



UNIVERSITY OF  
**SOUTH CAROLINA**

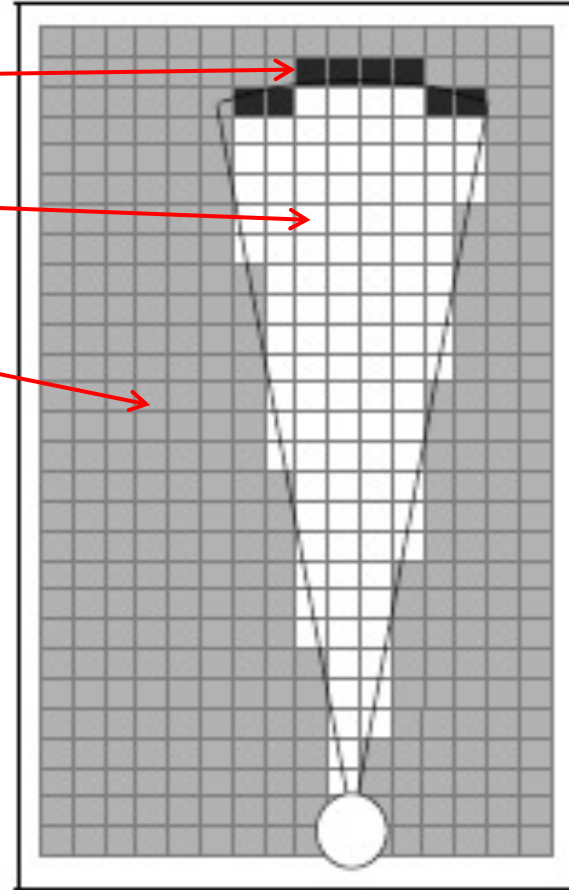
# CSCE 574 ROBOTICS

## Exploration

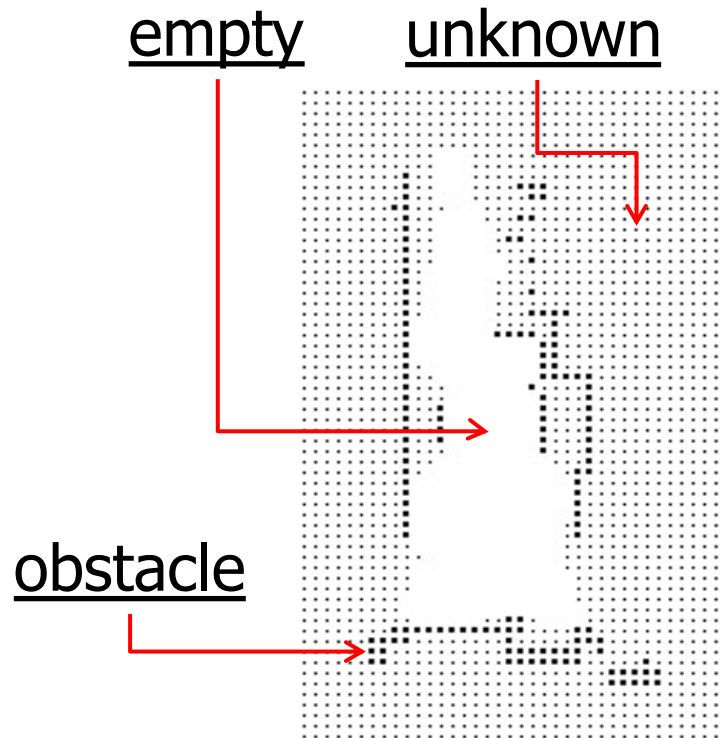


# Grid Based Maps

- Occupied cells
- Free cells
- Unknown cells



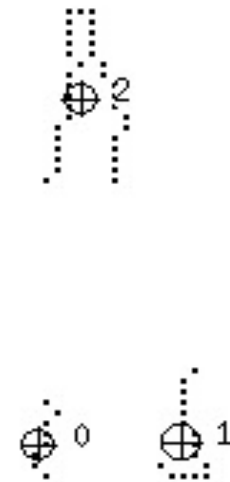
# Frontier based Exploration (Grid Maps)



Frontier Cells

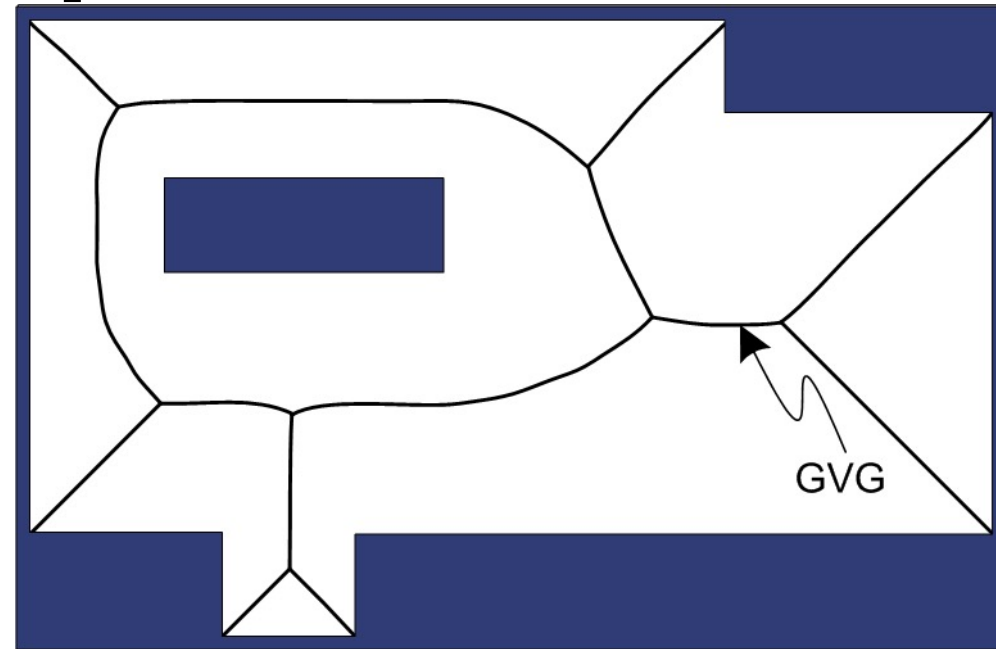
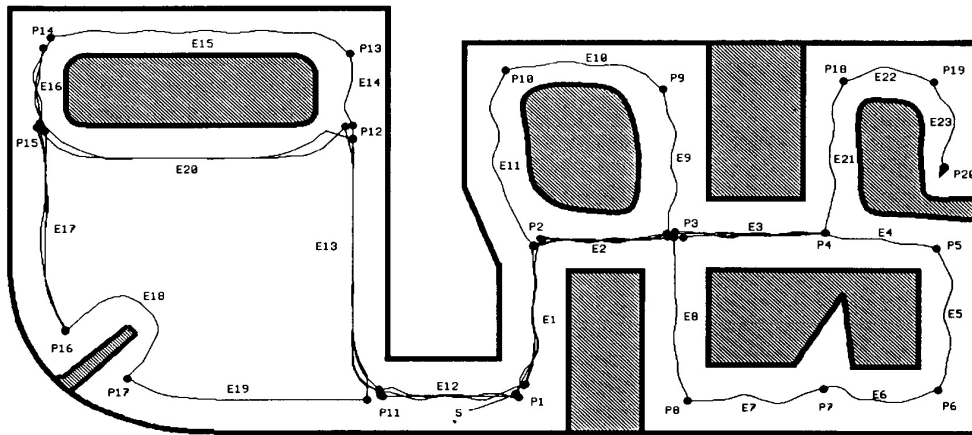


Frontier Targets



# Topological Representations

- Apply on a topological map



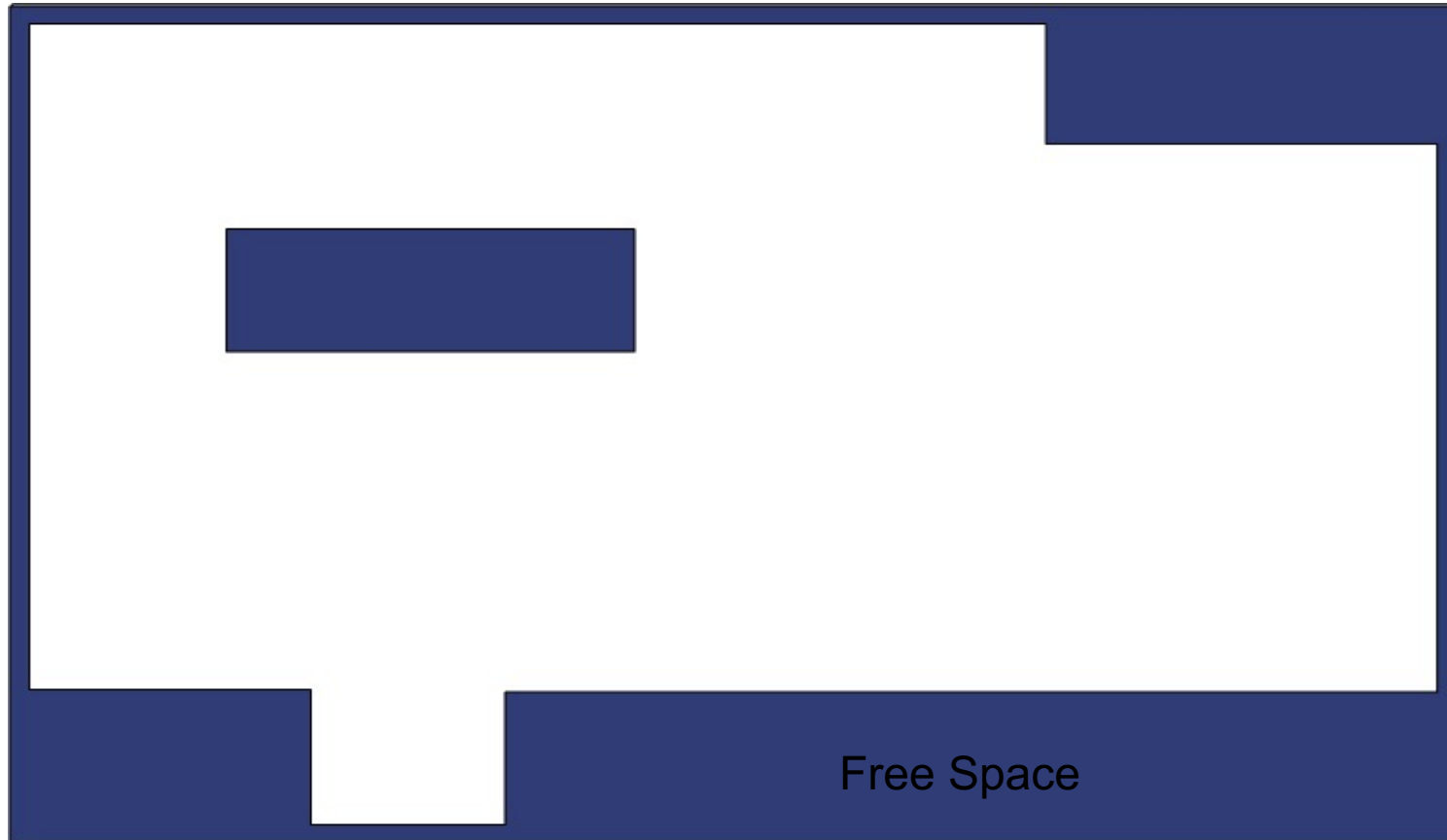
- B. J. Kuipers and Y.-T. Byun. “A robot exploration and mapping strategy based on a semantic hierarchy of spatial representations”. In *Journal of Robotics and Autonomous Systems*, 8: 47-63, 1991.

