

CSCE 574 ROBOTICS

Path Planning



Outline

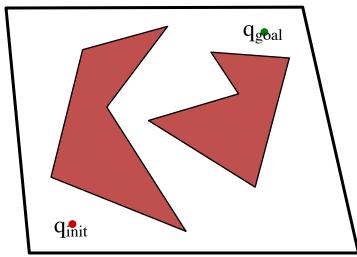
- Path Planning
 - Potential Fields
 - Visibility Graph
 - Bug Algorithms
 - Skeletons/Voronoi Graphs
 - C-Space

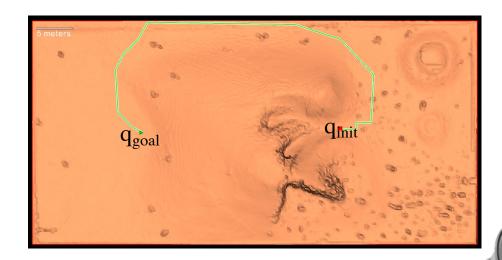


Motion Planning

- The ability to go from A to B
 - Known map Off-line planning
 - Unknown Environment Online planning
 - Static/Dynamic Environment

 $\bullet q_{init}$ $\bullet q_{goal}$







World

Robot

Мар





World

- •Indoor/Outdoor
- •2D/2.5D/3D
- •Static/Dynamic
- •Known/Unknown
- Abstract (web)

Мар

Robot





World

Robot

- Mobile
 - ➤ Indoor/Outdoor
 - ➤ Walking/Flying/Swimming
- Manipulator
- •Humanoid
- Abstract

Мар





World

Robot

Мар

- Topological
- Metric
- •Feature Based
- •1D,2D,2.5D,3D





World

- Indoor/Outdoor
- •2D/2.5D/3D
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- Known/Unknown
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Robot

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- Humanoid
- Abstract

Map

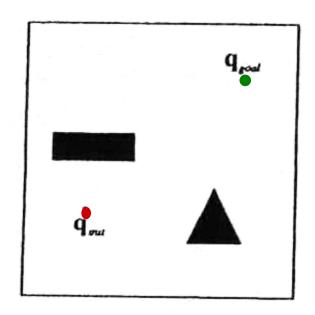
- Topological
- Metric
- •Feature Based
- •1D,2D,2.5D,3D

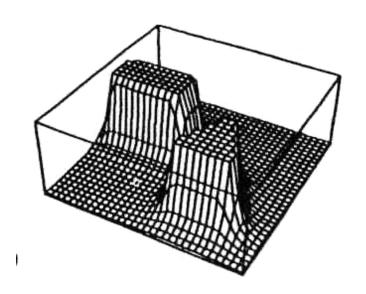




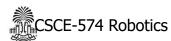
Potential Field methods

• compute a repulsive force away from obstacles





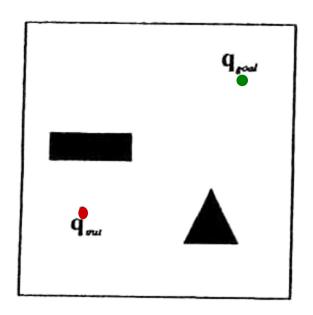


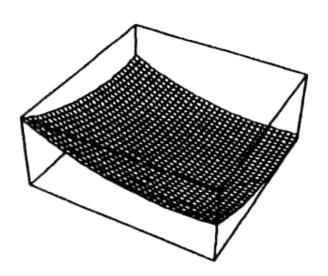


Local techniques

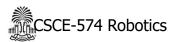
Potential Field methods

- compute a repulsive force away from obstacles
- compute an attractive force toward the goal





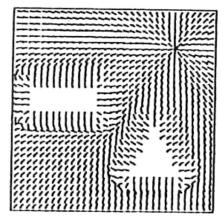




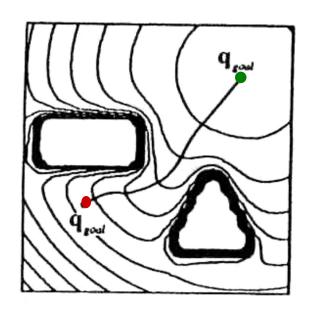
Local techniques

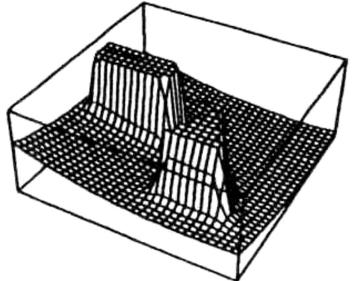
Potential Field methods

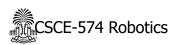
- compute a repulsive force away from obstacles
- compute an attractive force toward the goal
- → let the sum of the forces control the robot



key advantages



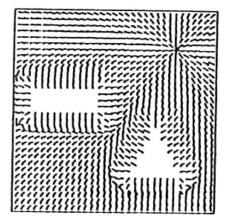


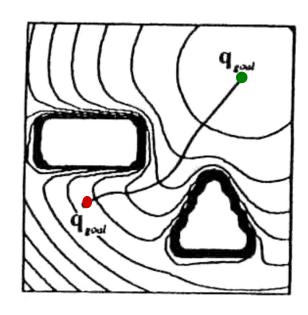


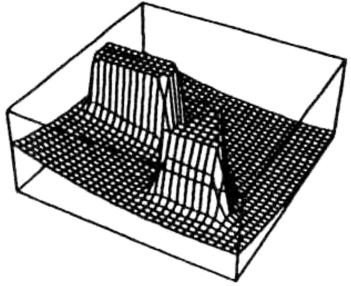
Local techniques

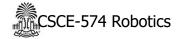
Potential Field methods

- compute a repulsive force away from obstacles
- compute an attractive force toward the goal
- → let the sum of the forces control the robot



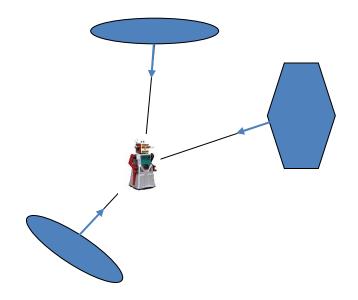






To a large extent, this is computable from sensor readings

Sensor Based Calculations





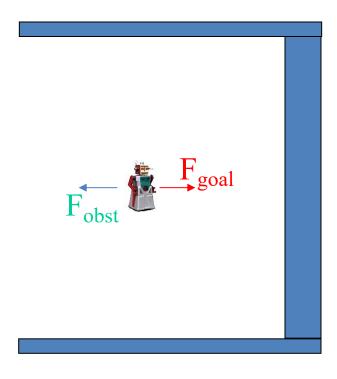


Major Problem?





Local Minima!









