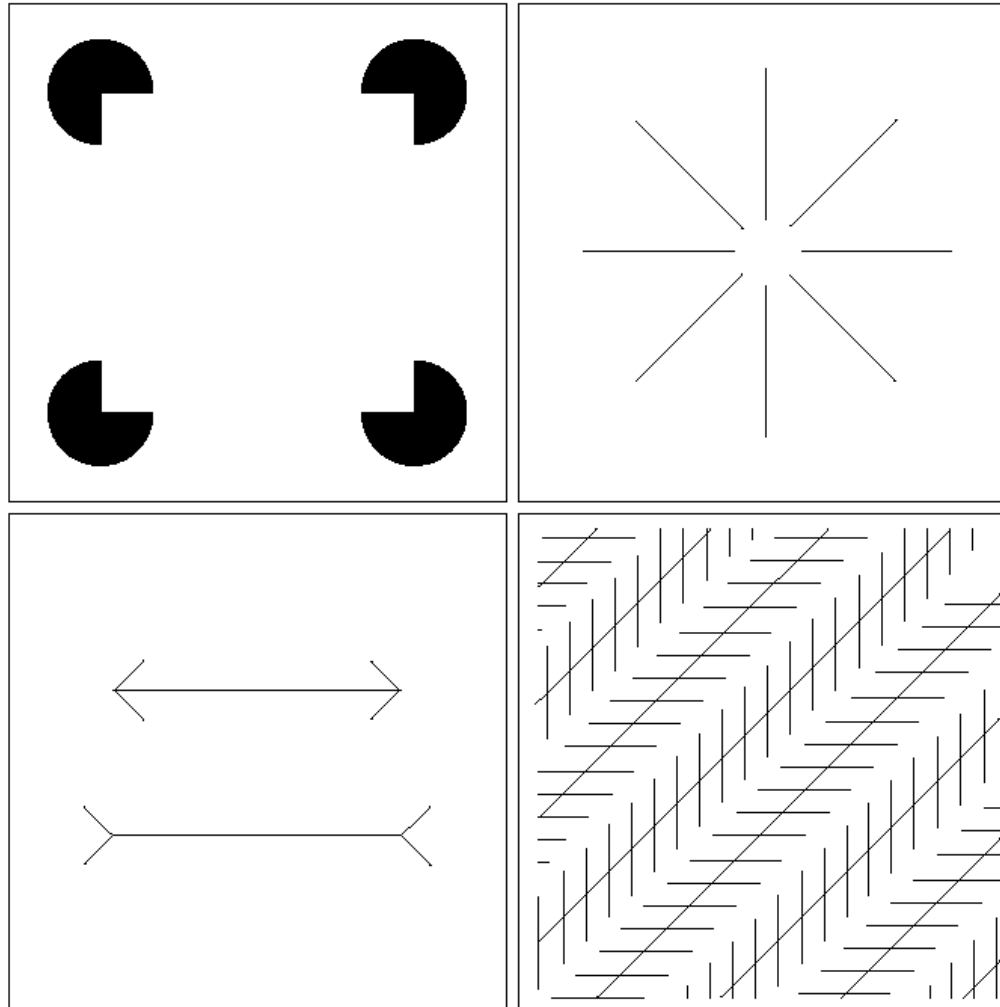
**FIGURE 2.8** Examples of simultaneous contrast. All the inner squares have the same intensity, but they appear progressively darker as the background becomes lighter.

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# Optical Illusions: Complexity of Human Vision

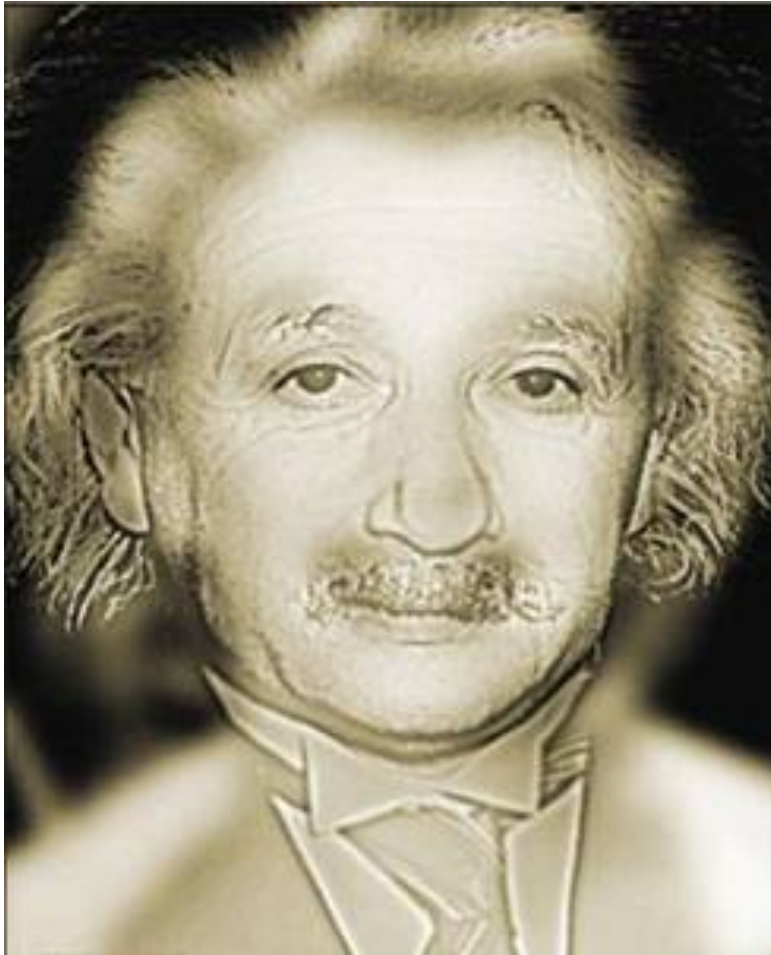
a b  
c d

**FIGURE 2.9** Some well-known optical illusions.



# More Optical Illusions

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<http://www.123opticalillusions.com/>



<http://brainden.com/optical-illusions.htm>



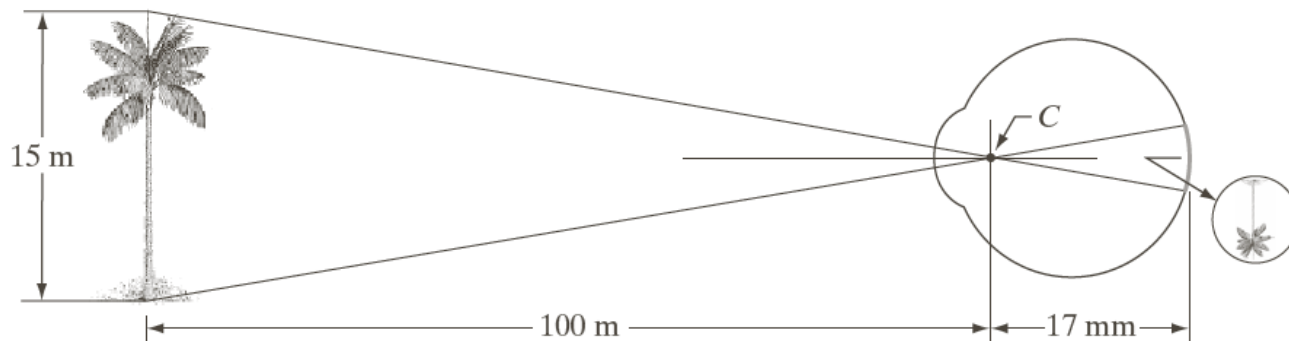
# More Optical Illusions

---



# Image Formation in the Eye

**Image is upside down in the retina/imaging plane!**



**FIGURE 2.3**

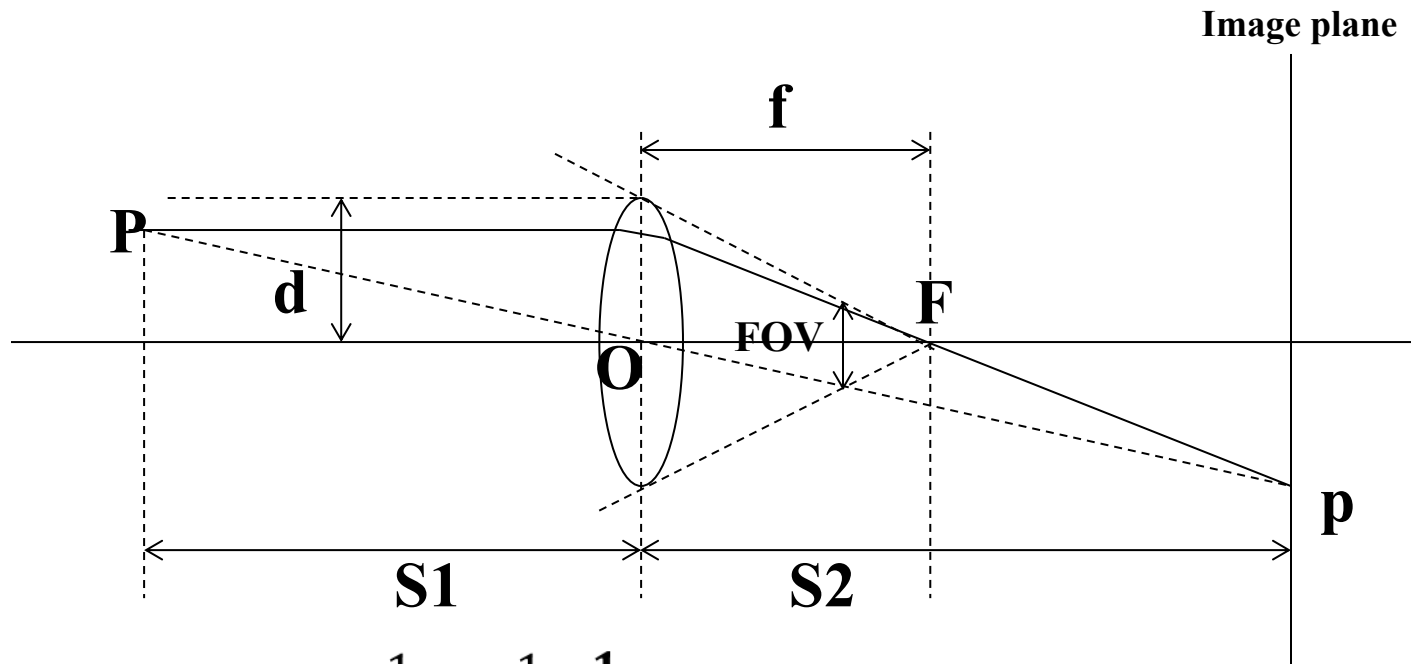
Graphical representation of the eye looking at a palm tree. Point *C* is the optical center of the lens.