H. Choset, J. Burdick, “Sensor based planning, part ii: Incremental construction of the generalized Voronoi graph”. In *IEEE Conference on Robotics and Automation*, pp. 1643 – 1648, 1995.



# Generalized Voronoi Graph (GVG)

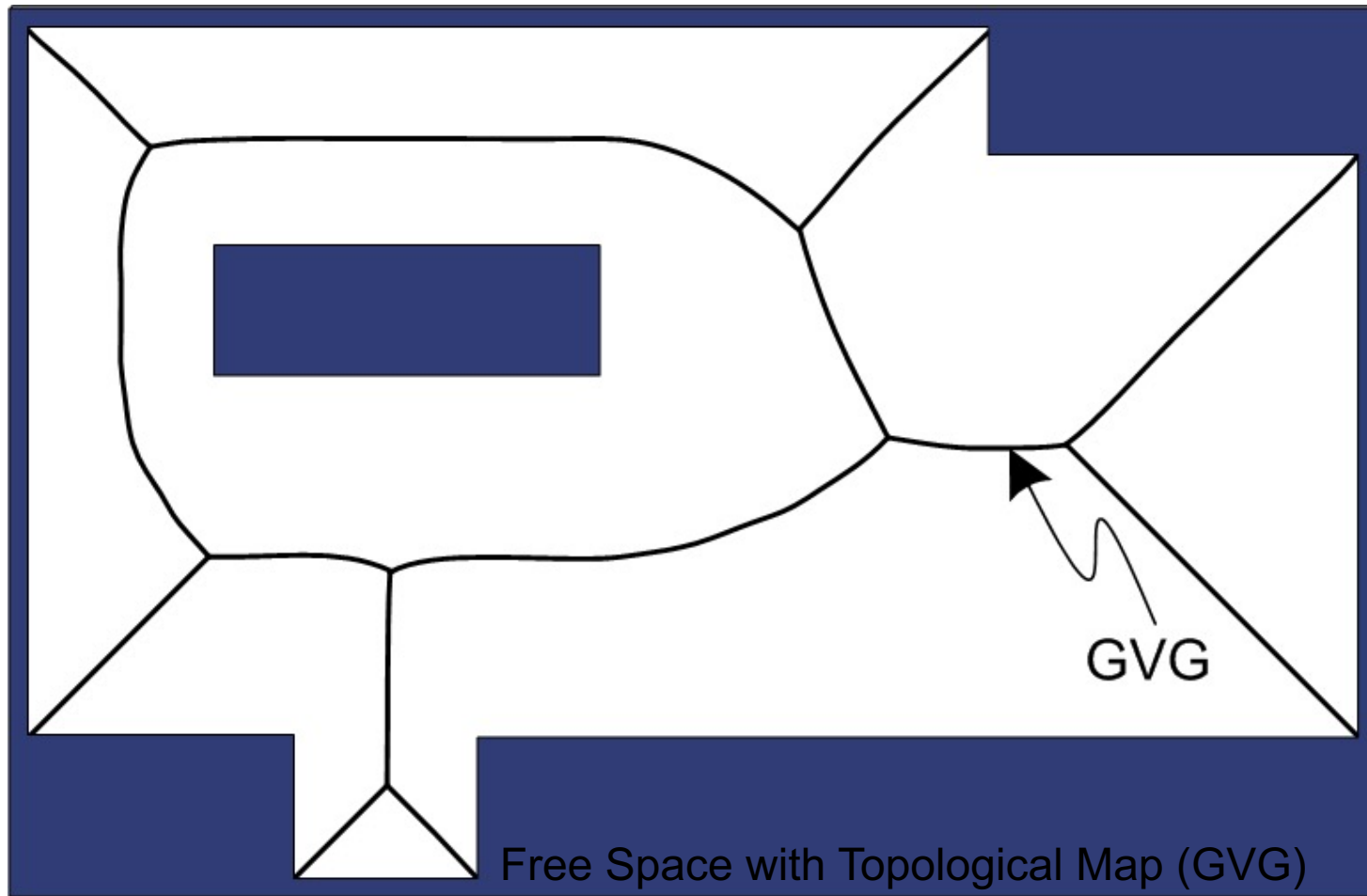
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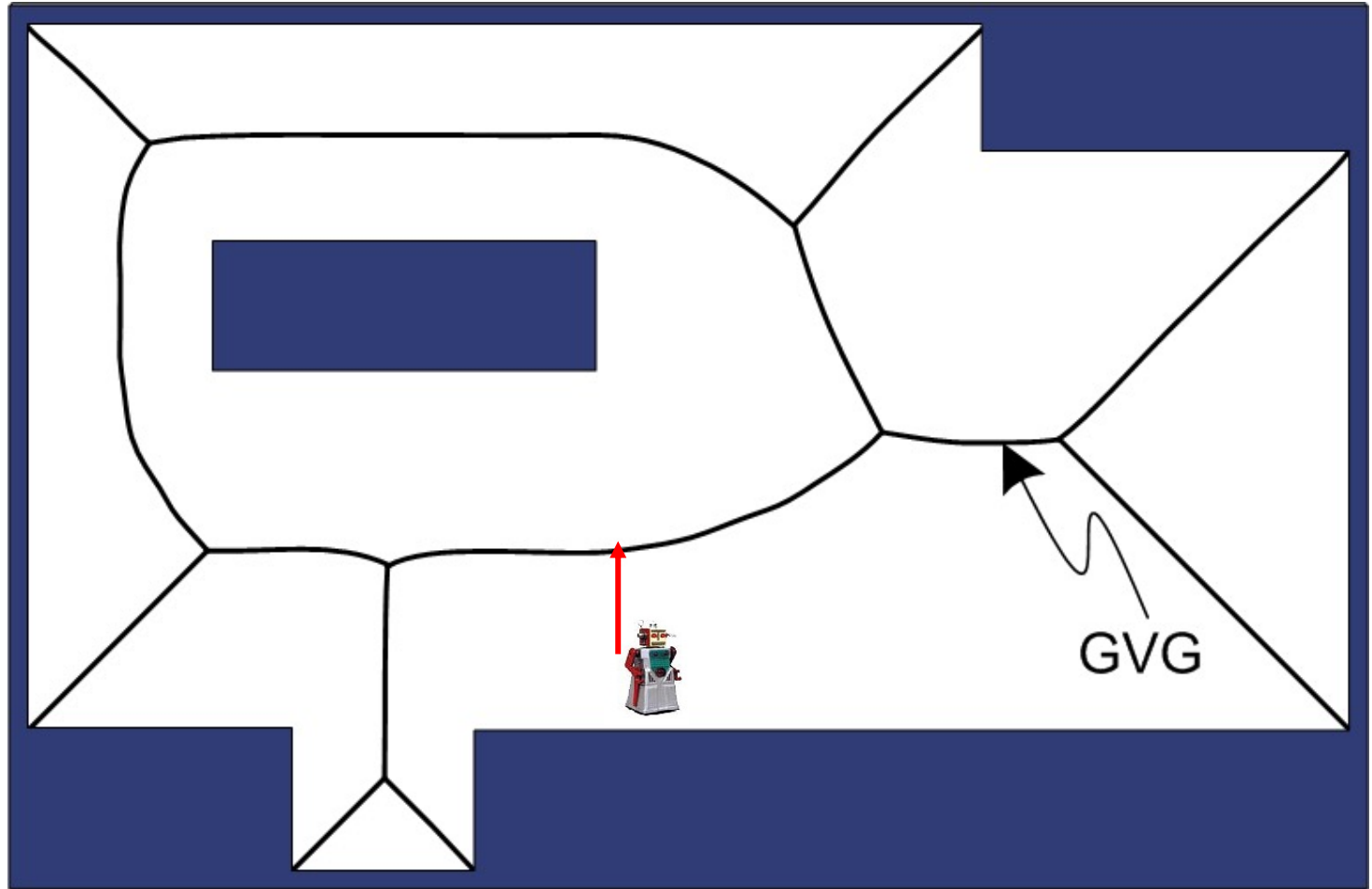