Simulated Annealing

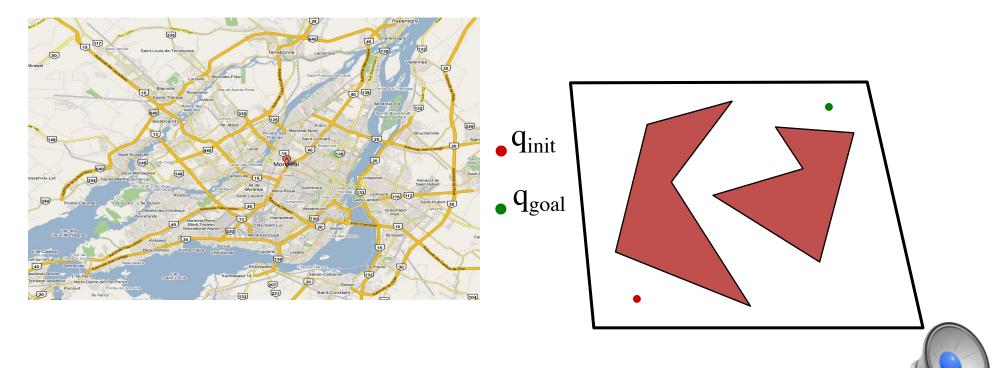
Every so often add some random force





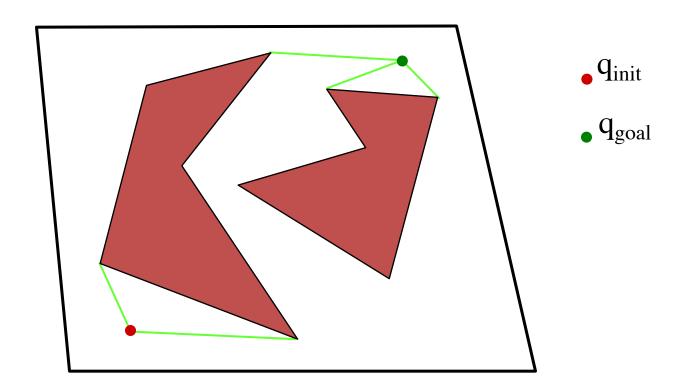
Path Planning: Assumptions

- Known Map
- Roadmaps (Graph representations)
- Polygonal Representation



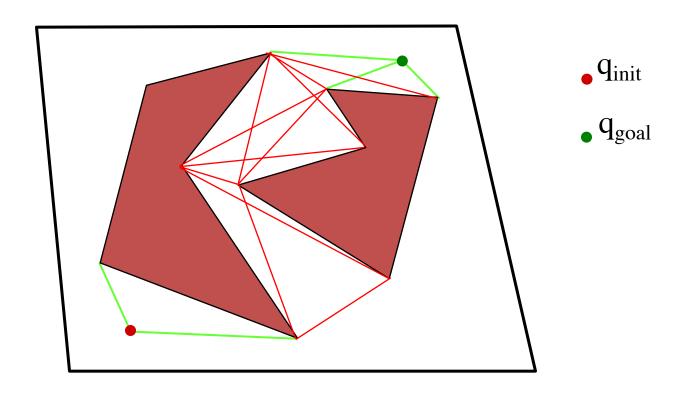


Connect Initial and goal locations with all the visible vertices





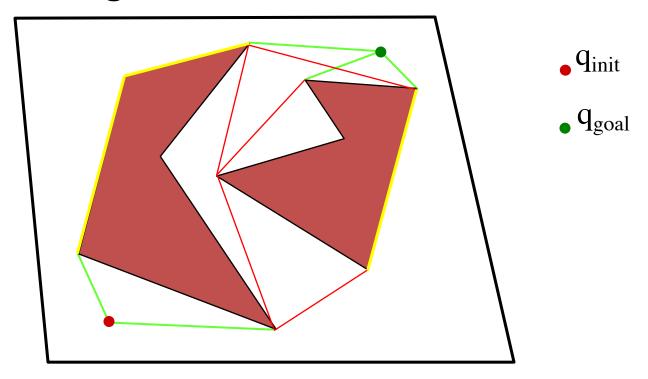
- Connect initial and goal locations with all the visible vertices
- Connect each obstacle vertex to every visible obstacle vertex







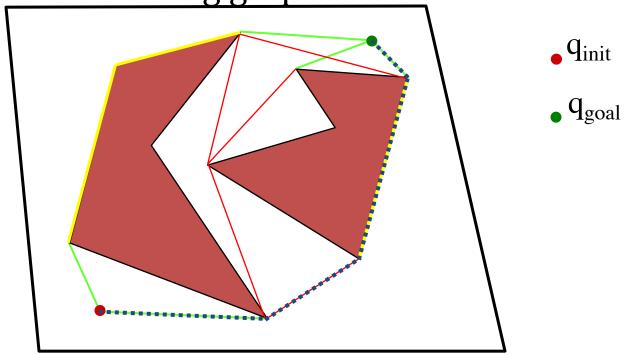
- Connect initial and goal locations with all the visible vertices
- Connect each obstacle vertex to every visible obstacle vertex
- Remove edges that intersect the interior of an obstacle





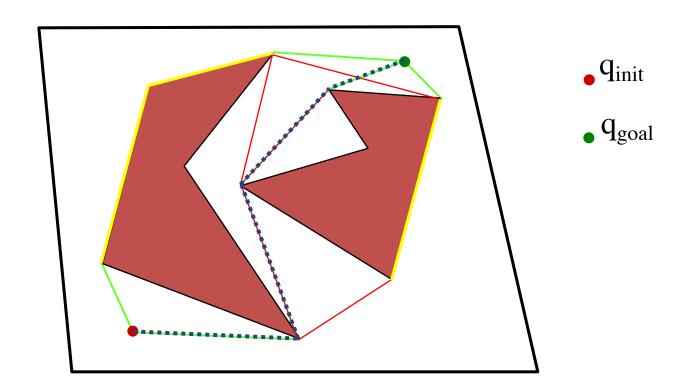
- Connect initial and goal locations with all the visible vertices
- Connect each obstacle vertex to every visible obstacle vertex
- Remove edges that intersect the interior of an obstacle

• Plan on the resulting graph





- An alternative path
- Alternative name: "Rubber band algorithm"







Major Fault

- Point robot
- Path planning like that guarantees to hit the obstacles

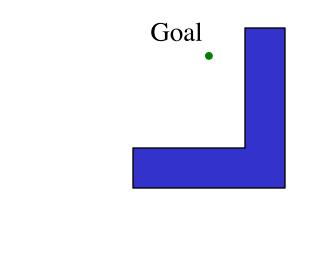






Limited-knowledge path planning

- Path planning with limited knowledge
 - Insect-inspired "bug" algorithms



- known direction to goal
- otherwise local sensing
 walls/obstacles encoders
- •"reasonable" world
- 1. finitely many obstacles in any finite disc
- 2. a line will intersect an obstacle finitely many times



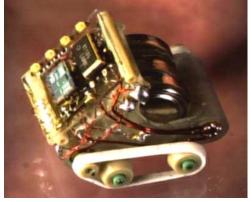


Not truly modeling bugs...

Insects do use several cues for navigation:



visual landmarks
polarized light
chemical sensing



neither are the current bugsized robots

they're not ears...

Other animals use information from

magnetic fields

electric currents

temperature



CSCE-574 Robotics

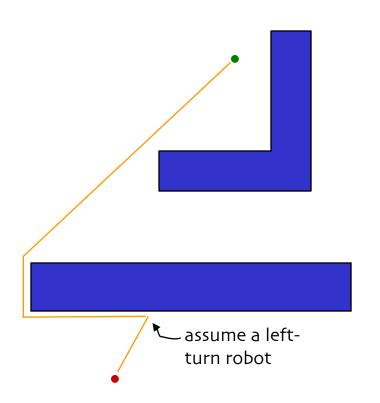
bacteria





Bug Strategy

Insect-inspired "bug" algorithms



- known direction to goal •
- otherwise only local sensing walls/obstacles encoders

"Bug 0" algorithm

- 1) head toward goal
- 2) follow obstacles until you can head toward the goal again
- 3) continue





Does It Work?



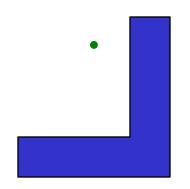


Bug 1

Insect-inspired "bug" algorithms

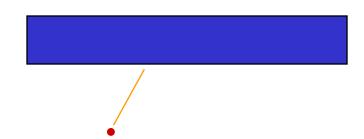


 otherwise only local sensing walls/obstacles encoders



"Bug 1" algorithm

1) head toward goal





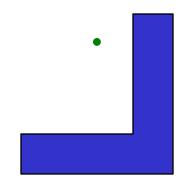


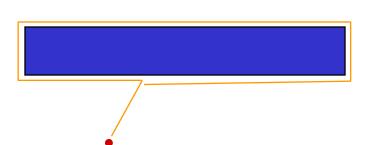
Bug 1

Insect-inspired "bug" algorithms



 otherwise only local sensing walls/obstacles encoders





"Bug 1" algorithm

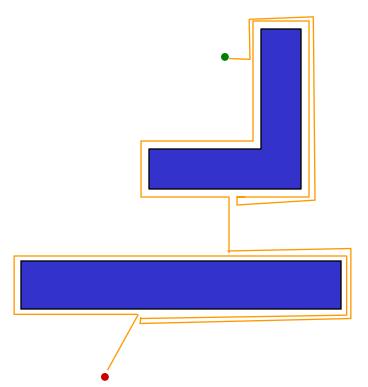
- 1) head toward goal
- 2) if an obstacle is encountered, circumnavigate it *and* remember how close you get to the goal





Bug 1

Insect-inspired "bug" algorithms



- known direction to goal
- otherwise only local sensing walls/obstacles encoders

"Bug 1" algorithm

- 1) head toward goal
- 2) if an obstacle is encountered, circumnavigate it *and* remember how close you get to the goal
- 3) return to that closest point (by wall-following) and continue



Bug 1 analysis

Distance Traveled

What are bounds on the path length that the robot takes?



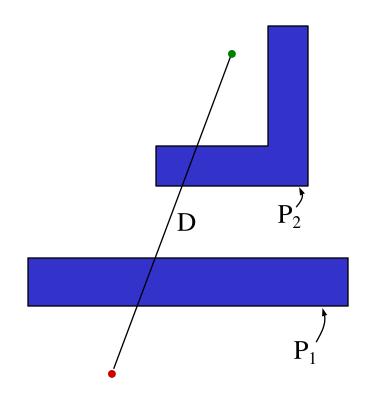
D = straight-line distance from start to goal

 P_i = perimeter of the *i*th obstacle

Lower and upper bounds?

Lower bound:

Upper bound:







Bug 1 analysis

Distance Traveled

What are bounds on the path length that the robot takes?