Adjust focus length

- Camera
- Human eye



# Lens Parameters



Thin lens theory:  $\frac{1}{S_1} + \frac{1}{S_2} = \frac{1}{f}$

• Increasing the distance from the object to the lens will reduce the size of image

Field of View:  $\omega = 2 \arctan \frac{d}{f}$

• Large focus length will give a small FOV



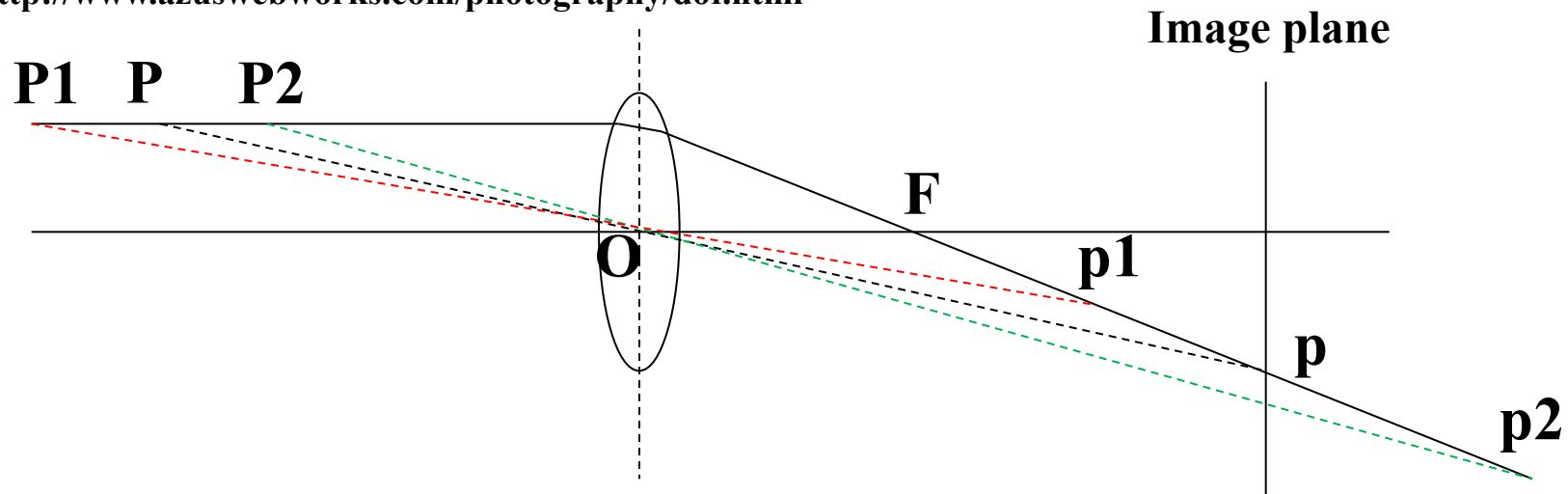


# Depth of Field & Out of Focus

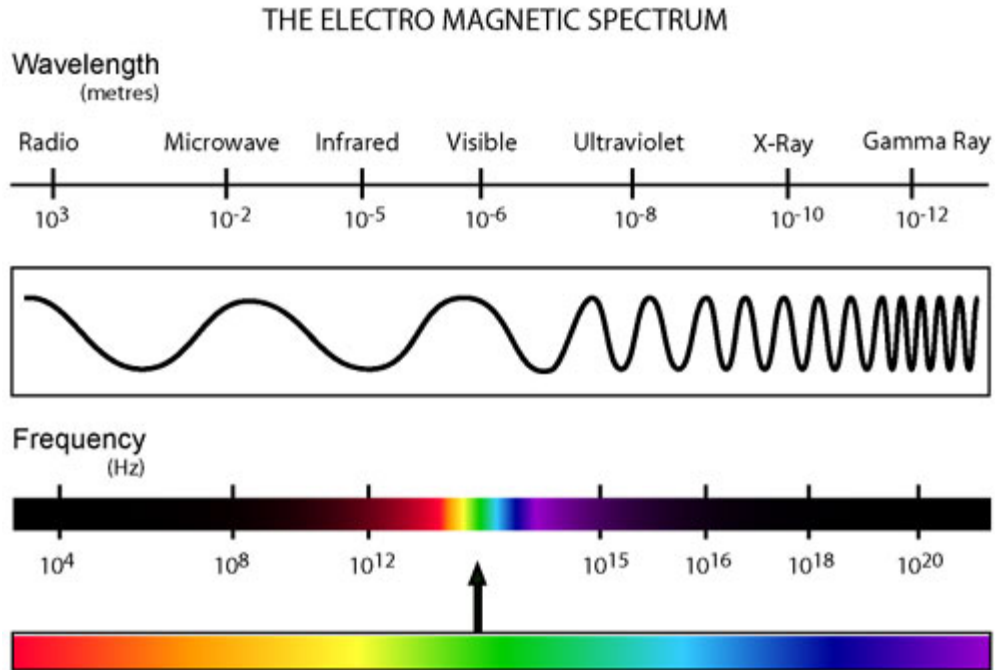


- DOF is inversely proportional to the focus length
- DOF is proportional to  $S1$

<http://www.azuswebworks.com/photography/dof.html>



# Light and EM Spectrum

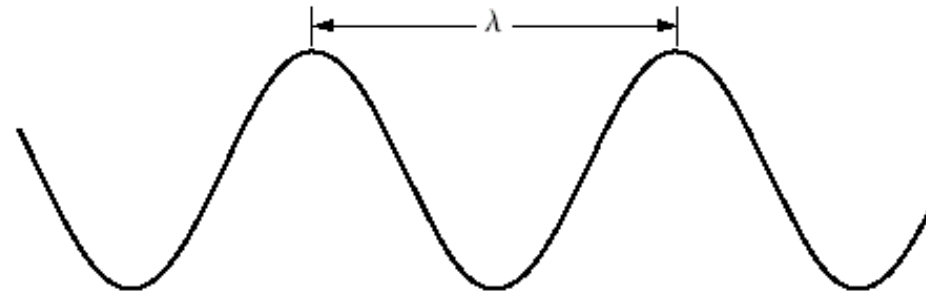


<http://www.kollewin.com/blog/electromagnetic-spectrum/>



# Relation Among Wavelength, Frequency and Energy

**FIGURE 2.11**  
Graphical  
representation of  
one wavelength.



wavelength ( $\lambda$ ), frequency ( $\nu$ ), and energy ( $E$ )

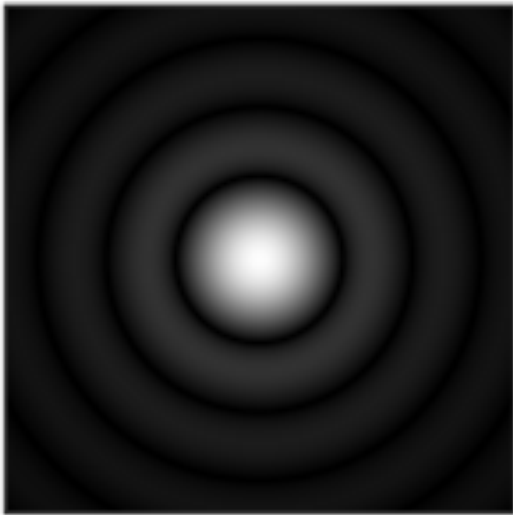
$$\lambda = \frac{c}{\nu}, \quad c = 2.998 \times 10^8 \text{ m/s is the speed of light}$$

$$E = h\nu, \quad h \text{ is the Planck's constant, } 6.626068 \times 10^{-34} \text{ m}^2 \text{ kg / s}$$

# Light and EM Spectrum

---

**What size of the object you can “see”?** Diffraction-limit.



Airy disk: the size is proportional to wavelength and f-number (focal length/lens dimension)

$$\sim \lambda \frac{f}{d}$$

[http://en.wikipedia.org/wiki/Airy\\_disc](http://en.wikipedia.org/wiki/Airy_disc)