# Generalized Voronoi Graph (GVG)



# Generalized Voronoi Graph (GVG)

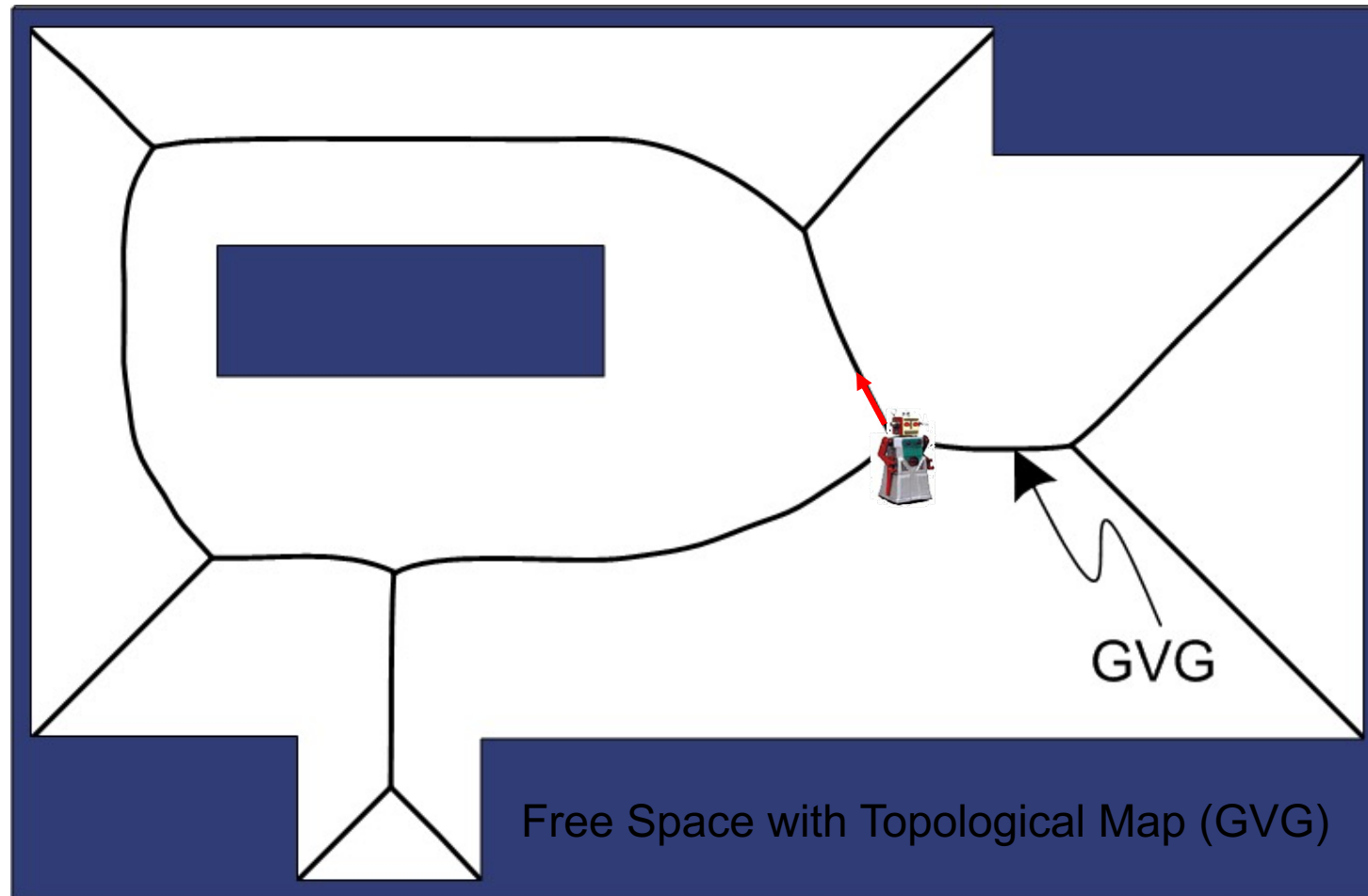
- Access GVG



Free Space with Topological Map (GVG)

# Generalized Voronoi Graph (GVG)

- Access GVG
- Follow Edge
- Home to the MeetPoint
- Select Edge

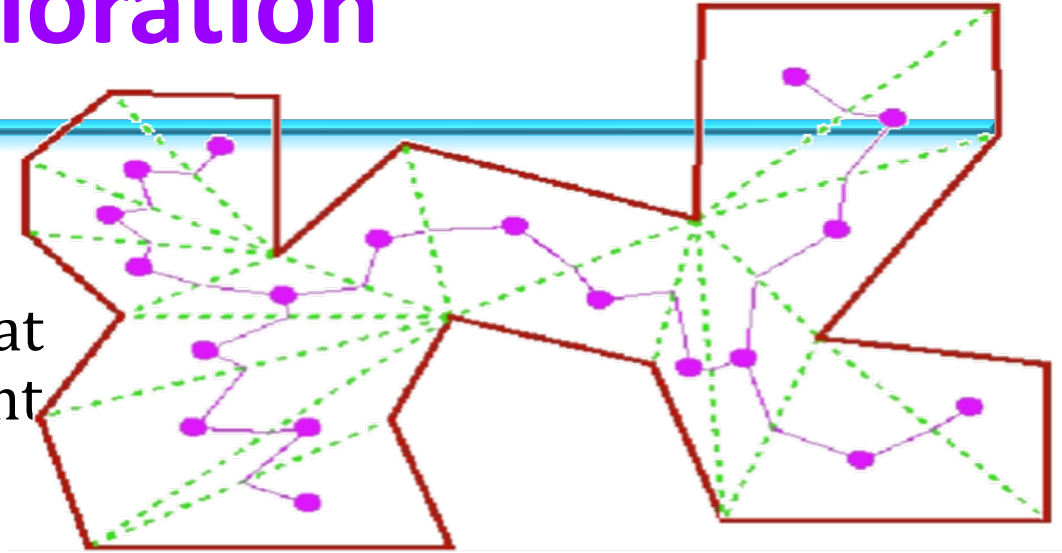






# Cooperative Exploration

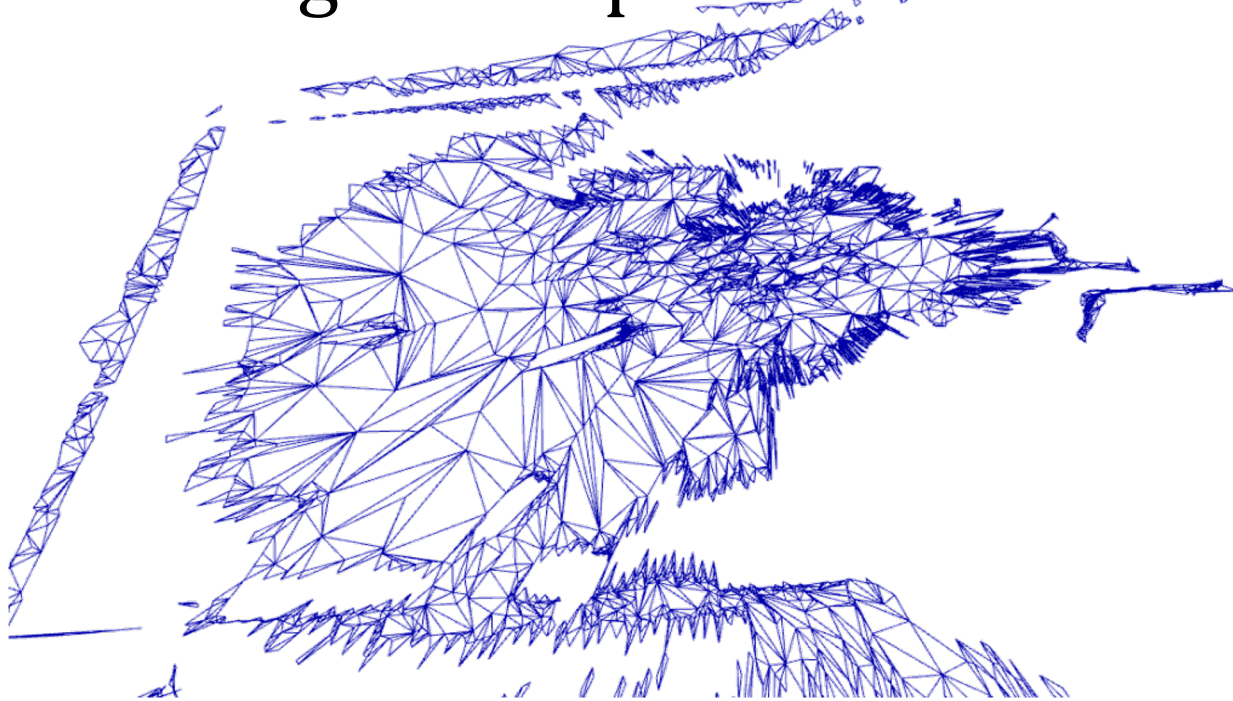
- **Robot Position:**
  - Stationary Robot: Positioned at the corners of the environment
  - Moving Robot: Follows the walls.
- **Exploration order:**
  - The two robots explore the free space by following the Dual Graph of the Triangulation.
- **Decision points:**
  - Reflex vertices.