Available Information:

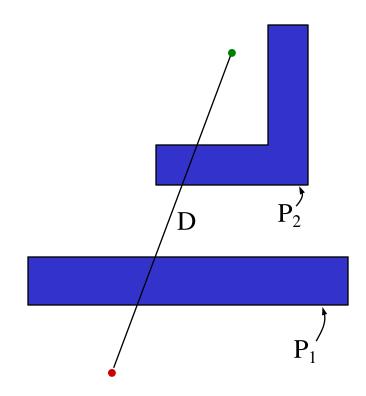
D = straight-line distance from start to goal

 P_i = perimeter of the /th obstacle

Lower and upper bounds?

Lower bound: D

Upper bound:







Bug 1 analysis

Distance Traveled

What are bounds on the path length that the robot takes?

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 P_i = perimeter of the /th obstacle

Lower and upper bounds?

Lower bound: D

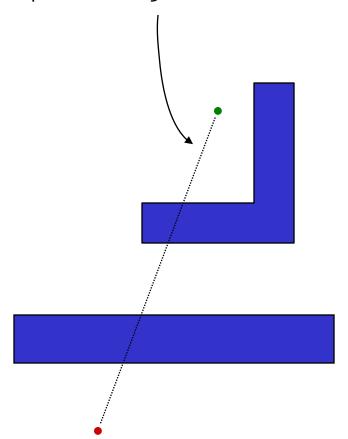
Upper bound: $D + 1.5 \sum_{i} P_{i}$

How good a bound? How good an algorithm?



A better bug?

Call the line from the starting point to the goal the *s-line*



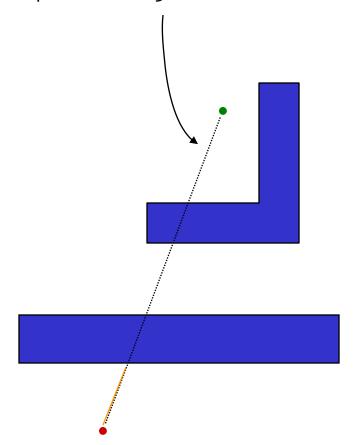
"Bug 2" algorithm





A better bug?

Call the line from the starting point to the goal the *s-line*



"Bug 2" algorithm

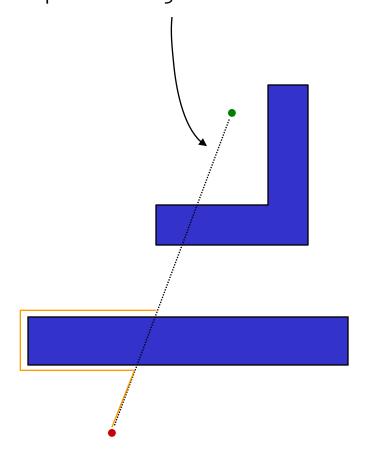
1) head toward goal on the *s-line*





A better bug?

Call the line from the starting point to the goal the *s-line*



"Bug 2" algorithm

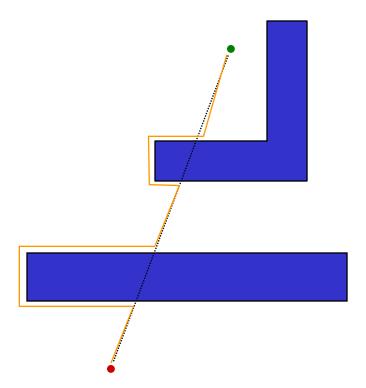
- 1) head toward goal on the *s-line*
- 2) if an obstacle is in the way, follow it until encountering the sline again.





A better bug?

s-line



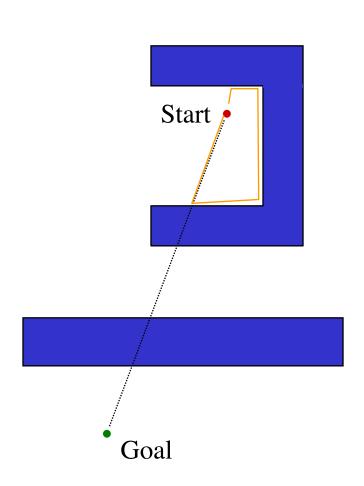
"Bug 2" algorithm

- 1) head toward goal on the *s-line*
- 2) if an obstacle is in the way, follow it until encountering the sline again.
- 3) Leave the obstacle and continue toward the goal





A better bug?

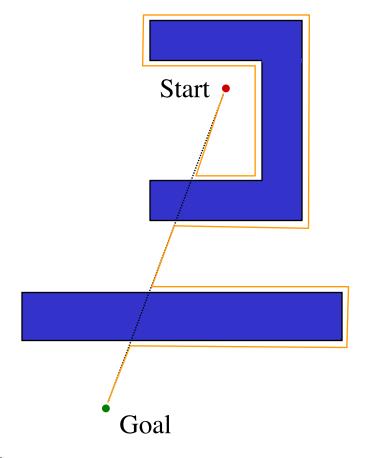


"Bug 2" algorithm

- 1) head toward goal on the *s-line*
- 2) if an obstacle is in the way, follow it until encountering the sline again *closer to the goal*.
- 3) Leave the obstacle and continue toward the goal



Distance Traveled



What are bounds on the path length that the robot takes?

Available Information:

D = straight-line distance from start to goal

 P_i = perimeter of the /th obstacle

Lower and upper bounds?

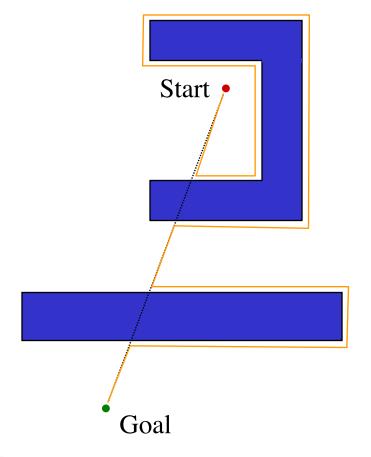
Lower bound:

Upper bound:





Distance Traveled



What are bounds on the path length that the robot takes?

Available Information:

D = straight-line distance from start to goal

 P_i = perimeter of the *i*th obstacle

 N_i = number of s-line intersections with the ith obstacle

Lower and upper bounds?

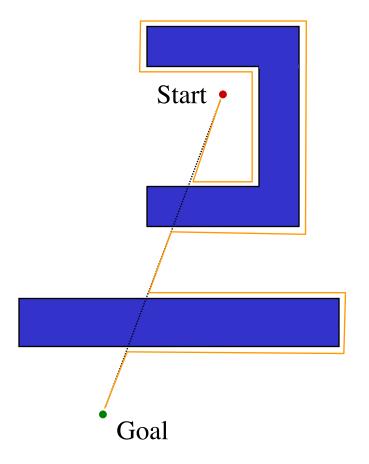
Lower bound:

Upper bound:





Distance Traveled



What are bounds on the path length that the robot takes?

Available Information:

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 P_i = perimeter of the *i*th obstacle

 N_i = number of s-line intersections with the ith obstacle

Lower and upper bounds?

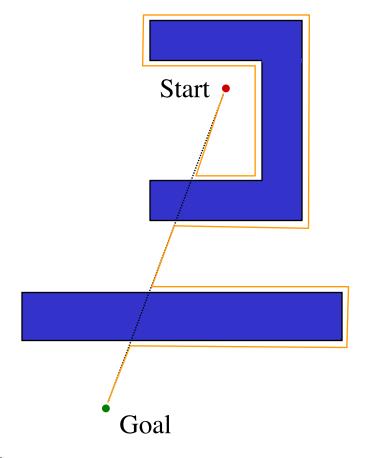
Lower bound: D

Upper bound:





Distance Traveled



What are bounds on the path length that the robot takes?

Available Information:

D = straight-line distance from start to goal

 P_i = perimeter of the /th obstacle

 N_i = number of s-line intersections with the ith obstacle

Lower and upper bounds?

Lower bound: D

Upper bound: $D + 0.5 \sum_{i} N_i P_i$



head-to-head comparison

or thorax-to-thorax, perhaps

What are worlds in which Bug 2 does better than Bug 1 (and vice versa)?