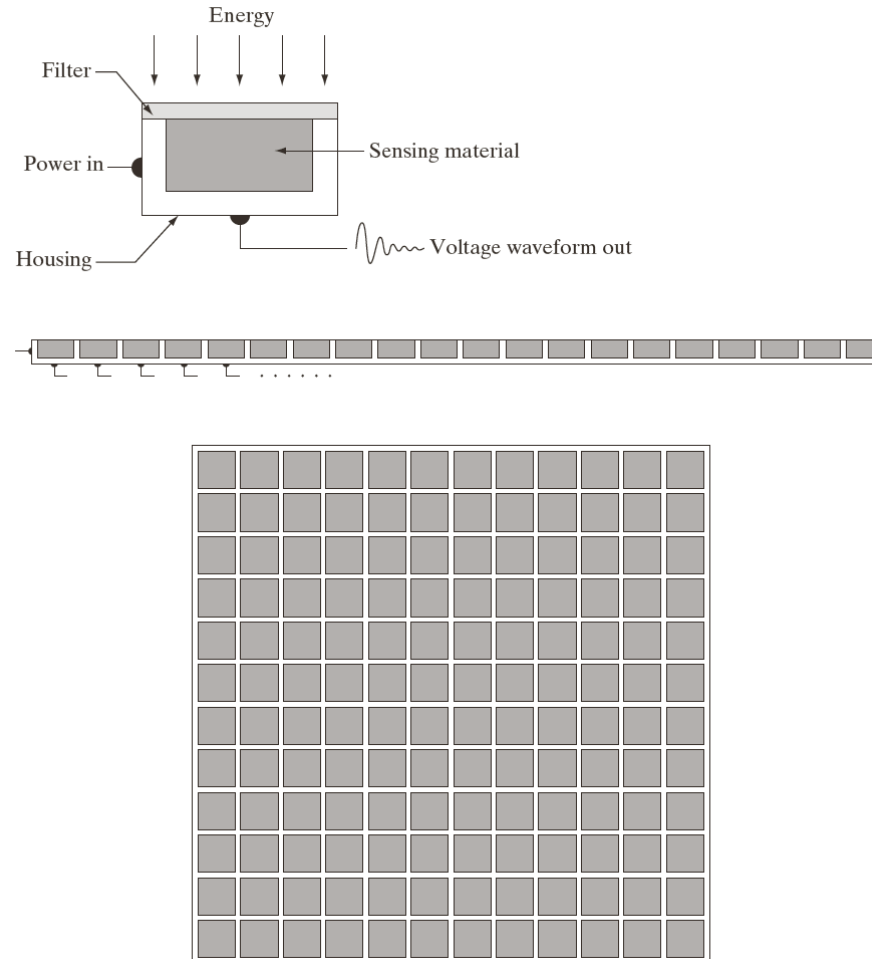


# Image Sensing and Acquisition

**Illumination energy → digital images**

**Incoming energy is transformed into a voltage**

**Digitizing the response**



a  
b  
c

**FIGURE 2.12**  
(a) Single imaging sensor.  
(b) Line sensor.  
(c) Array sensor.



# A (2D) Image

**An image = a 2D function  $f(x,y)$  where**

- $x$  and  $y$  are spatial coordinates
- $f(x,y)$  is the intensity or gray level

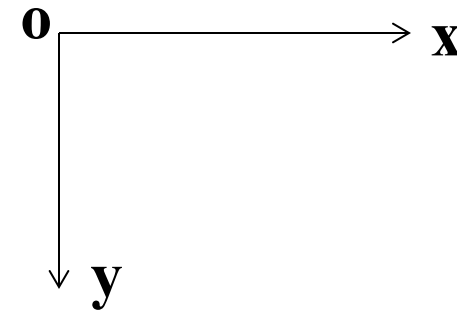
**A digital image:**

- $x$ ,  $y$ , and  $f(x,y)$  are all finite
- For example  $x \in \{1,2,\dots,M\}$ ,  $y \in \{1,2,\dots,N\}$

$$f(x, y) \in \{0,1,2,\dots,255\}$$

**Digital image processing → processing digital images by means of a digital computer**

**Each element  $(x,y)$  in a digital image is called a **pixel** (picture element)**



# A Simple Image Formation Model

---

$$f(x, y) = i(x, y) \cdot r(x, y)$$

$0 < f(x, y) < \infty$  : **Image (positive and finite)**

**Source:**  $0 < i(x, y) < \infty$  : **Illumination component**

**Object:**  $0 < r(x, y) < 1$  : **Reflectance/transmission component**

$$L_{\min} < f(x, y) < L_{\max} \quad \text{in practice}$$

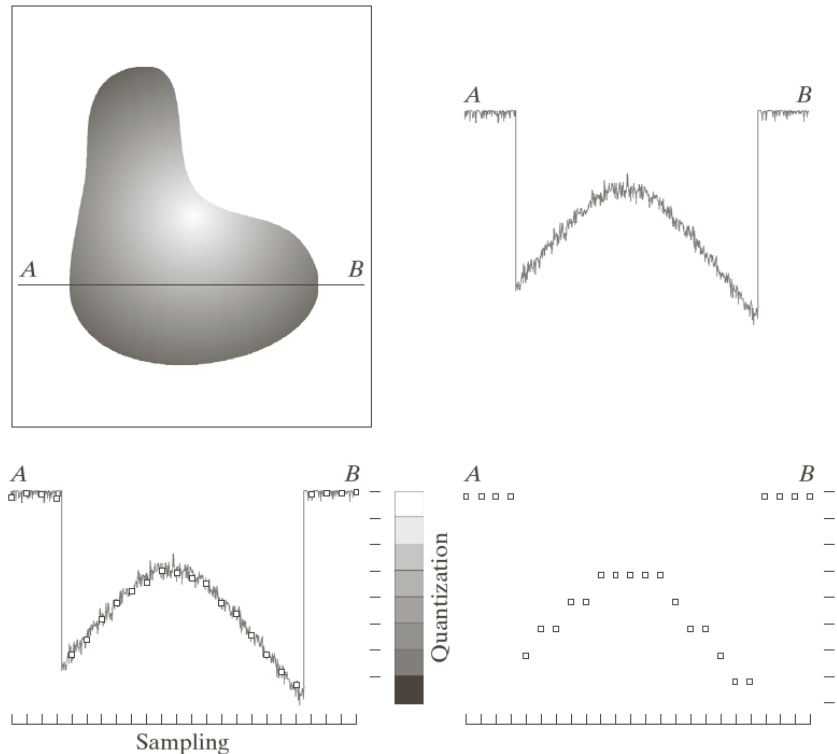
$$\text{where } L_{\min} = i_{\min} r_{\min} \quad \text{and} \quad L_{\max} = i_{\max} r_{\max}$$

**$i(x, y)$ :** **Sunlight: 10,000 lm/m<sup>2</sup> (cloudy), 90,000lm/m<sup>2</sup> clear day**  
**Office: 1000 lm/m<sup>2</sup>**

**$r(x, y)$ :** **Black velvet 0.01; white pall 0.8; 0.93 snow**



# Image Sampling and Quantization



a b  
c d

**FIGURE 2.16** Generating a digital image. (a) Continuous image. (b) A scan line from *A* to *B* in the continuous image, used to illustrate the concepts of sampling and quantization. (c) Sampling and quantization. (d) Digital scan line.

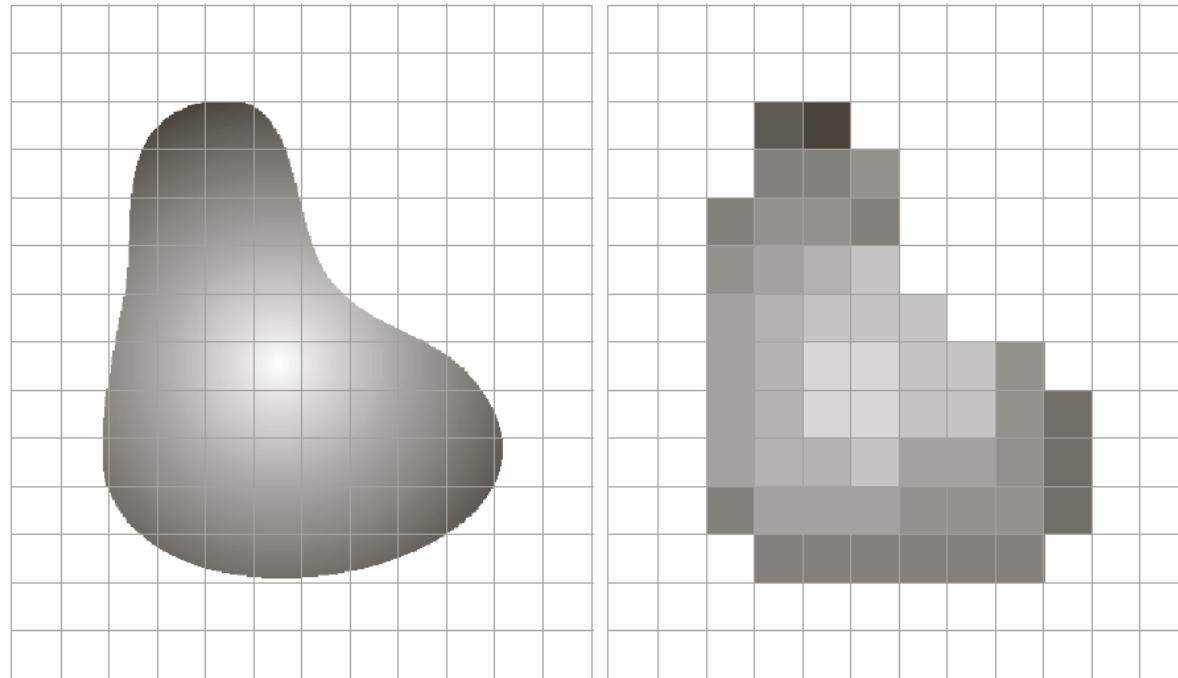
**Sampling: Digitizing the coordinate values (usually determined by sensors)**