# Irregular Triangular Mesh (ITM)

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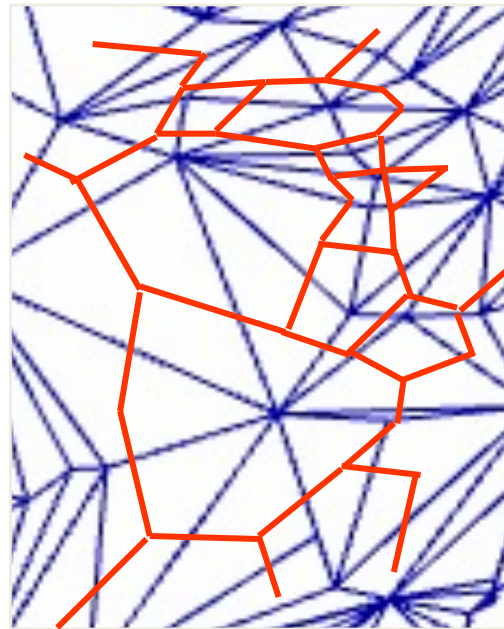
- Terrain Representation
- Underlying Topological Structure
- Path Planning and Exploration



# From 2.5D Representation to Topological

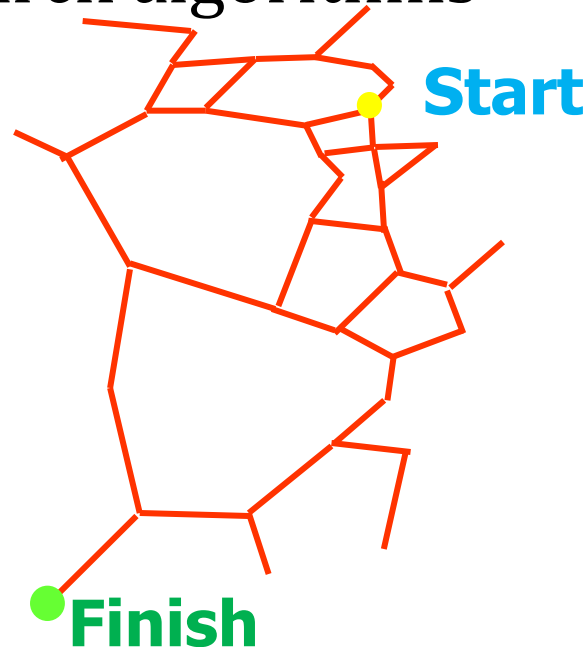
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- Convert ITM into Connected Graph



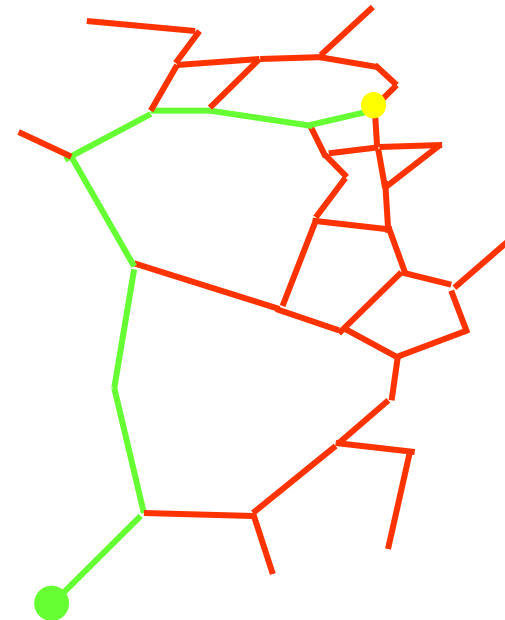
# Planning

- Convert ITM into Connected Graph
- Planning using Graph Search Algorithms:
  - Dijkstra, A\* search algorithms



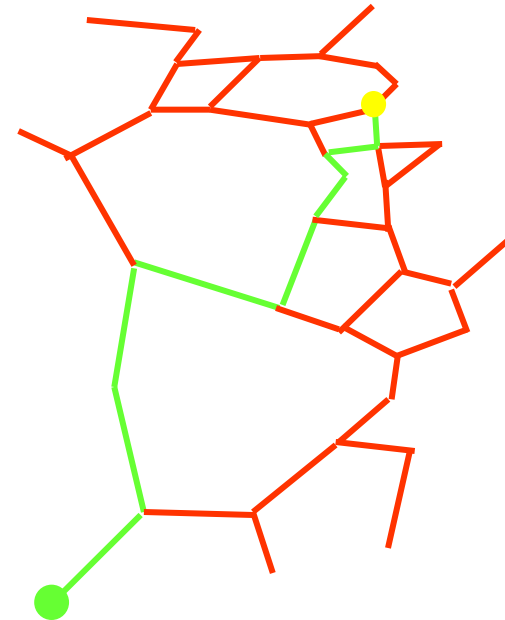
# Planning

- Convert ITM into Connected Graph
- Path Planning using Graph Search Algorithms:
  - Dijkstra, A\* search algorithms
- Different Cost Functions  $Q$ 
  - Number of triangles  $Q = 1$



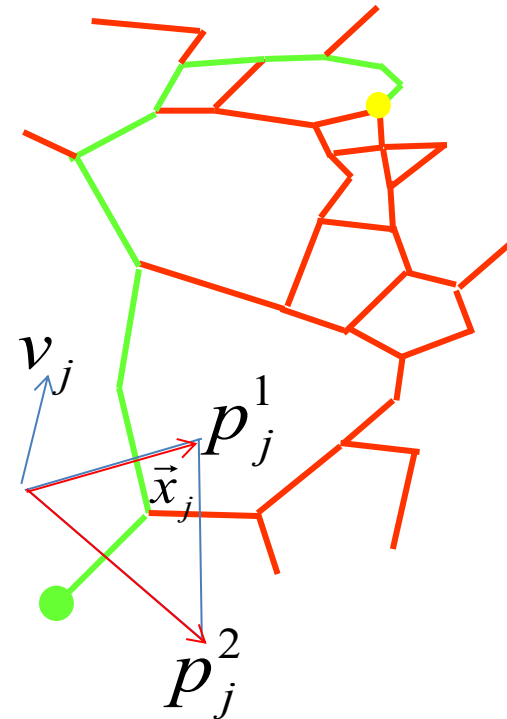
# Planning

- Convert ITM into Connected Graph
- Path Planning using Graph Search Algorithms:
  - Dijkstra, A\*
- Different Cost Functions  $Q$ 
  - Number of triangles
  - Euclidian distance  $Q = \|\vec{x}_i - \vec{x}_j\|$



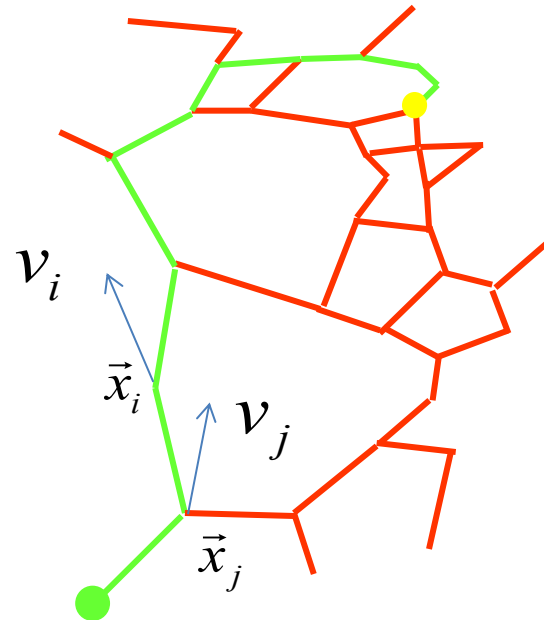
# Planning

- Convert ITM into Connected Graph
- Path Planning using Graph Search Algorithms:
  - Dijkstra, A\*
- Different Cost Functions  $Q$ 
  - Number of triangles
  - Euclidian distance
  - Slope of each triangle  $v_j = \frac{p_j^1 \times p_j^2}{\|p_j^1\| \|p_j^2\|}$



# Planning

- Convert ITM into Connected Graph
- Path Planning using Graph Search Algorithms:
  - Dijkstra, A\*
- Different Cost Functions  $Q$ 
  - Number of triangles
  - Euclidian distance
  - Slope of each triangle
  - Cross triangle slope





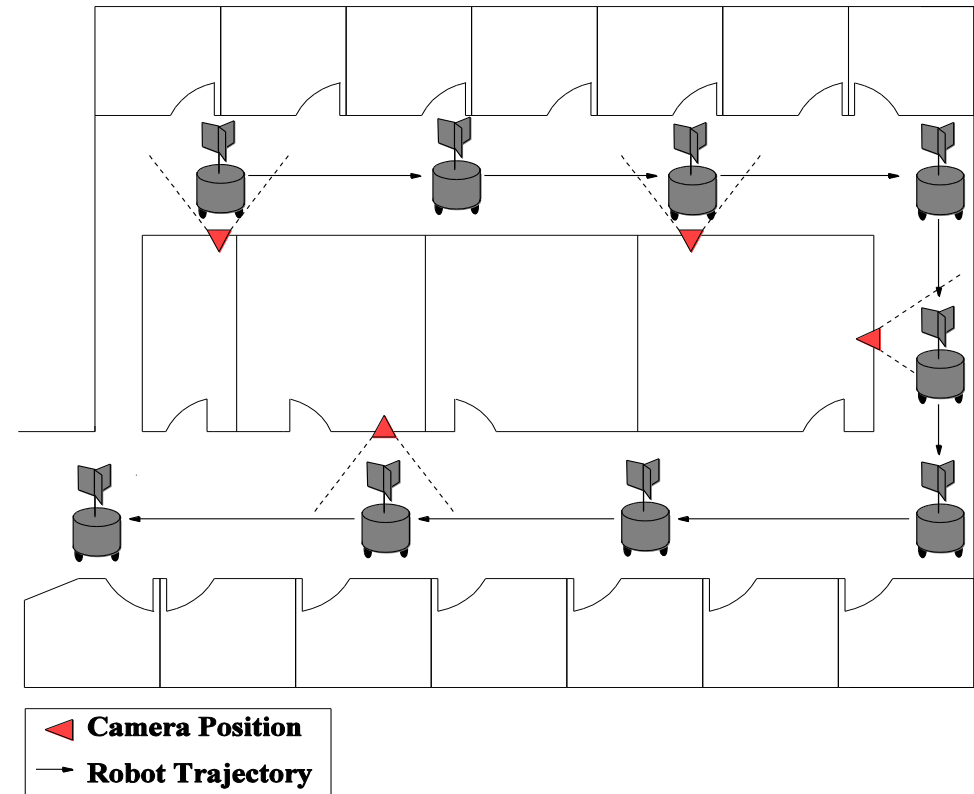
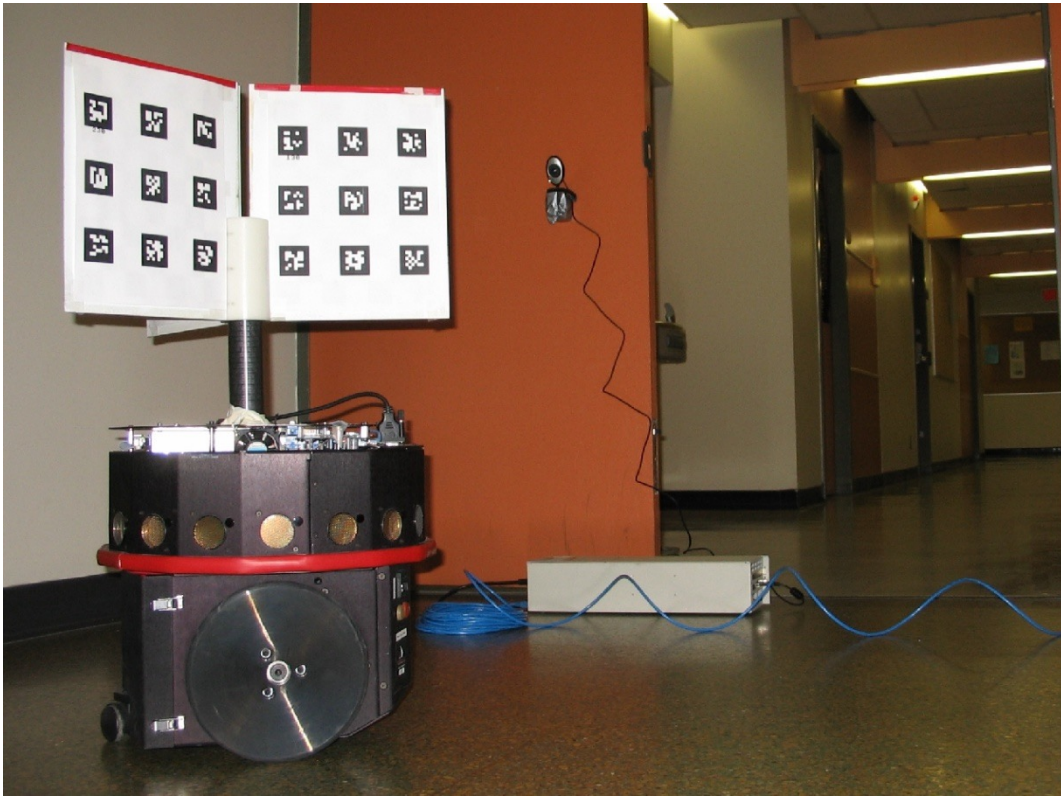
# Exploration via Graph Search