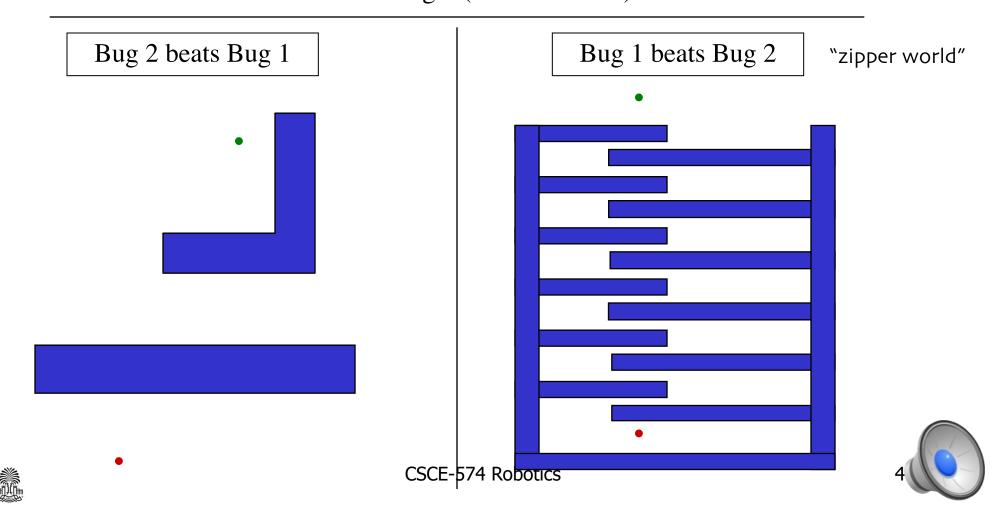
Bug 2 beats Bug 1 Bug 1 beats Bug 2



head-to-head comparison

or thorax-to-thorax, perhaps

What are worlds in which Bug 2 does better than Bug 1 (and vice versa)?



Bug Mapping

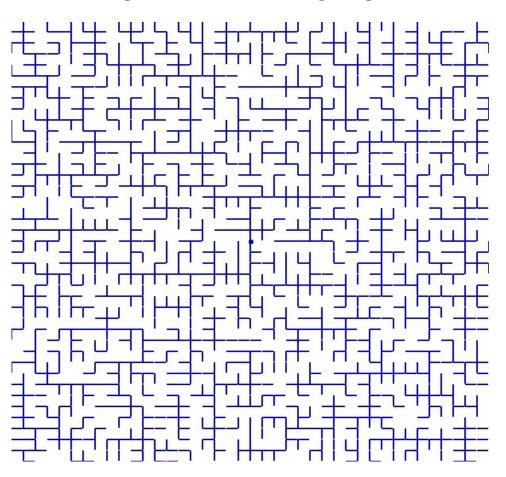






Other bug-like algorithms

The Pledge maze-solving algorithm



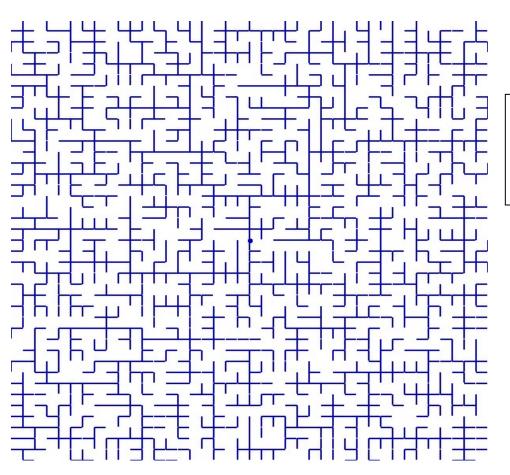
- 1. Go to a wall
- 2. Keep the wall on your right
- 3. Continue until out of the maze





Other bug-like algorithms

The Pledge maze-solving algorithm



- 1) Go to a wall
- 2) Keep the wall on your right
- 3) Continue until out of the maze

int a[1817]; main(z,p,q,r){for(p=80;q+p-80;p=2*a[p]) for(z=9;z--;)q=3&(r=time(0)+r*57)/7,q=q?q-1?q-2?1-p%79?-1:0:p%79-77?1:0:p<1659?79:0:p>158?-79:0,q?!a[p+q*2]?a[p+=a[p+=q]=q]=q:0:0;for(;q++-1817;)printf(q%79?"%c":"%c\n"," #"[!a[q-1]]);}

IOCCC random maze generator

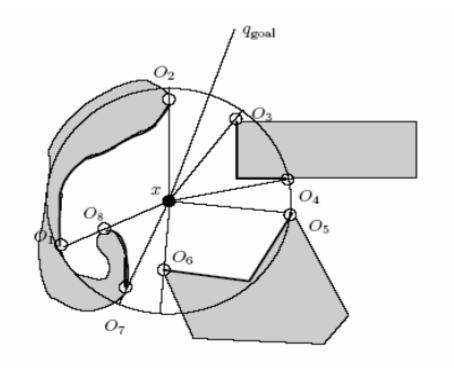


discretized RRT

CSCE-574 Robotics

Tangent Bug

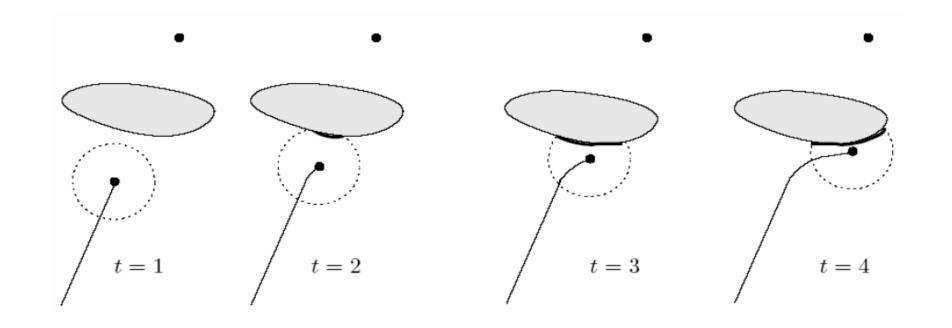
- Limited Range Sensor
- Tangent Bug relies on finding endpoints of finite, continues segments of the obstacles







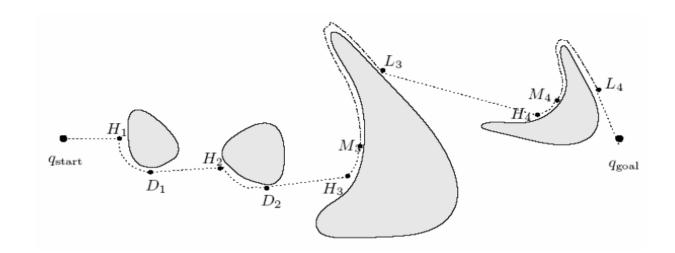
Tangent Bug







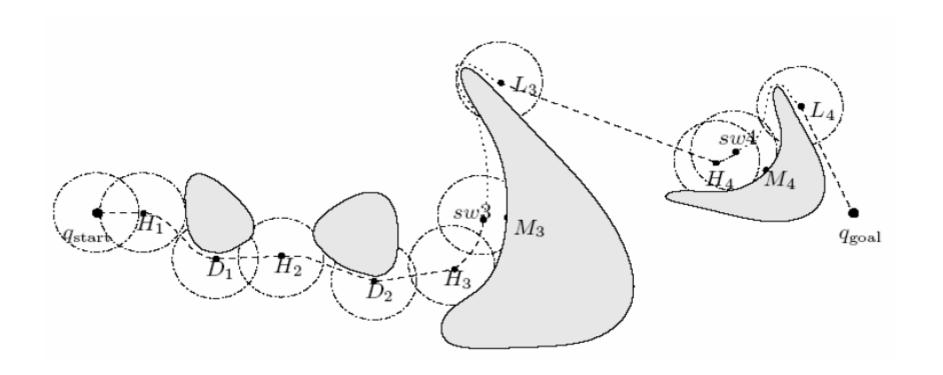
Contact Sensor Tangent Bug



- 1. Robot moves toward goal until it hits obstacle 1 at H1
- 2. Pretend there is an infinitely small sensor range and the direction which minimizes the heuristic is to the right
- 3. Keep following obstacle until robot can go toward obstacle again
- 4. Same situation with second obstacle
- 5. At third obstacle, the robot turned left until it could not increase heuristic
- 6. D_followed is distance between M3 and goal, d_reach is distance between robot and goal because sensing distance is zero