**Quantization: Digitizing the amplitude values**





# Image Sampling and Quantization in a Sensor Array



**CCD array**

a b

**FIGURE 2.17** (a) Continuous image projected onto a sensor array. (b) Result of image sampling and quantization.

# Dynamic Range

$$L_{\min} < f(x,y) < L_{\max} \quad \text{in practice}$$

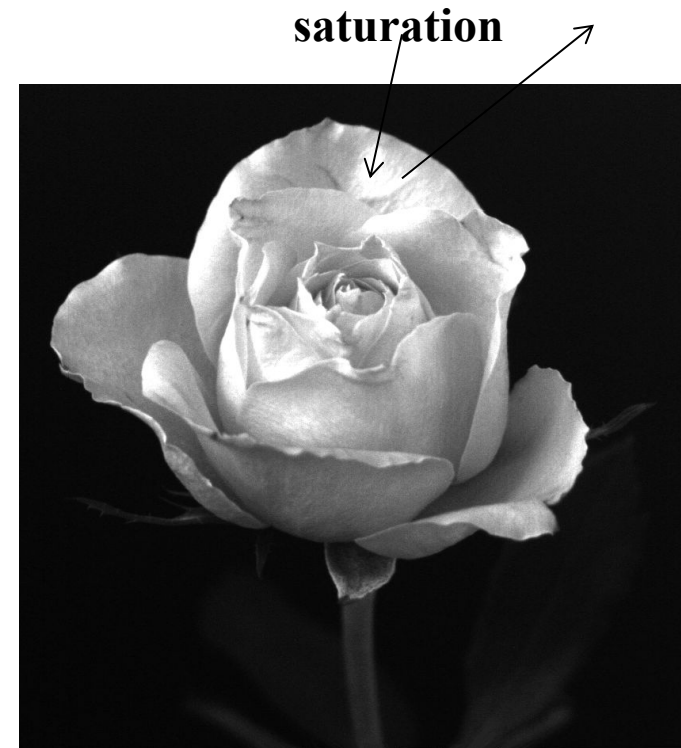
$$\text{where } L_{\min} = i_{\min} r_{\min} \quad \text{and} \quad L_{\max} = i_{\max} r_{\max}$$

$$0 \leq f(x,y) \leq L-1 \quad \text{and} \quad L = 2^k$$

**Dynamic range/contrast ratio:**

the ratio of the maximum detectable intensity level (saturation) to the minimum detectable intensity level (noise)

$$\frac{I_{\max}}{I_{\min}}$$



# High Dynamic Range

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[https://en.wikipedia.org/wiki/High-dynamic-range\\_imaging](https://en.wikipedia.org/wiki/High-dynamic-range_imaging)



# High Dynamic Range



# High Dynamic Range



# High Dynamic Range



# High Dynamic Range



# Representing Digital Images

(a):  $f(x,y)$ ,  $x=0, 1, \dots, M-1$ ,  $y=0,1, \dots, N-1$

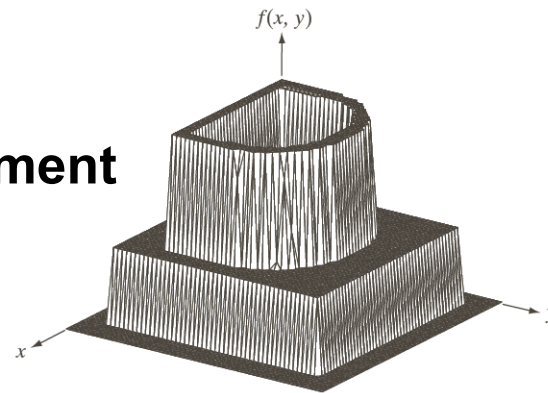
$x, y$ : spatial coordinates  $\rightarrow$  spatial domain

(b): suitable for visualization

(c): processing and algorithm development

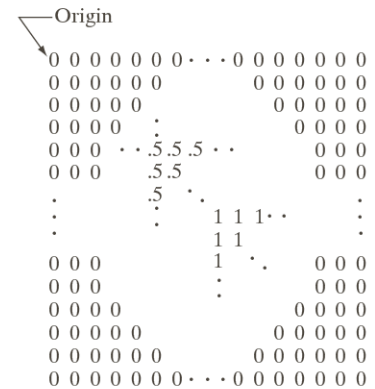
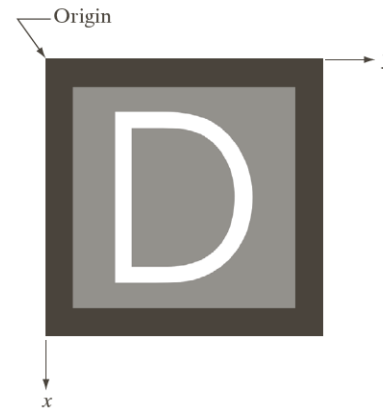
$x$ : extend downward (rows)

$y$ : extend to the right (columns)



a  
b c

**FIGURE 2.18**  
(a) Image plotted as a surface.  
(b) Image displayed as a visual intensity array.  
(c) Image shown as a 2-D numerical array (0, .5, and 1 represent black, gray, and white, respectively).



Number of bits storing the image

$$\uparrow$$
$$b = M \times N \times k$$





# Spatial Resolution

**Spatial resolution: smallest discernible details**

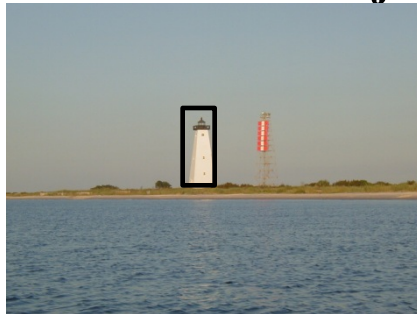
- # of line pairs per unit distance
- # of dots (pixels) per unit distance
  - Printing and publishing
  - In US, dots per inch (dpi)

Newspaper → magazines → book



**Large image size itself does not mean high spatial resolution!**

→ **Scene/object size in the image**



1280\*960

[http://www.shimanodealer.com/fishing\\_reports.htm](http://www.shimanodealer.com/fishing_reports.htm)



a b  
c d

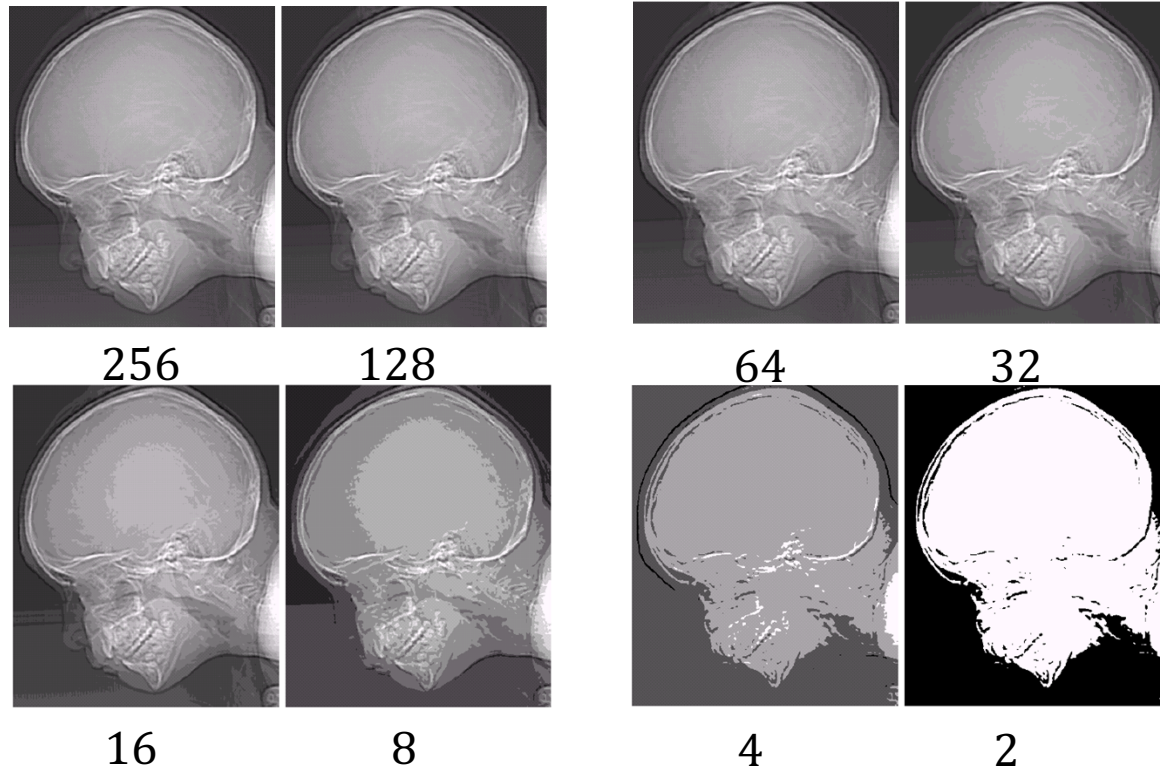
**FIGURE 2.20** Typical effects of reducing spatial resolution. Images shown at: (a) 1250 dpi, (b) 300 dpi, (c) 150 dpi, and (d) 72 dpi. The thin black borders were added for clarity. They are not part of the data.