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- Exhaustive Depth First Search
- Breadth-First Search
- Heuristics



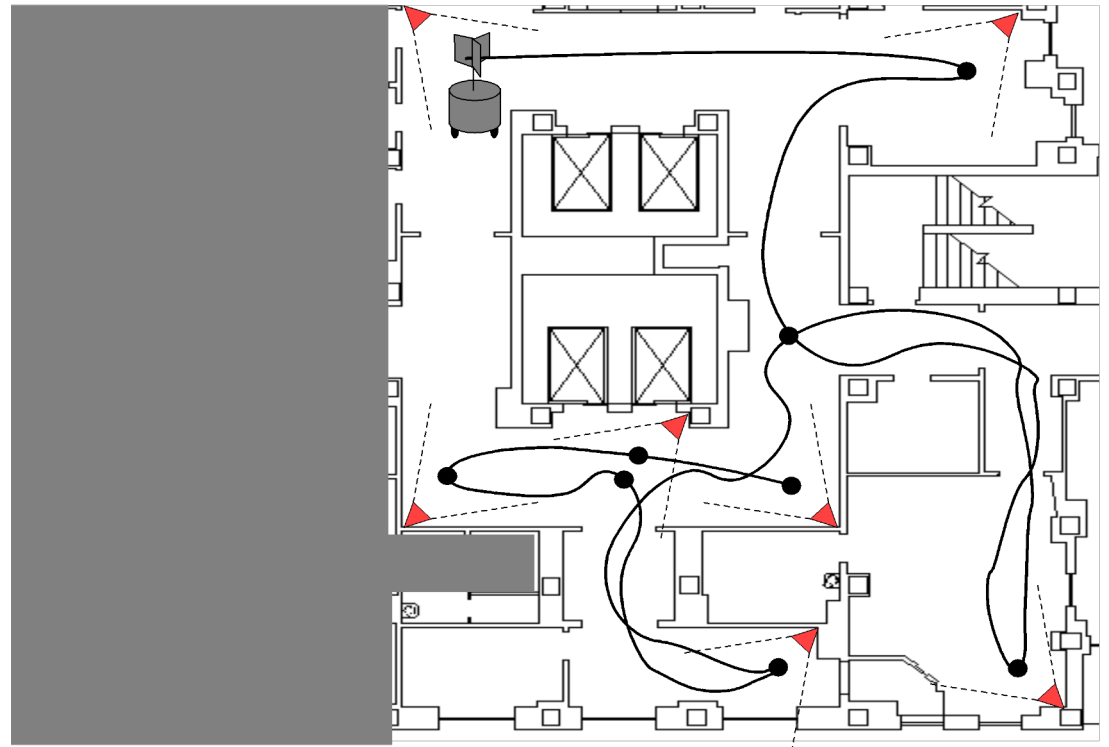
# Exploring a Camera Sensor Network



D. Meger, I. Rekleitis, and G. Dudek. "Heuristic Search Planning to Reduce Exploration Uncertainty", IROS 2008.

# Exploration Planning Problem

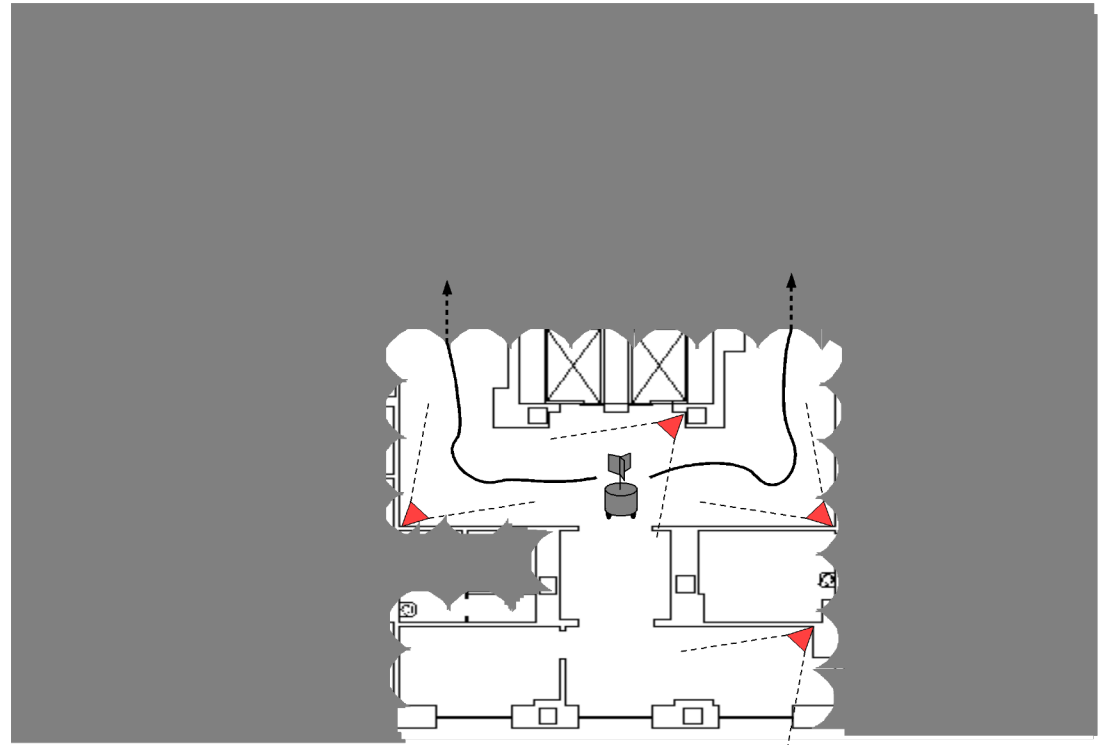
Two fundamental problems for path planning during exploration and mapping:



# Exploration Planning Problem

Two fundamental problems for path planning during exploration and mapping:

- Planning for re-localization
- Planning the exploration of new territory



# Heuristic Search Planning Method

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- Solution to exploration planning for camera sensor networks
  - Composed of two alternated steps: exploration and re-localization
  - Combined distance and uncertainty cost function
  - Heuristic search for good paths



# Exploration and Uncertainty Reduction

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- Decision (exploration vs exploitation)
- Target Node
- Path Planning through the known graph
- Exploration Strategies



# Exploration and Uncertainty Reduction

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- Decision (exploration vs. exploitation)
  - **Epsilon-Greedy**
  - **Epsilon-First**
  - **Adaptive**
  - **Bounded Uncertainty**
- Target Node
- Path Planning through the known graph
- Exploration Strategies



# Exploration and Uncertainty Reduction

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- Decision (exploration vs. exploitation)
- Target Node (Exploration)
  - **Random**
  - **Shortest distance**
  - **Maximum Uncertainty**
  - **Minimum Uncertainty**
- Path Planning through the known graph
- Exploration Strategies





# Exploration and Uncertainty Reduction

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- Decision (exploration vs. exploitation)
- Target Node (Relocalization)
  - **Maximum Uncertainty**
- Path Planning through the known graph
- Exploration Strategies