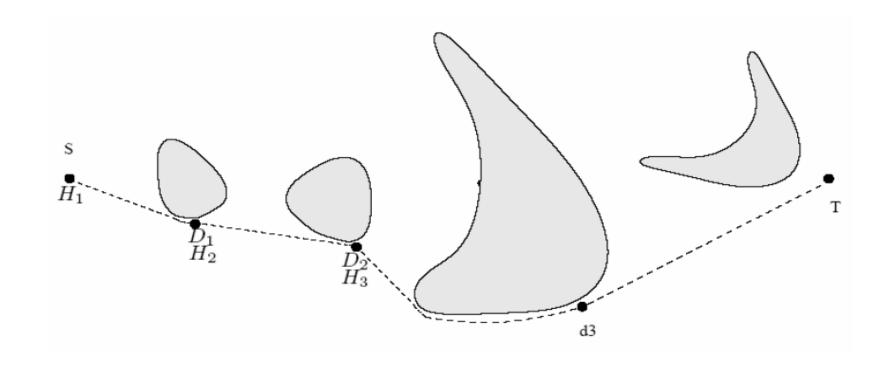
Limited Sensor Range Tangent-Bug







Infinite Sensor Range Tangent Bug

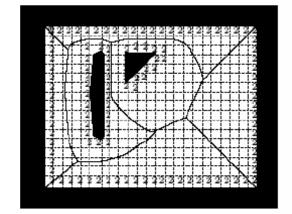


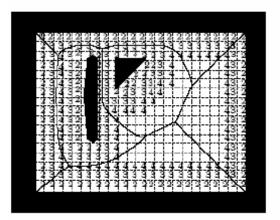


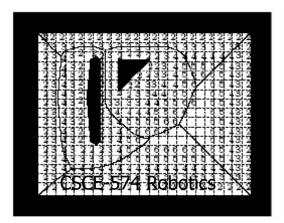


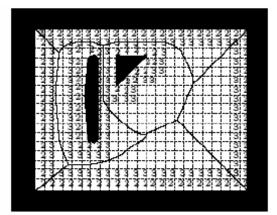
Known Map

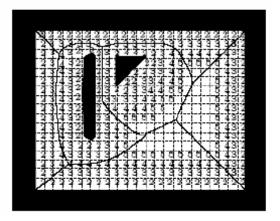
Brushfire Transform

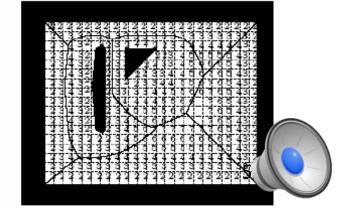






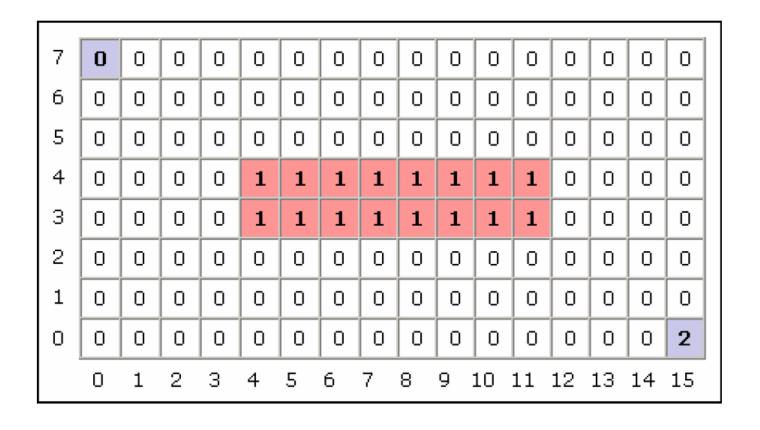








The Wavefront Planner: Setup

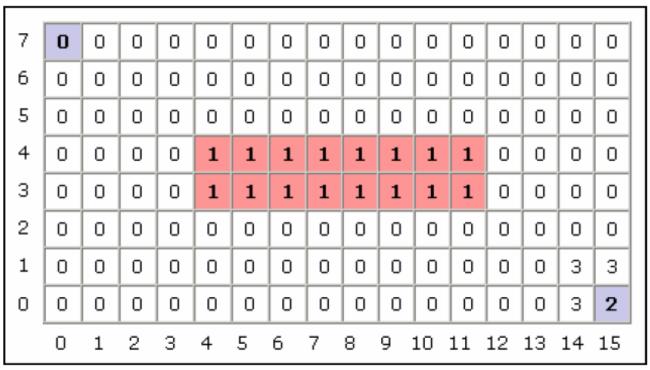






The Wavefront in Action (Part 1)

- Starting with the goal, set all adjacent cells with "0" to the current cell + 1
 - 4-Point Connectivity or 8-Point Connectivity?
 - Your Choice. We'll use 8-Point Connectivity in our example

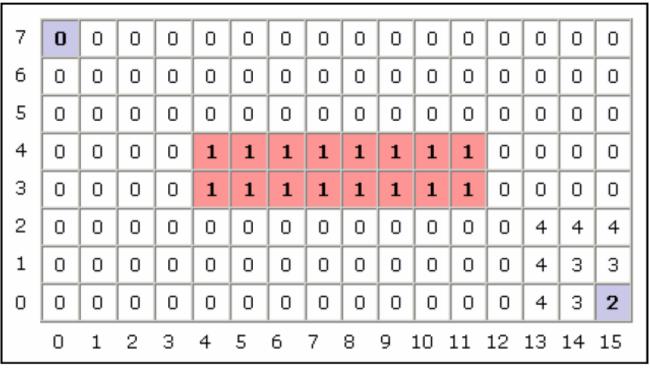






The Wavefront in Action (Part 2)

- Now repeat with the modified cells
 - This will be repeated until no 0's are adjacent to cells with values ≥ 2
- 0's will only remain when regions are unreachable

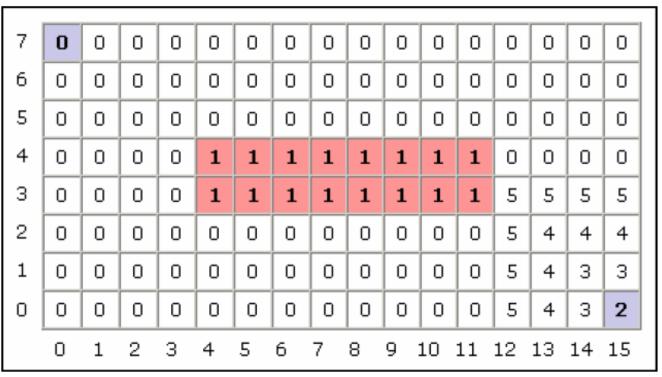




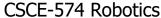


The Wavefront in Action (Part 3)

Repeat

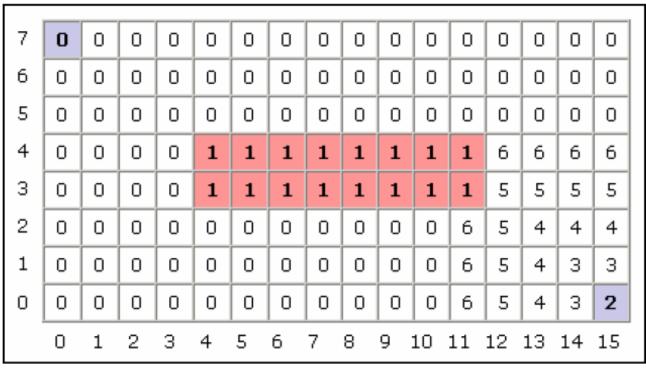






The Wavefront in Action (Part 3)

Repeat





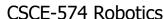
The Wavefront in Action (Part 3)

Until Done

- 0's would only remain in the unreachable areas

															_		
7	18	17	16	15	14	13	12	11	10	9	9	9	9	9	9	9	
6	17	17	16	15	14	13	12	11	10	9	8	8	8	8	8	8	
5	17	16	16	15	14	13	12	11	10	9	8	7	7	7	7	7	
4	17	16	15	15	1	1	1	1	1	1	1	1	6	6	6	6	
3	17	16	15	14	1	1	1	1	1	1	1	1	5	5	5	5	
2	17	16	15	14	13	12	11	10	9	8	7	6	5	4	4	4	
1	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	3	
0	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	
	0	1	2	3	4	5	6	7 (3 9	9 1	0 1	.1 1	12	13	14	15	

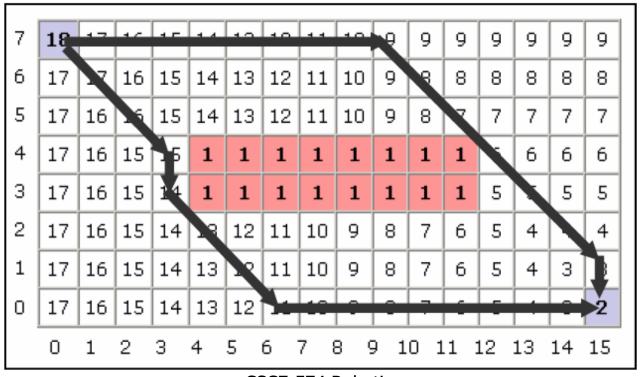






The Wavefront in Action

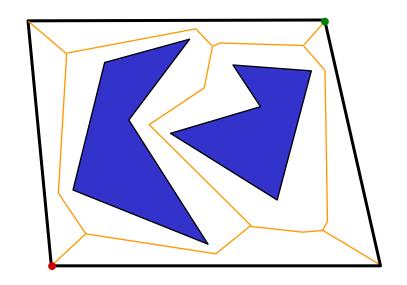
- To find the shortest path, according to your metric, simply always move toward a cell with a lower number
 - The numbers generated by the Wavefront planner are roughly proportional to their distance from the goal





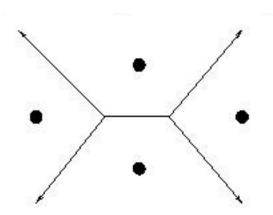


An alternative roadmap







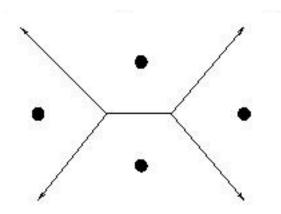


These line segments make up the **Voronoi diagram** for the four points shown here.