# Intensity Resolution

## Intensity resolution

- Smallest discernible change in intensity levels
- Using the number of levels of intensities
- False contouring (banding) when  $k$  is small - undersampling



# Isopreference Curves

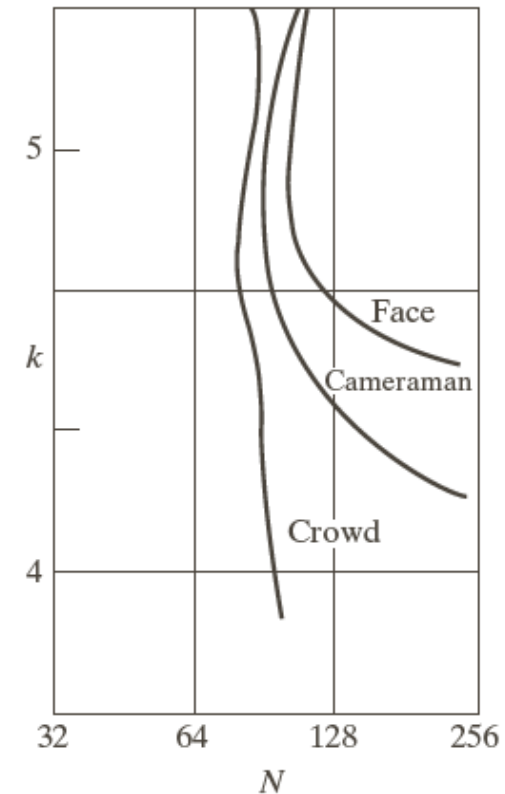


a b c

**FIGURE 2.22** (a) Image with a low level of detail. (b) Image with a medium level of detail. (c) Image with a relatively large amount of detail. (Image (b) courtesy of the Massachusetts Institute of Technology.)

**Vary the spatial and intensity sampling simultaneously:**

**FIGURE 2.23** Typical isopreference curves for the three types of images in Fig. 2.22.



# Data heavy



From GoPro HERO3+ at Barbados 2015 Field Trials

1920

1080	[	43	43	42	40	39	...	29	29	31	33	]	R
	[	42	41	40	39	38	...	31	32	35	37	]	
	[	⋮	⋮	⋮	⋮	⋮	...	⋮	⋮	⋮	⋮	]	
	[	54	57	60	62	66	...	42	43	56	46	]	
1080	[	129	129	129	129	128	...	149	149	151	153	]	G
	[	128	128	127	128	127	...	151	152	155	157	]	
	[	⋮	⋮	⋮	⋮	⋮	...	⋮	⋮	⋮	⋮	]	
	[	146	146	148	148	148	...	149	150	151	152	]	
1080	[	146	146	146	145	146	...	166	166	168	170	]	B
	[	145	145	144	144	145	...	168	169	172	174	]	
	[	⋮	⋮	⋮	⋮	⋮	...	⋮	⋮	⋮	⋮	]	
	[	159	160	160	161	162	...	165	166	165	166	]	

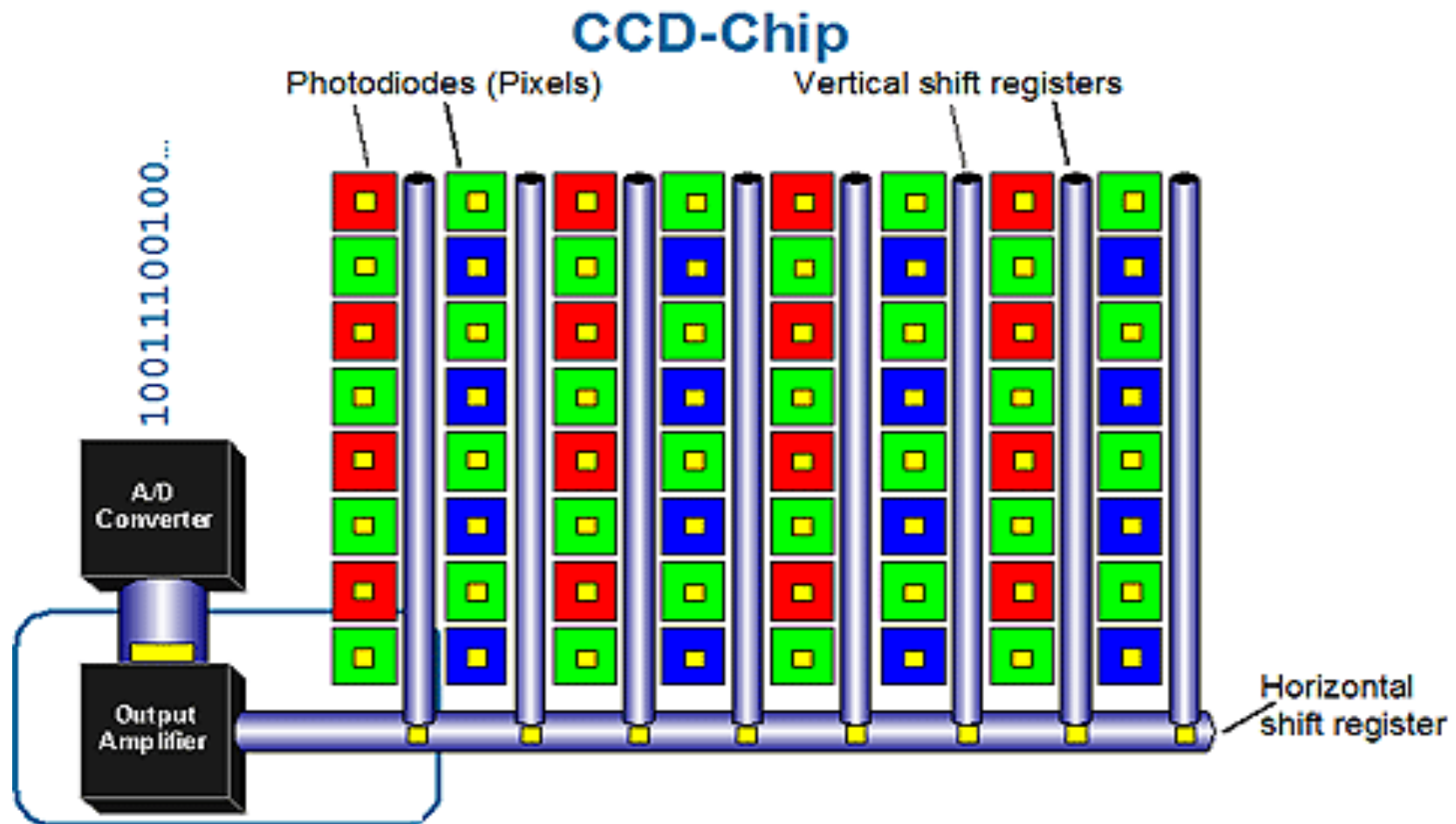
# Aliasing

---

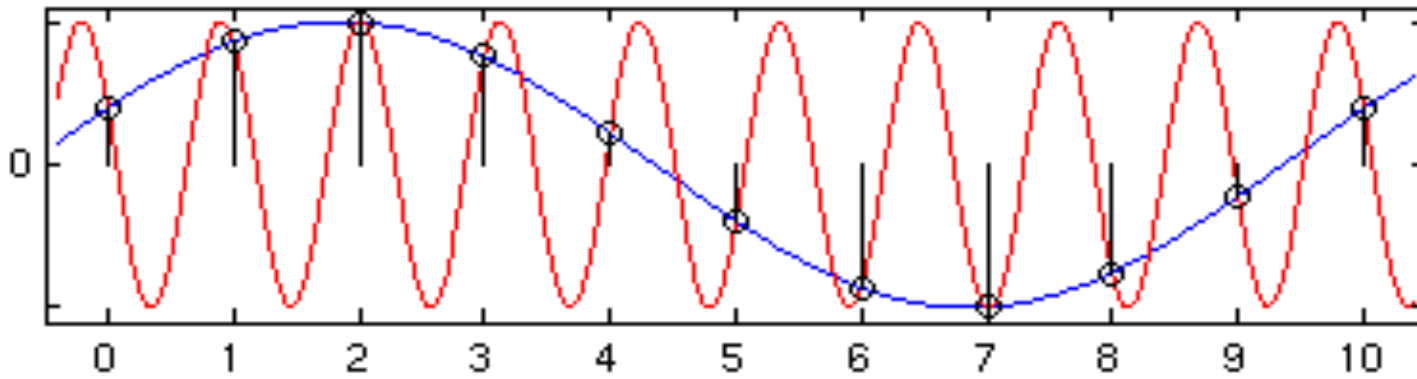
- Images are not actually continuous.
- The sampling (and hardware) issues lead to a few other minor problems.