# Exploration and Uncertainty Reduction

- Decision (exploration vs. exploitation)
- Target Node
- Path Planning through the known graph
  - Work with D. Meger and G. Dudek [IROS 2008]
  - A\* based strategy
  - Cost:  $C(p) = \omega_d \text{length}(p) + \omega_u \text{trace}(P(p))$
  - Distance-based “cost-to-go” heuristic function  $h$  used to compute estimated cost

$$C(n) = f(n) + h(n)$$

Estimated cost through n

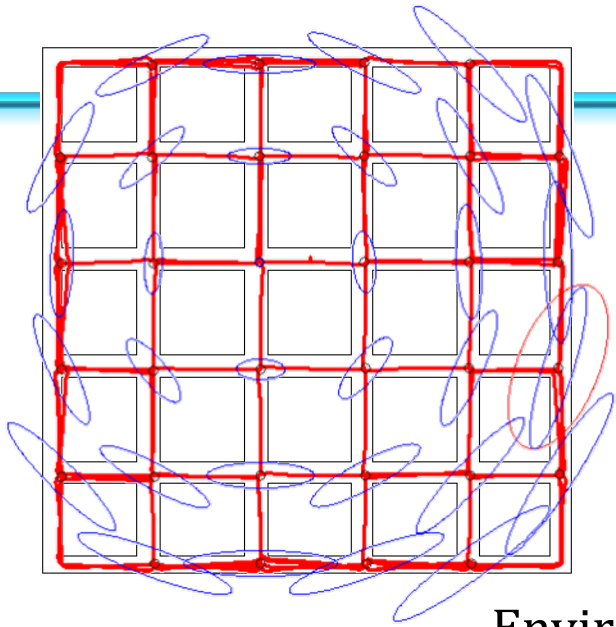
Cost so far

Estimated cost to go

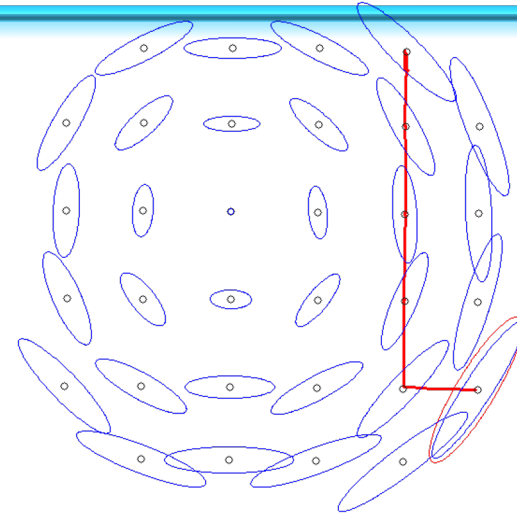
- Exploration Strategies



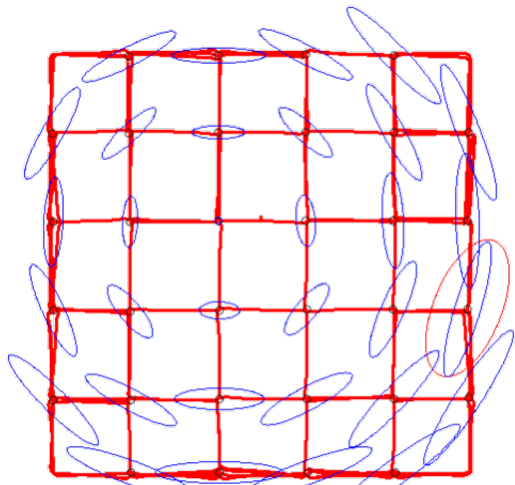
# Effect of $\alpha$ Parameter for Relocalization



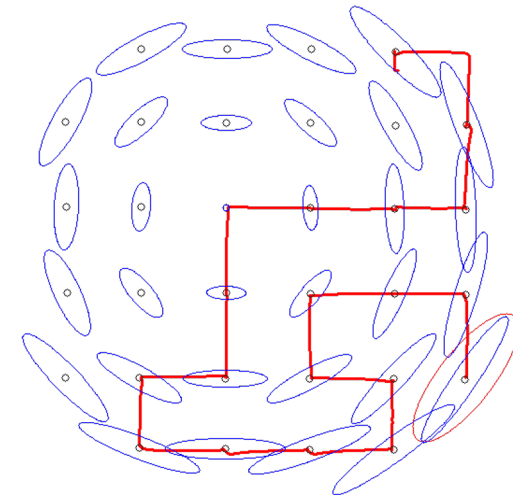
Environment with map



Shortest Path ( $\alpha=1$ )

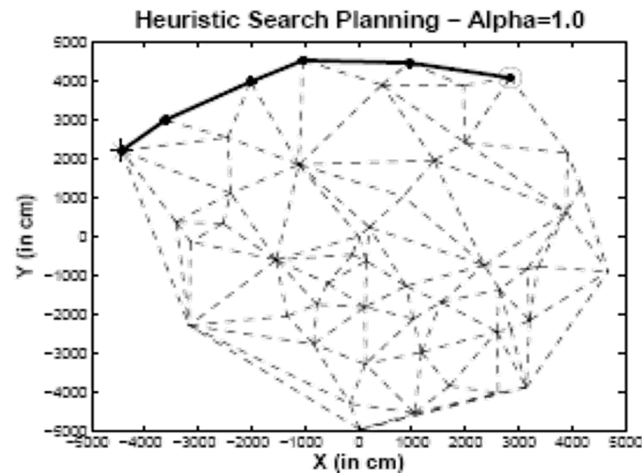


Initial map

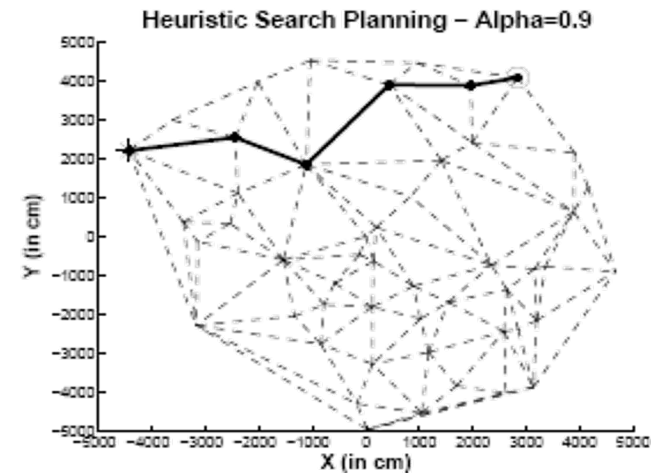


Lower Uncertainty ( $\alpha=0$ )

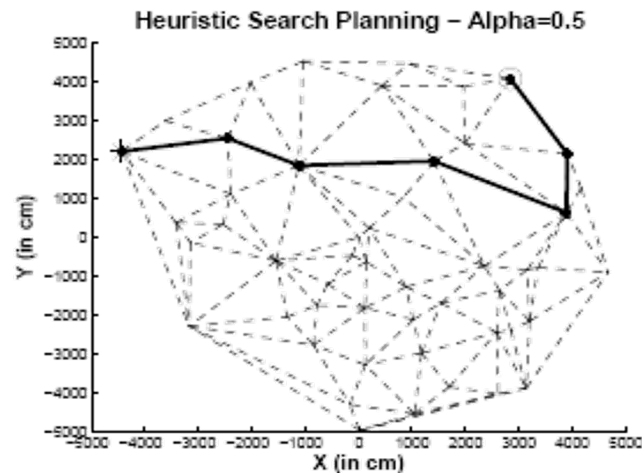
# Effect of $\alpha$ Parameter for Relocalization



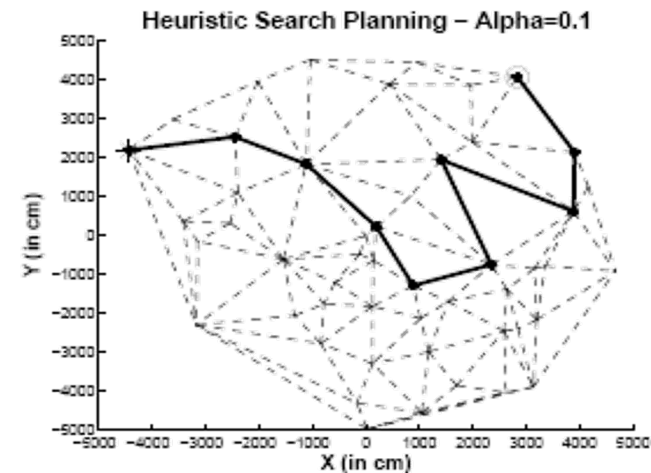
(a)



(b)



(c)



(d)



# Exploration and Uncertainty Reduction

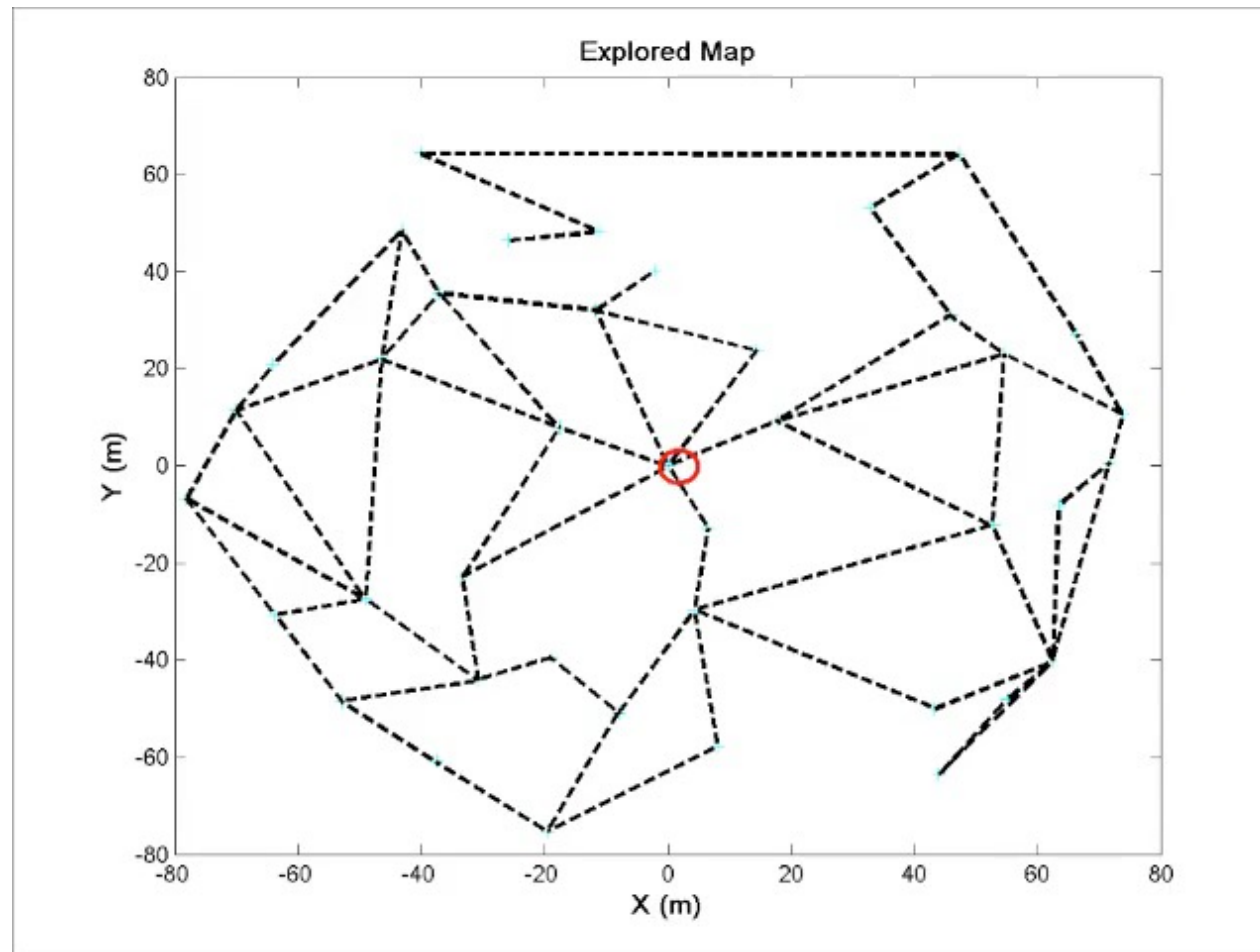
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- Decision (exploration vs. exploitation)
- Target Node
- Path Planning through the known graph
- **Exploration Strategies**
  - One Step Exploration
  - Ear based exploration