Solves the "Post Office Problem"

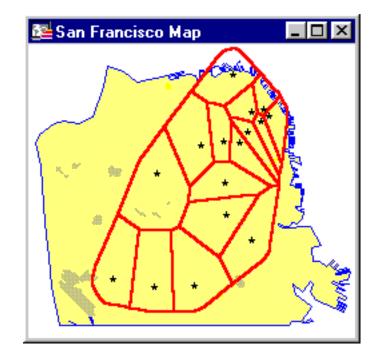






These line segments make up the **Voronoi diagram** for the four points shown here.

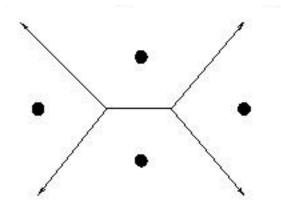
Solves the "Post Office Problem"



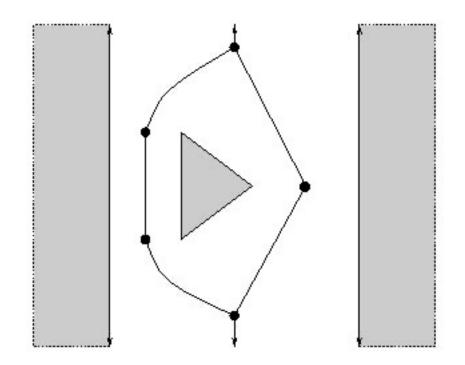
or, perhaps, more important problems...



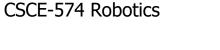




"true" Voronoi diagram (isolates a set of points)



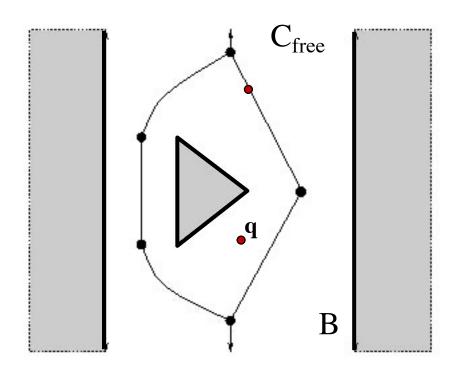
generalized Voronoi diagram What is it?





Let B =the boundary of C_{free} .

Let \mathbf{q} be a point in C_{free} . (•)







Cfree

B

Let B = the boundary of C_{free} .

Let \mathbf{q} be a point in C_{free} .

Define $clearance(q) = min \{ | q - p | \}, for all p \in B$





The contract of the contract o

Let B =the boundary of C_{free} .

Let \mathbf{q} be a point in C_{free} .

Define $clearance(q) = min \{ | q - p | \}, for all p \in B$

Define $near(q) = \{ p \in B \text{ such that } | q - p | = clearance(q) \}$



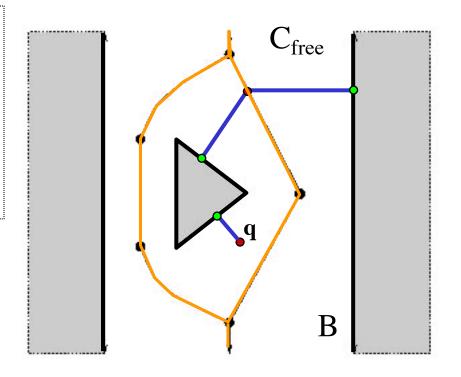


Evaluation

- + maximizes distance from obstacles
- + reduces to graph search
- + can be used in higher-dimensions
- nonoptimal
- real diagrams tend to be noisy

Let B = the boundary of C_{free} .

Let \mathbf{q} be a point in C_{free} .



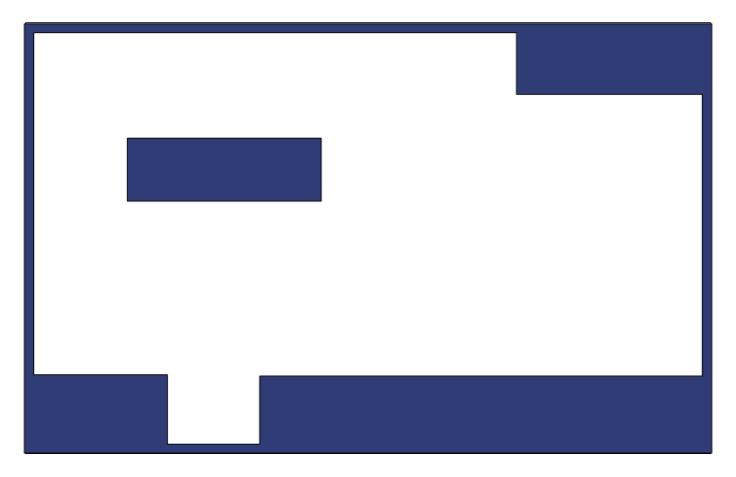
Define *clearance*(q) = min
$$\{ | q - p | \}$$
, for all $p \in B$

Define
$$near(q) = \{ p \in B \text{ such that } | q - p | = clearance(q) \}$$

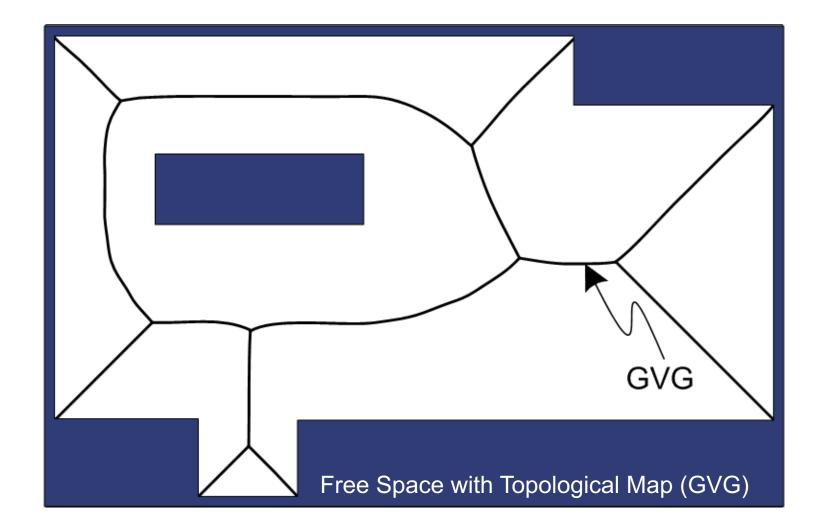
q is in the *Voronoi diagram* of C_{free} if |near(q)| > 1