# Aliasing



# Aliasing

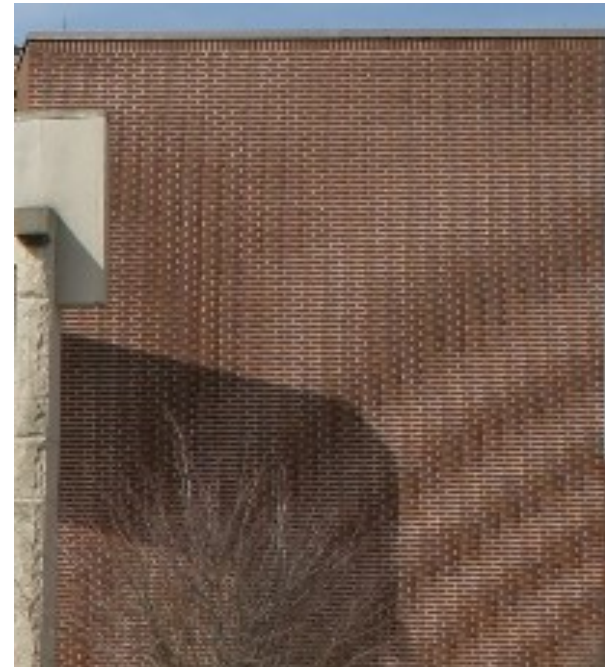
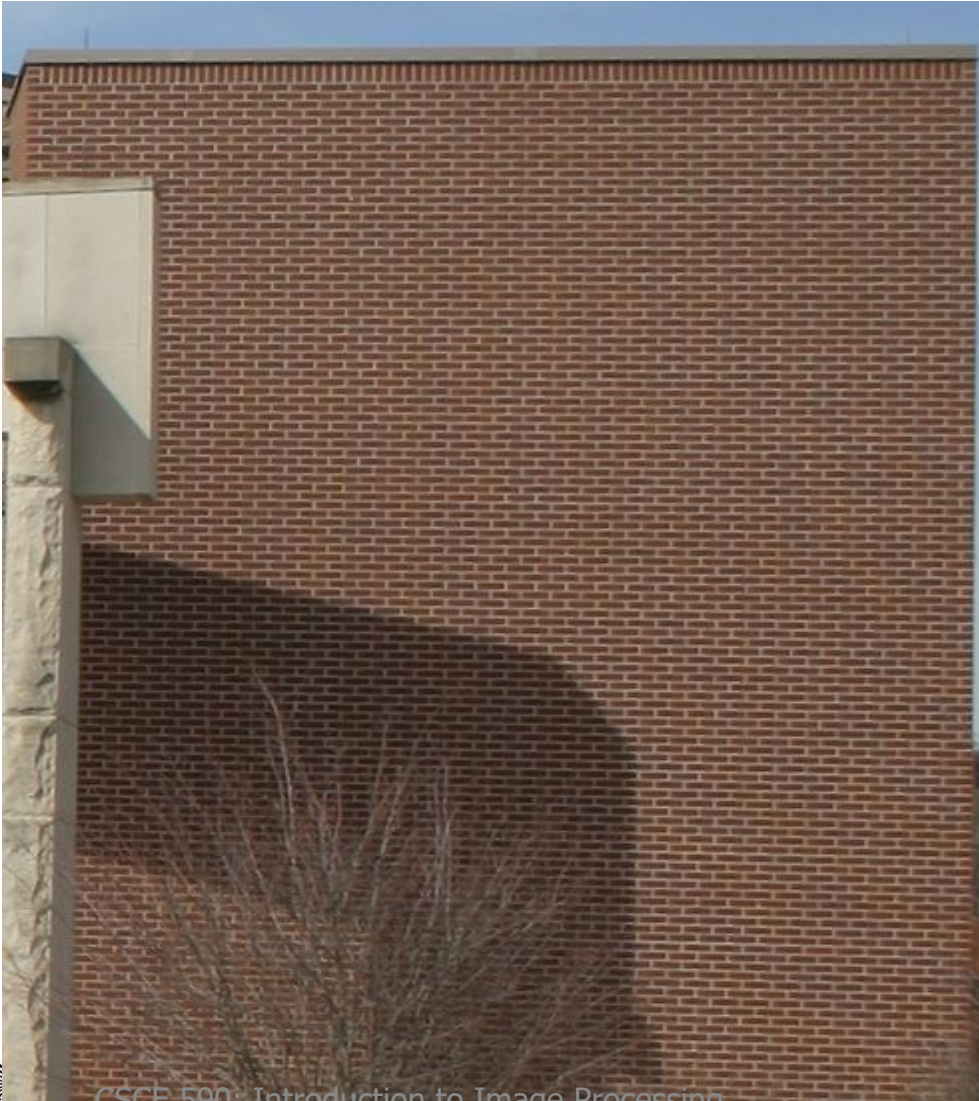


- To avoid:  $f_{sampling} > 2F_{max}$ 
  - Nyquist Rate



# Aliasing: Moiré Patterns

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# Ill-posed

- What a camera does to the 3d world...

Shigeo Fukuda



squeezes away one dimension

[http://www.psychologie.tu-dresden.de/i1/kaw/diverses\\_Material/www.illusionworks.com/html/art\\_of\\_shigeo\\_fukuda.html](http://www.psychologie.tu-dresden.de/i1/kaw/diverses_Material/www.illusionworks.com/html/art_of_shigeo_fukuda.html)



# Ill-posed

- What a camera does to the 3d world...

Shigeo Fukuda



<http://www.psychologie.tu-dresden.de/i1/kaw/diverses> Material/[www.illusionworks.com/html/art\\_of\\_shigeo\\_fukuda.html](http://www.illusionworks.com/html/art_of_shigeo_fukuda.html)



# Ill-posed

---

- In trying to extract 3d structure from 2d images, vision is an *ill-posed* problem.



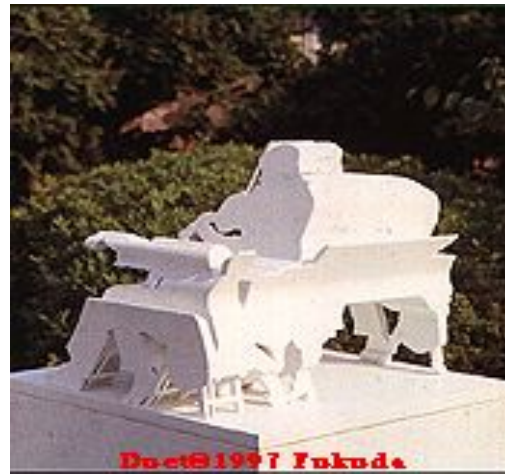
# Ill-posed

- In trying to extract 3d structure from 2d images, vision is an *ill-posed* problem.



# Ill-posed

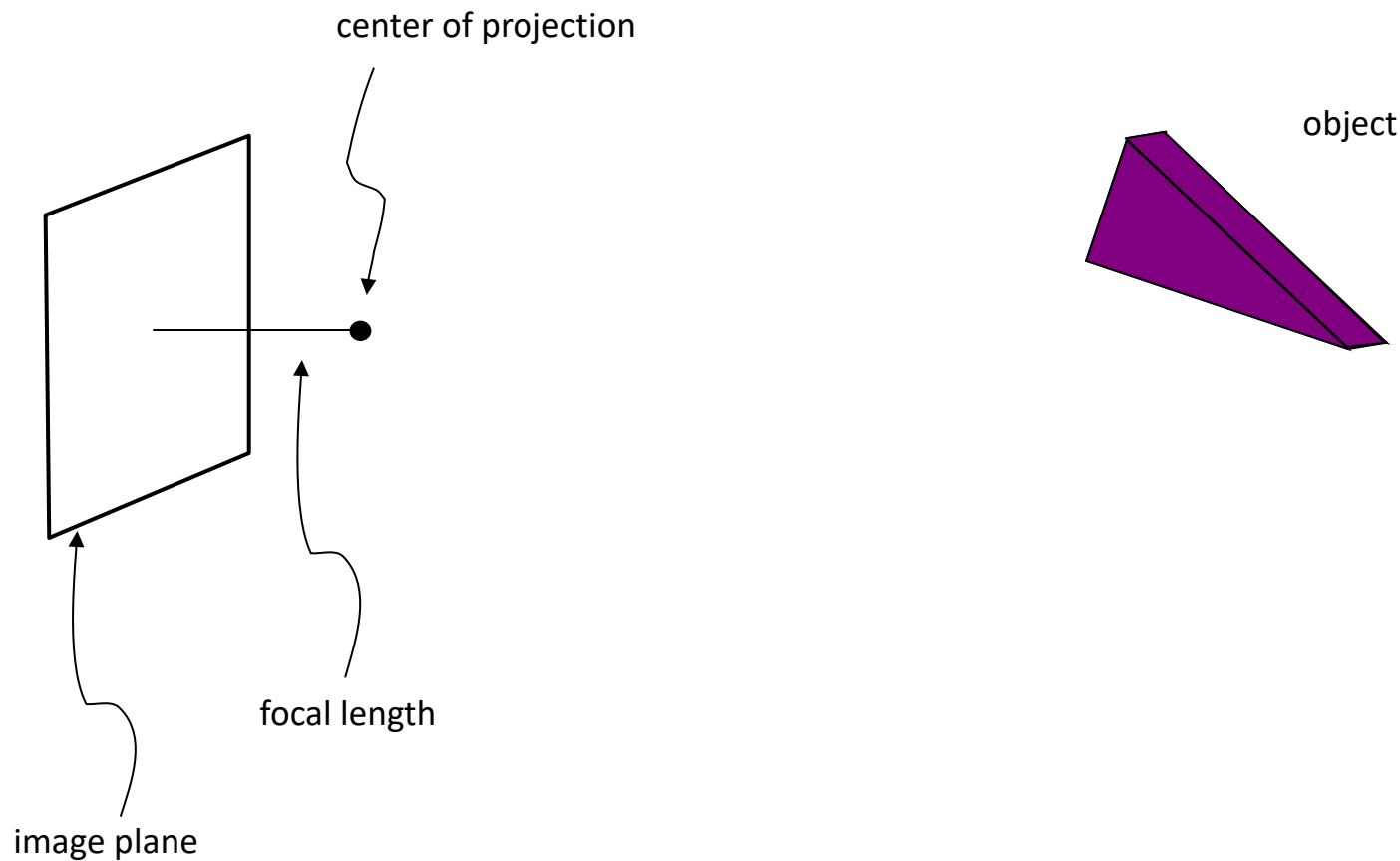
- In trying to extract 3d structure from 2d images, vision is an *ill-posed* problem.