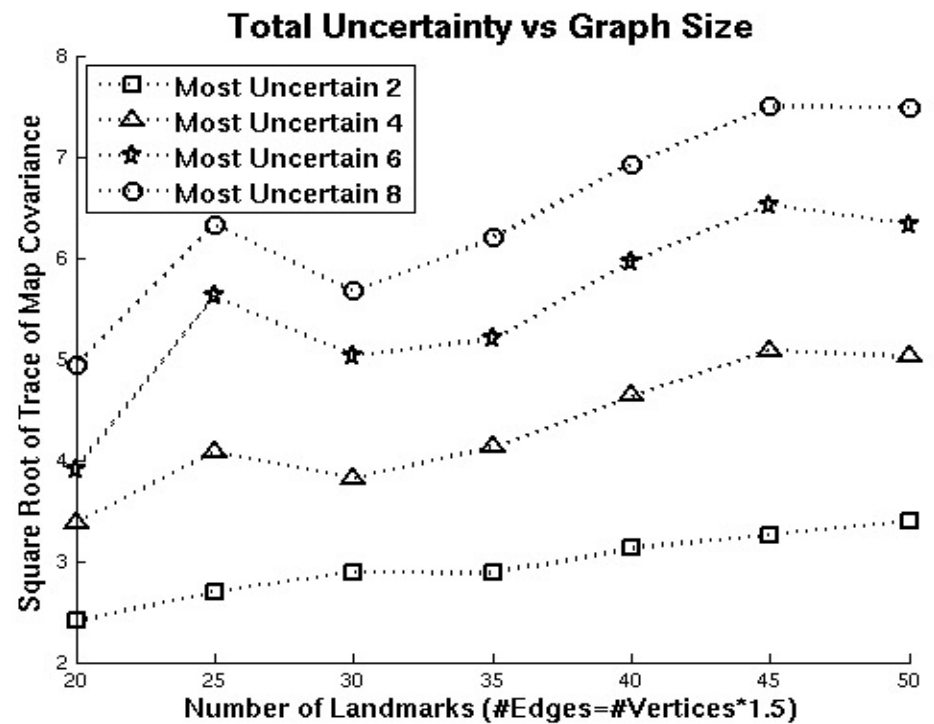
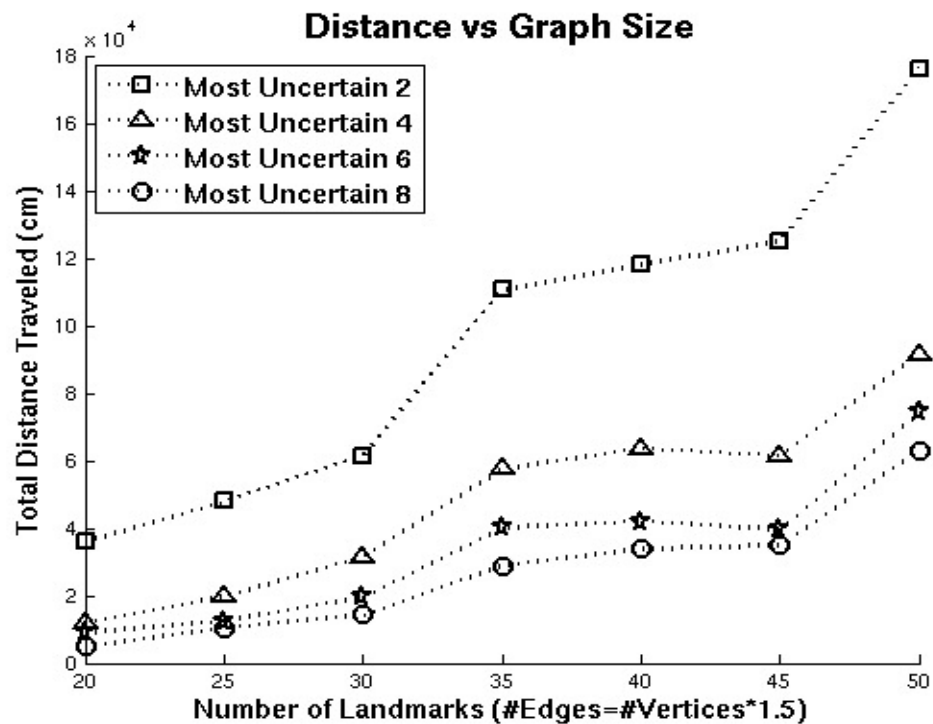
# Shortest Node

## $P(\text{exploit})=0.3$



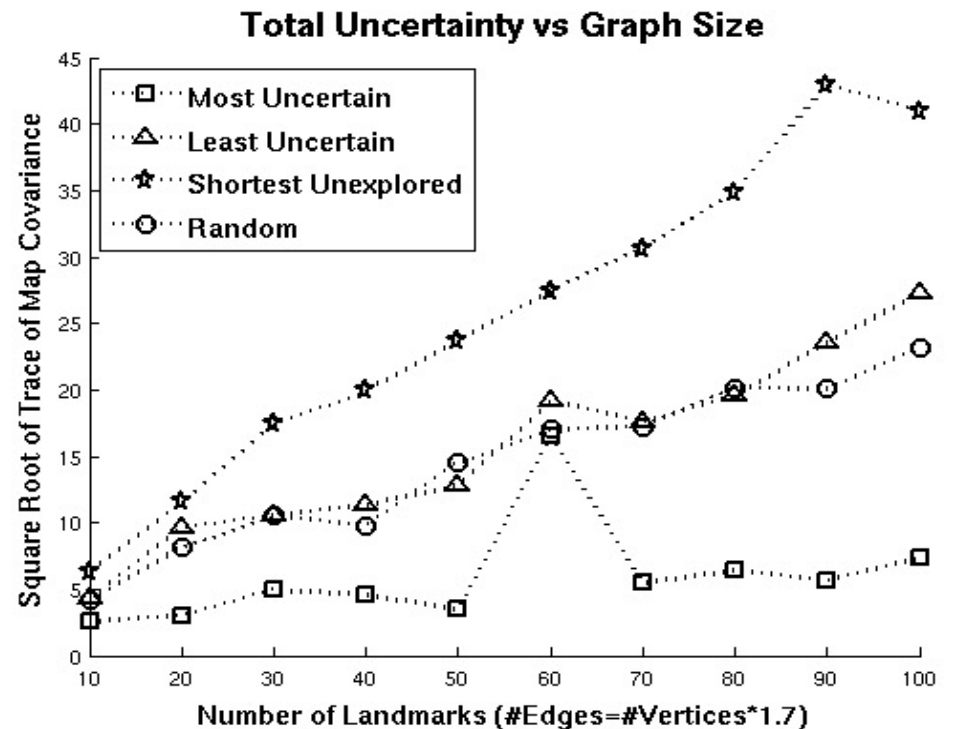
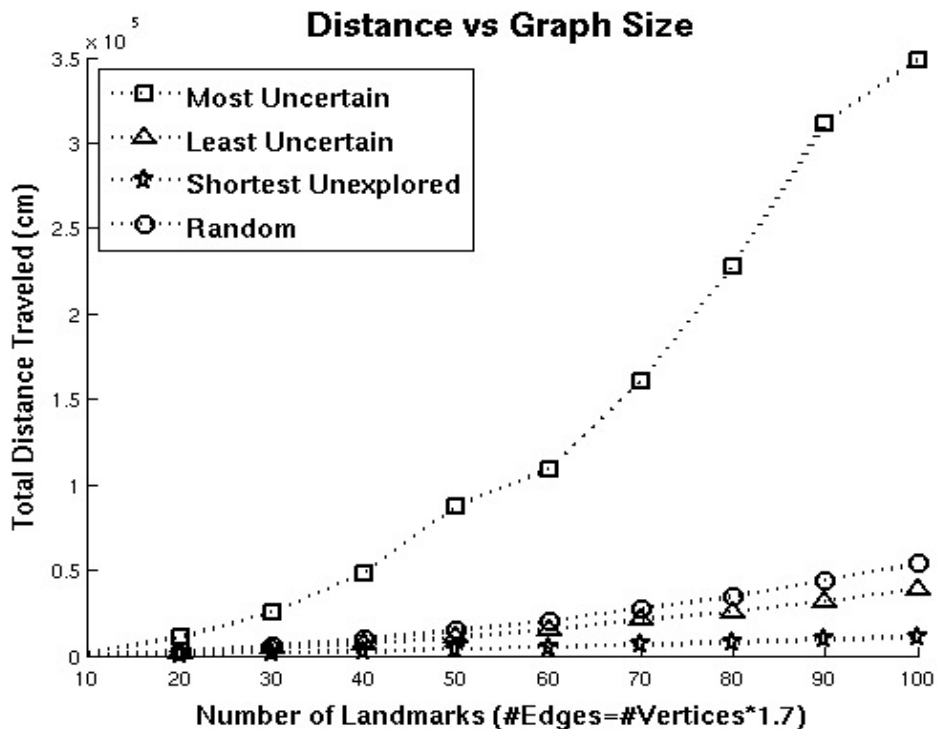
# Experimental Results