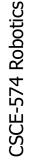


number of set elements





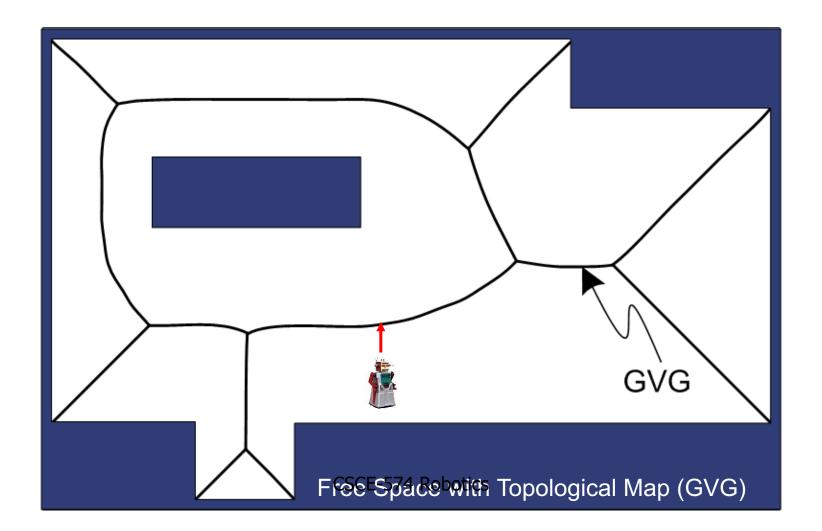








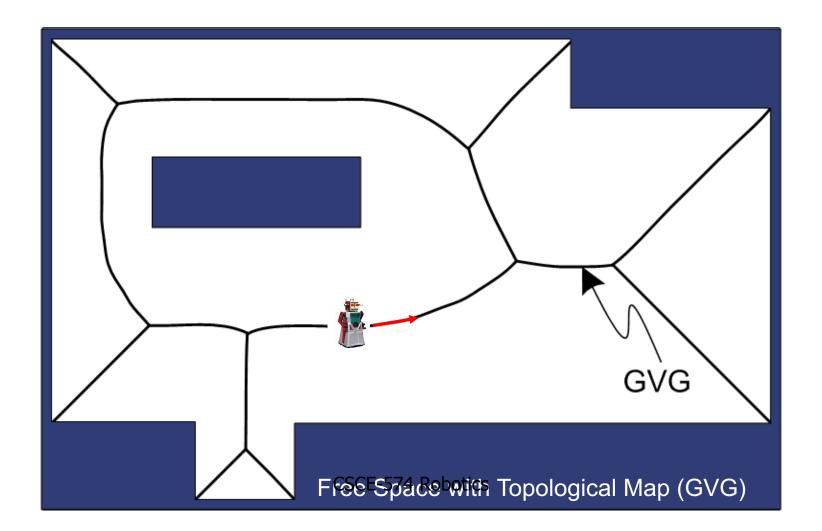
Access GVG







- Access GVG
- •Follow Edge

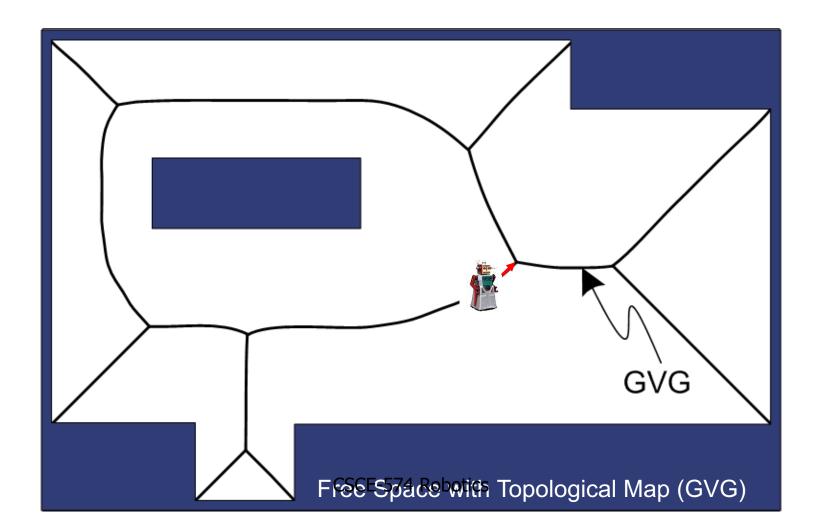






Generalized Voronoi Graph (GVG)

- •Access GVG •Home to the MeetPoint
- •Follow Edge

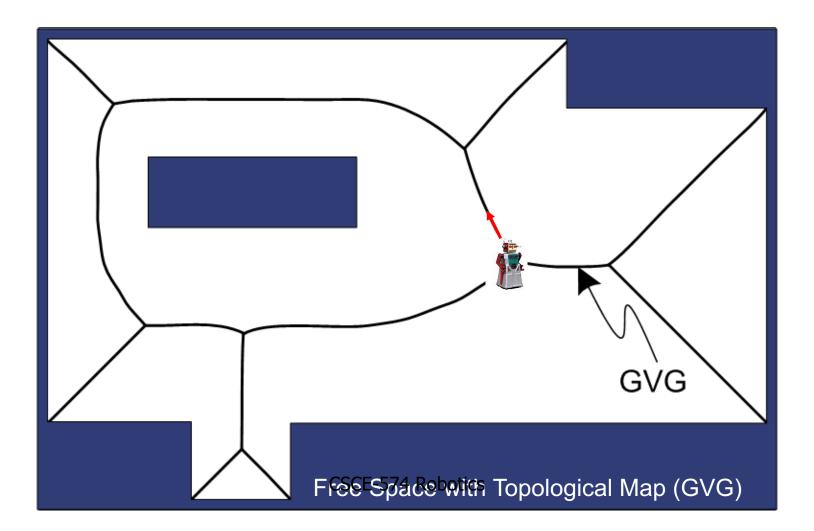






Generalized Voronoi Graph (GVG)

- •Access GVG •Home to the MeetPoint
- •Follow Edge •Select Edge







GVG construction using sonar

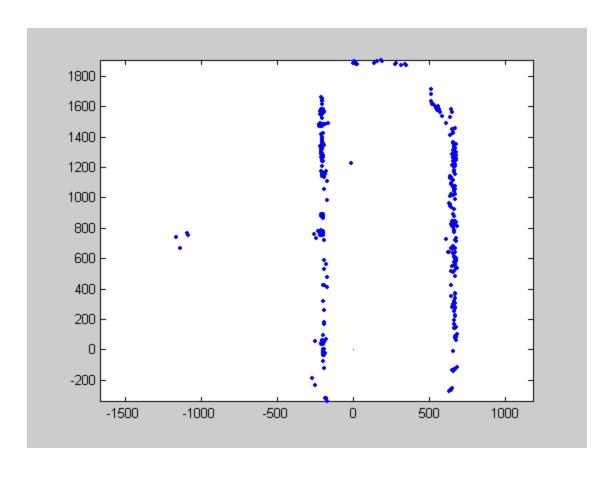


- Nomadic Scout
- Sonar (GVG navigation)
- Camera with omni-directional mirror (feature detection)
- Onboard 1.2 GHz processor



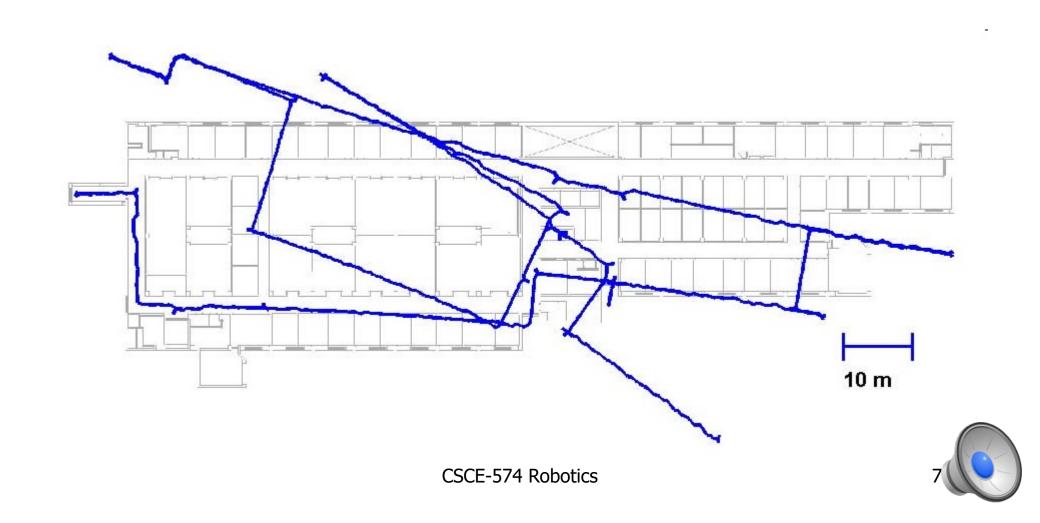


GVG construction using sonar

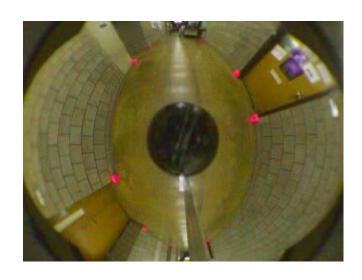




GVG construction using sonar



Slammer in Action

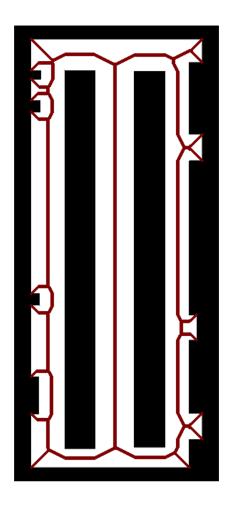


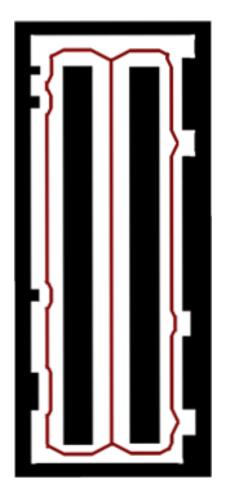






Removing Edges







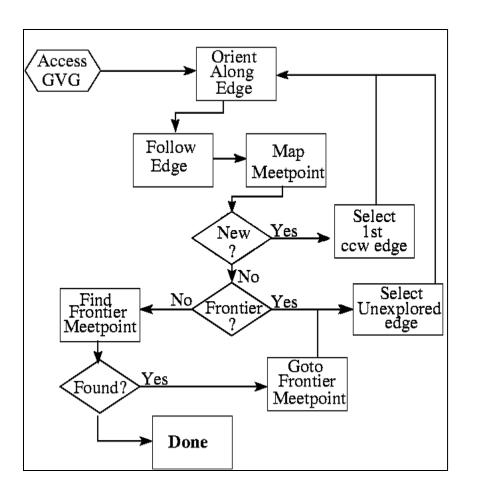


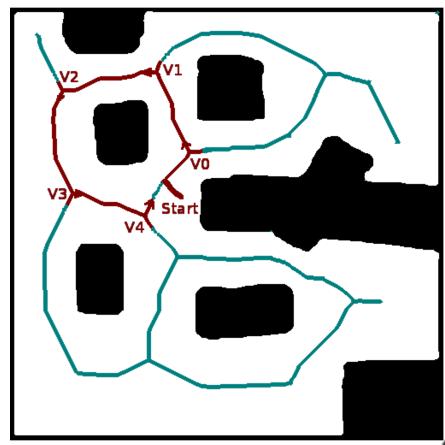
Meetpoint Detection

- 3σ uncertainty ellipse of explored meetpoints
- Meetpoint degree (branching factor)
- Distances to local obstacles
- Relative angle bearings
- Edge signature
 - Edge length
 - Edge Curvature
- Vertex signal