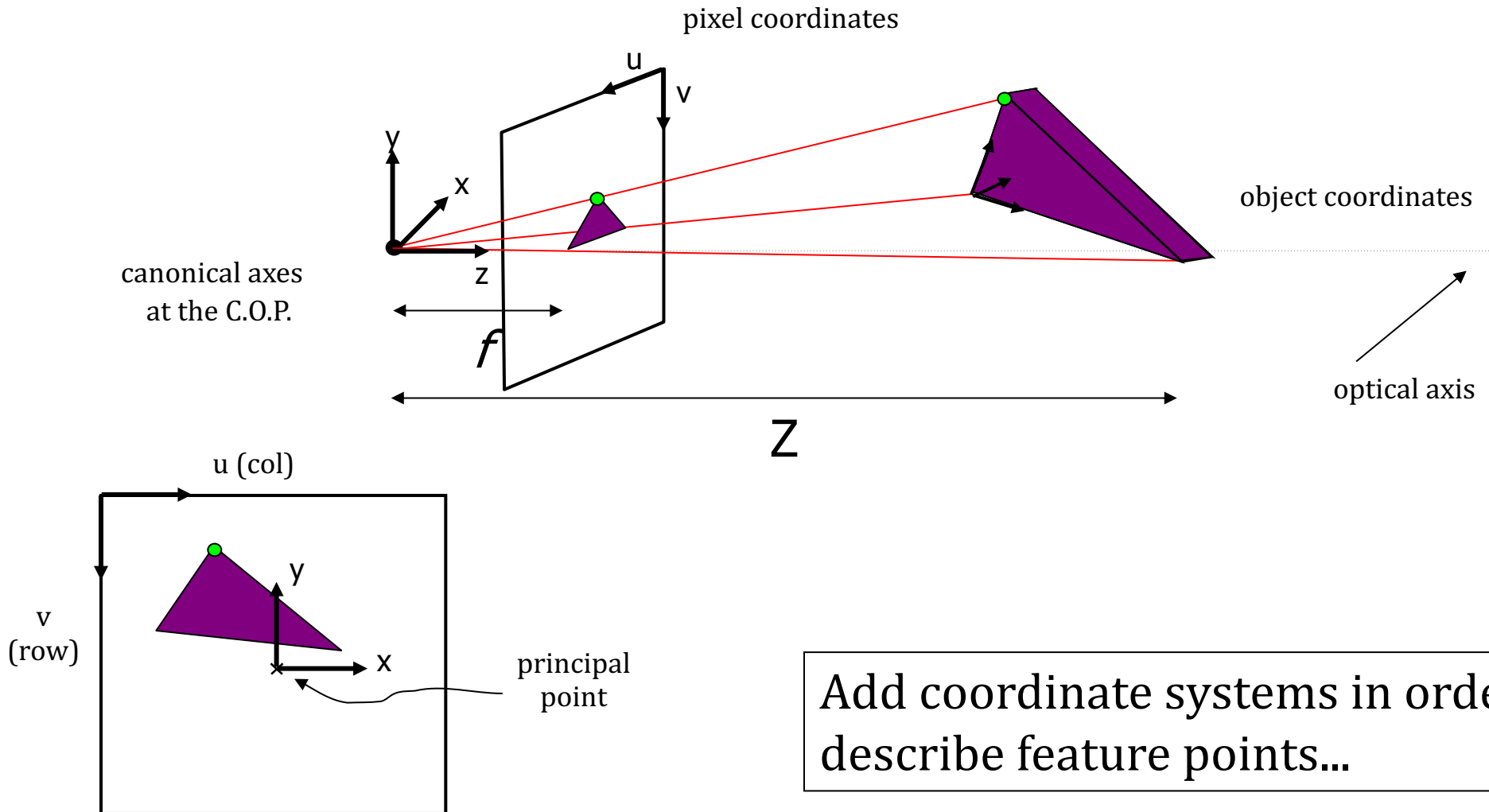
- An image isn't enough to disambiguate the many possible 3d worlds that could have produced it.

# Camera Geometry

## 3D $\rightarrow$ 2D transformation: perspective projection



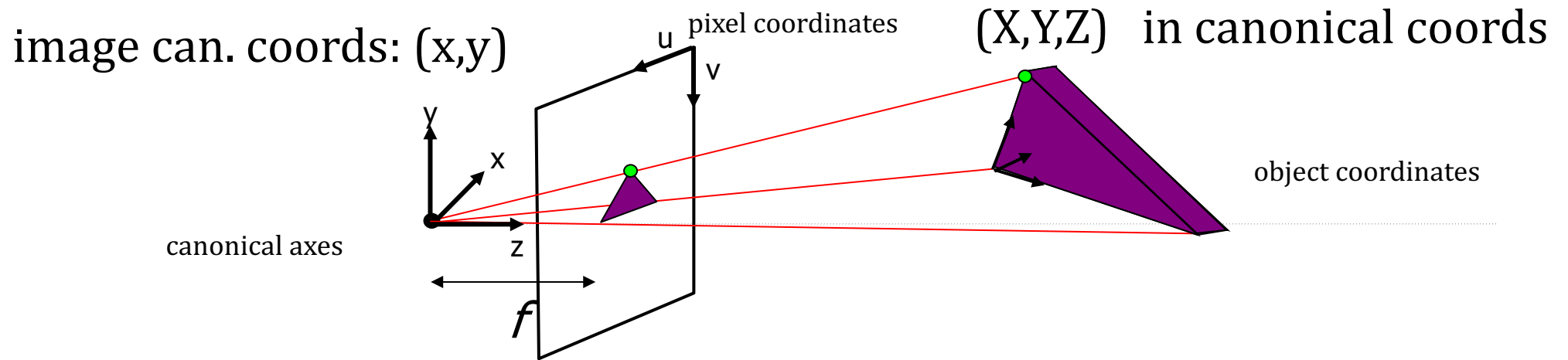
# Coordinate Systems



Add coordinate systems in order to describe feature points...

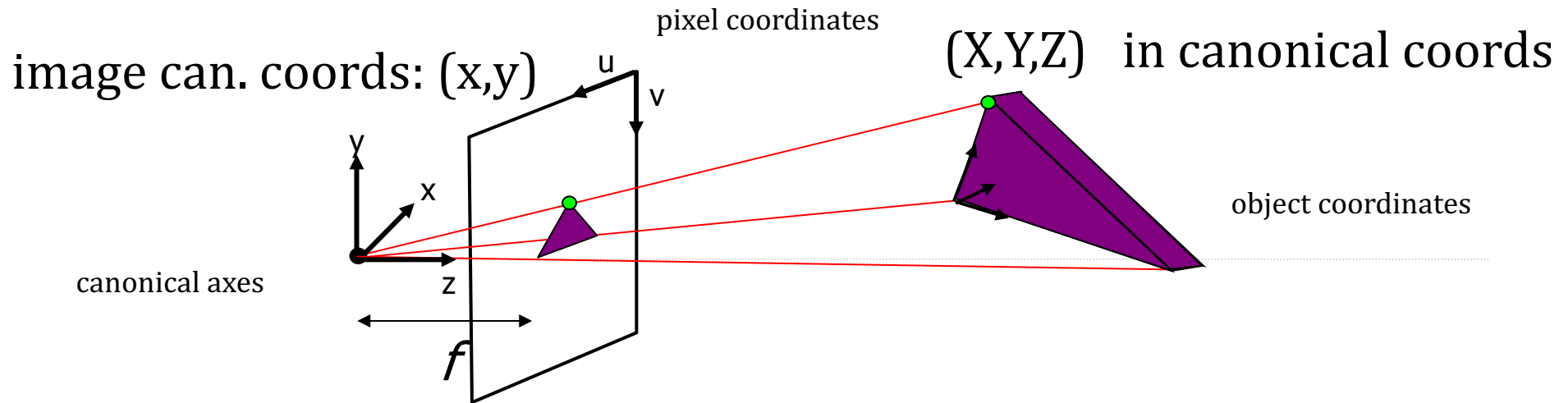


# Coordinate Systems





# From 3d to 2d



$$x = \frac{fX}{Z} \quad y = \frac{fY}{Z}$$

a nonlinear transformation

goal: to recover information about  $(X,Y,Z)$  from  $(x,y)$

# Camera Calibration

- Camera Model

- $[u \ v \ 1]$  Pixel coords

- $[x_w \ y_w \ z_w \ 1]^T$  World coords

$$z_c \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = A \begin{bmatrix} R & T \end{bmatrix} \begin{bmatrix} x_w \\ y_w \\ z_w \\ 1 \end{bmatrix}$$

- Intrinsic Parameters

- $\alpha_x = f \cdot m_x, \alpha_y = f \cdot m_y$  focal lengths in pixels

- $\gamma$  skew coefficient

- $u_0, v_0$  focal point

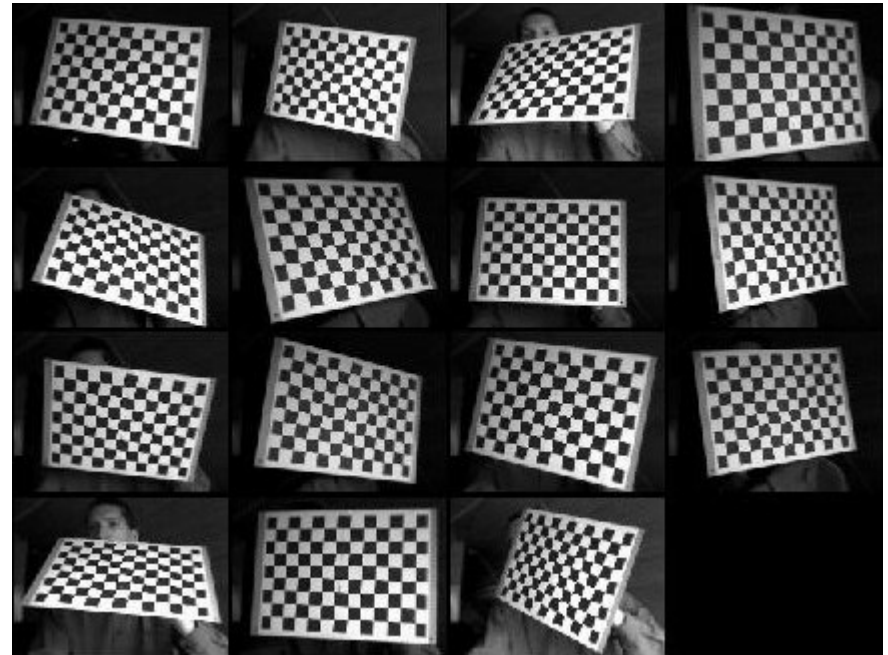
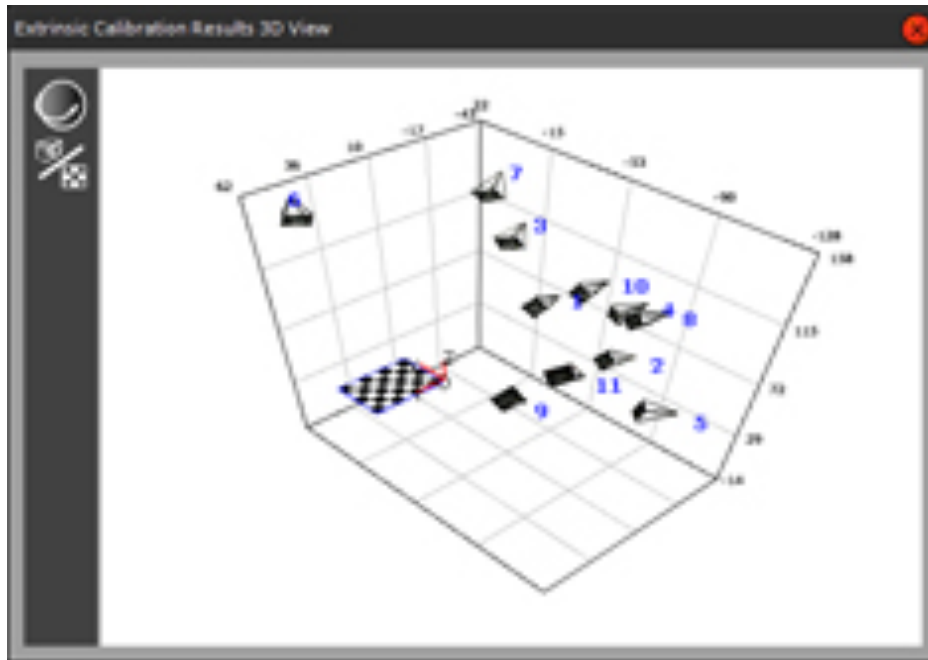
$$A = \begin{bmatrix} \alpha_x & \gamma & u_0 \\ 0 & \alpha_y & v_0 \\ 0 & 0 & 1 \end{bmatrix}$$

- Extrinsic Parameters

- $[R \ T]$  Rotation and Translation



# Camera Calibration



Existing packages in MATLAB, OpenCV, etc



# Rectified Image Sample

---

Unrectified



Rectified



From Clearpath Husky Axis M1013 camera

# Rectified Image Sample

---

Unrectified



Rectified



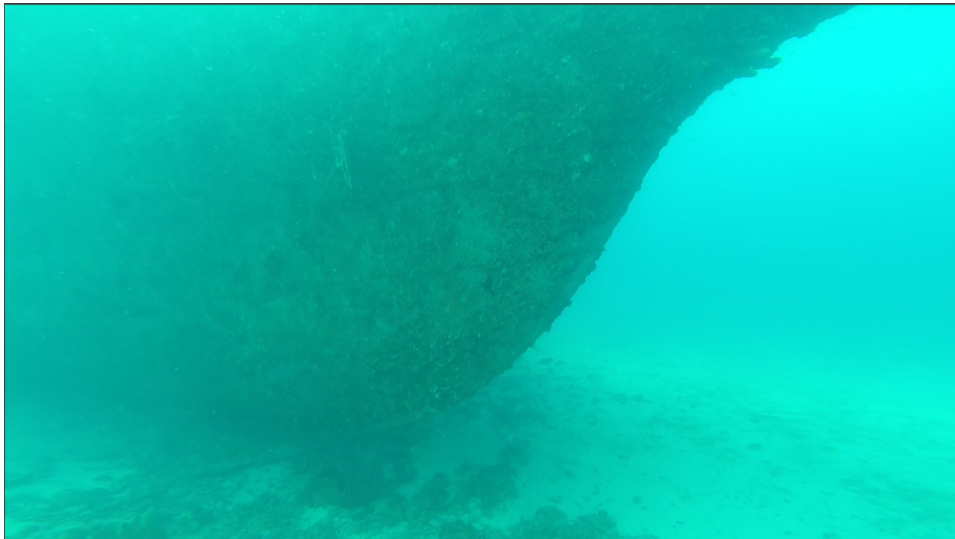
From Parrot ARDrone 2.0 front camera



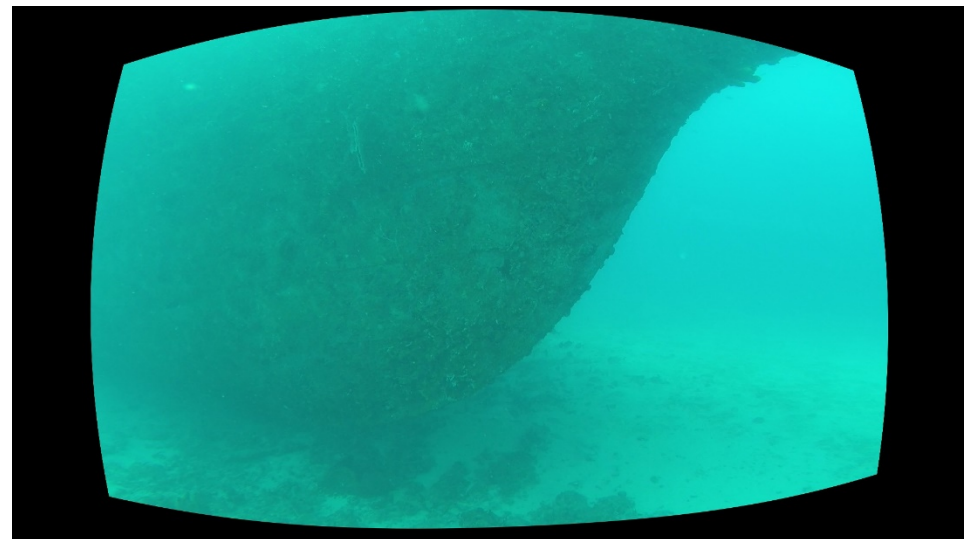
# Rectified Image Sample

---

Unrectified



Rectified



From GoPro HERO3+ at Barbados 2015 Field Trials

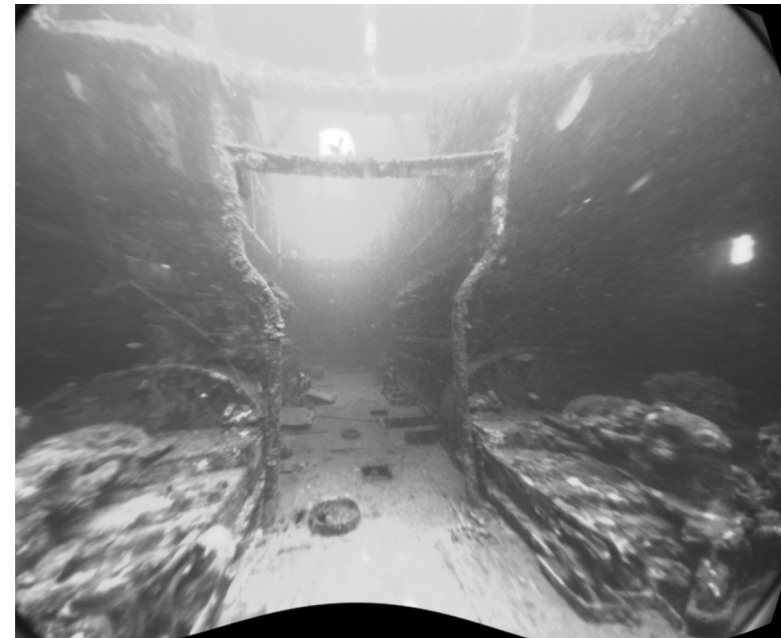
# ReRectified Image Sample

---

Rectified



ReRectified



From Aqua front camera at Barbados 2013 Field Trials