Ear-based Exploration

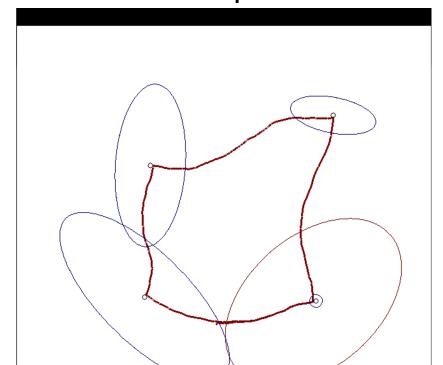




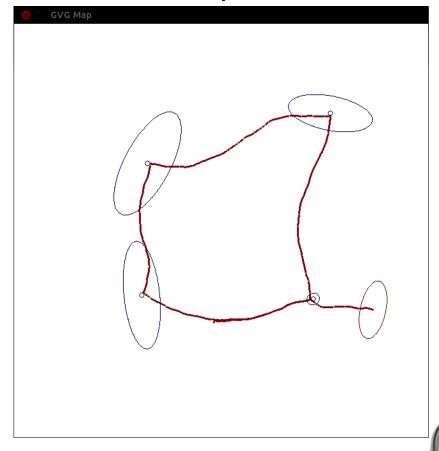


Uncertainty Reduction

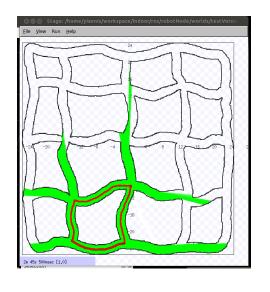
Before Loop-closure

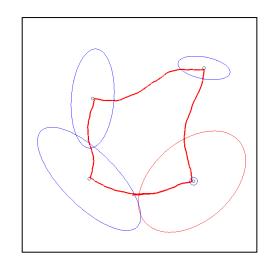


After Loop-closure

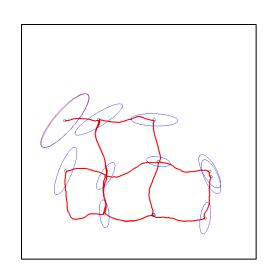


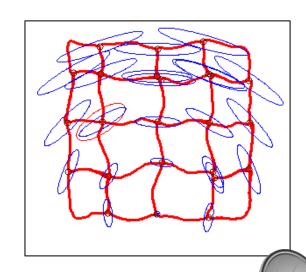






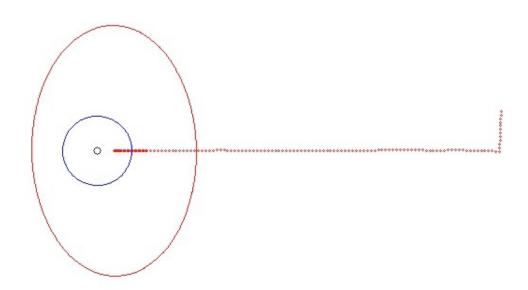
Simulation







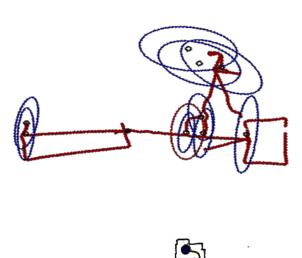
Simulated Environment

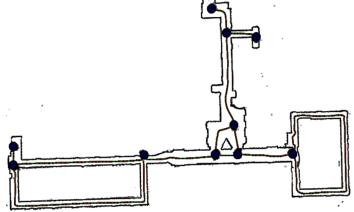


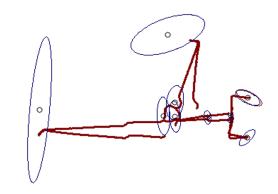


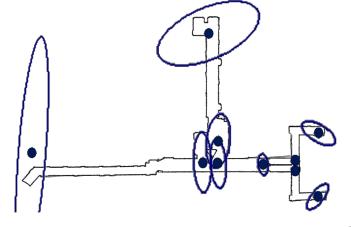


Real Environment











Work Presented at IROS 2014

Ear-based Exploration on Hybrid Metric/Topological Maps

Q. Zhang, D. Whitney, F. Shkurti, and I. Rekleitis School of Computer Science, McGill University

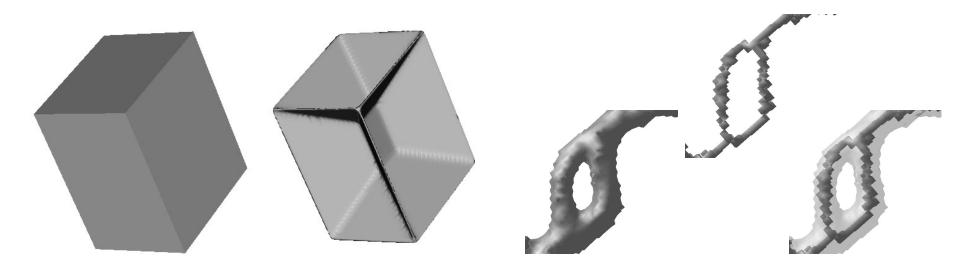








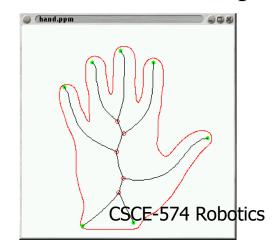
Voronoi applications



A retraction of a 3d object == "medial surface"

Skeletonizations resulting from constant-speed curve evolution



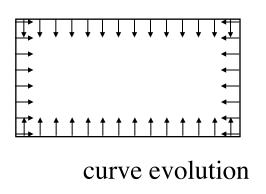


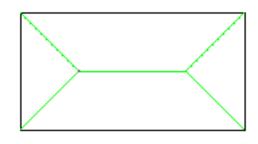


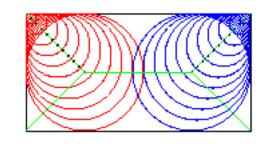
in 2d, it's call a medial ax



skeleton → shape







where wavefronts collide

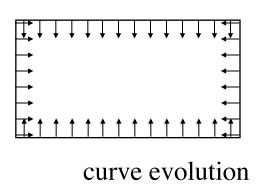
centers of maximal disks

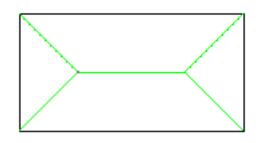
again reduces a 2d (or higher) problem to a question about graphs...

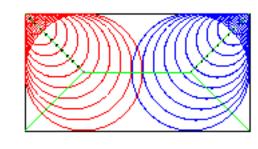




skeleton → shape





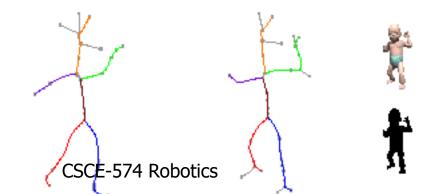


where wavefronts collide

centers of maximal disks

again reduces a 2d (or higher) problem to a question about graphs...

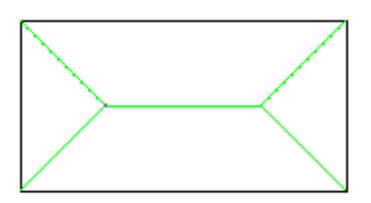


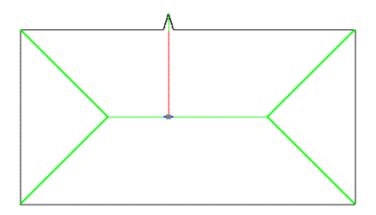






Problems





The skeleton is sensitive to small changes in the object's boundary.





Roadmap problems

If an obstacle decides to roll away... (or wasn't there to begin with)