## Bounded Uncertainty



# Experimental Results

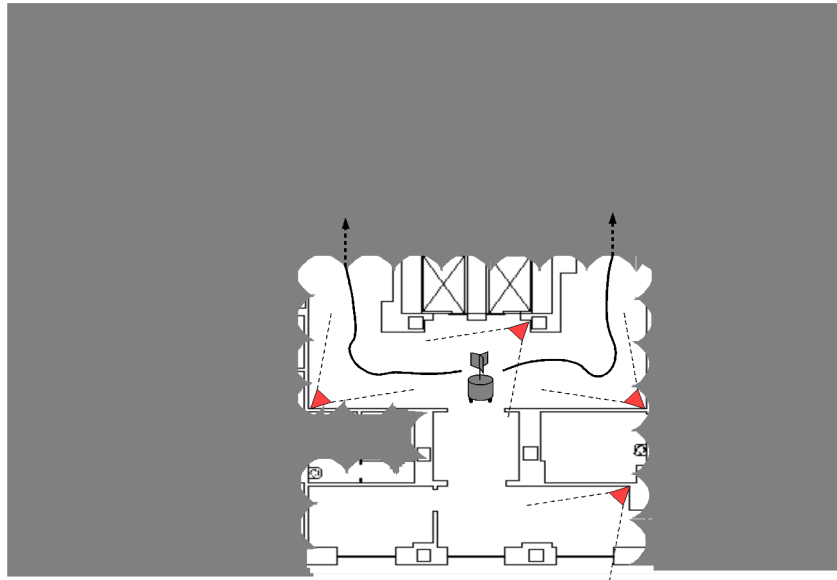
## Different Strategies





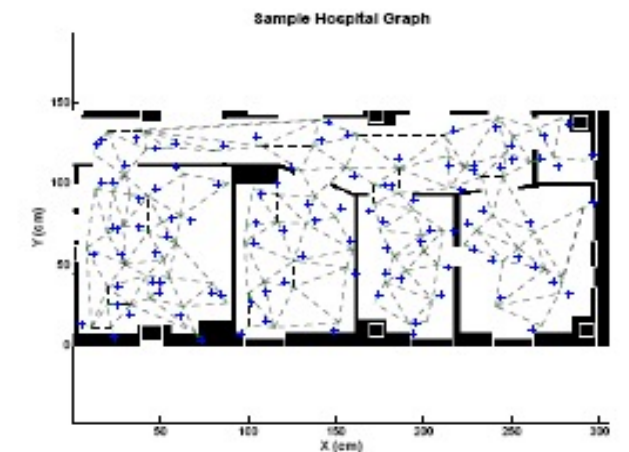
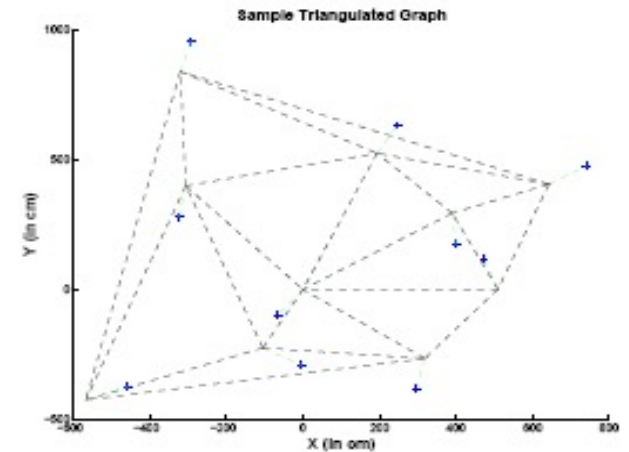
# Planning Exploratory Steps

- Choose motion in unexplored space to locate additional camera nodes
- Planner cannot simulate these paths
- Evaluated 2 strategies: 1) nearest camera and 2) a randomly selected camera

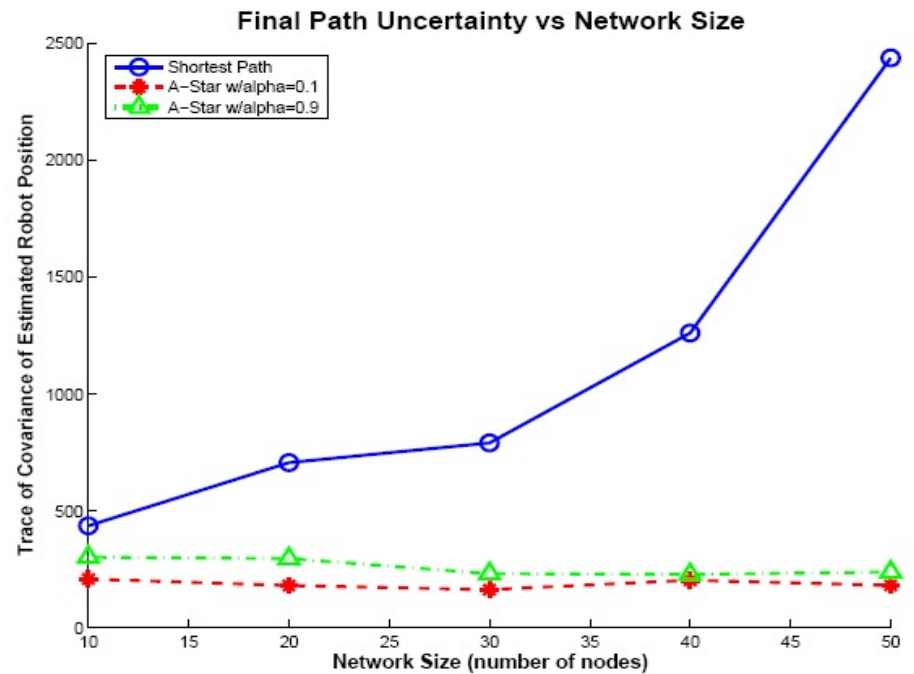
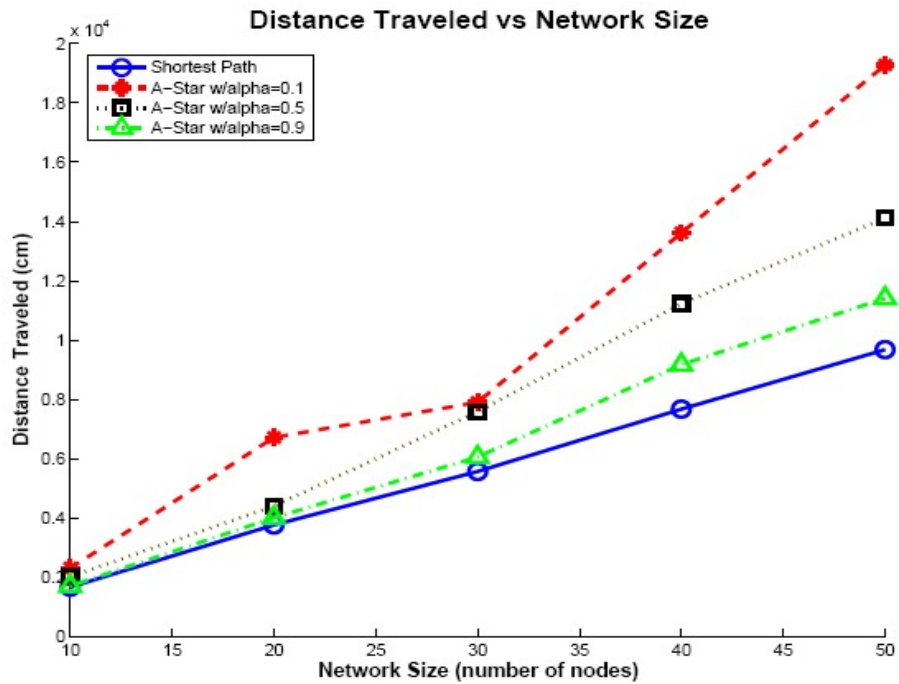


# Simulation Results

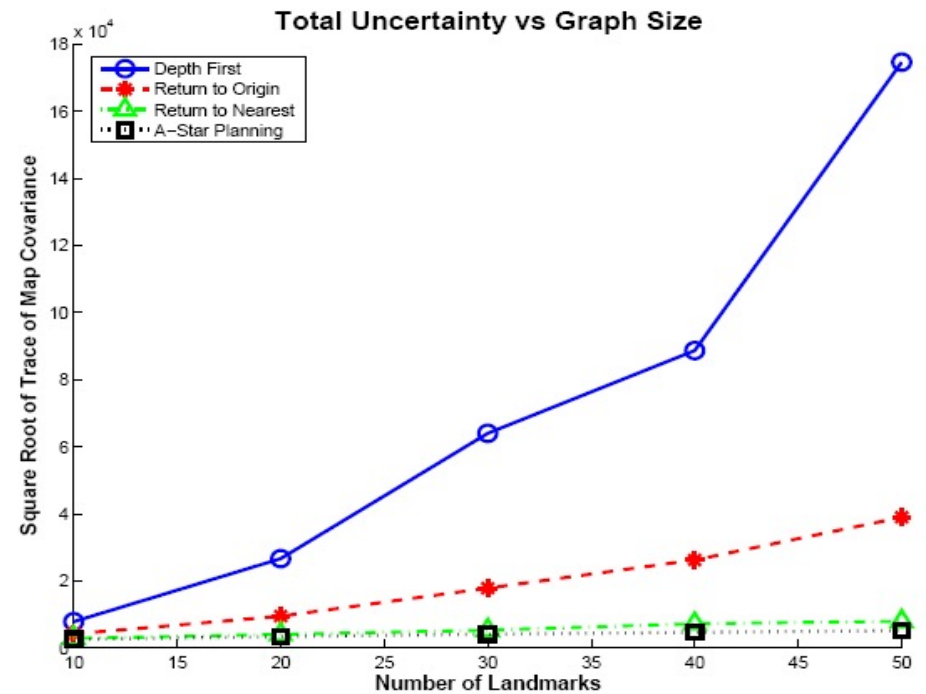
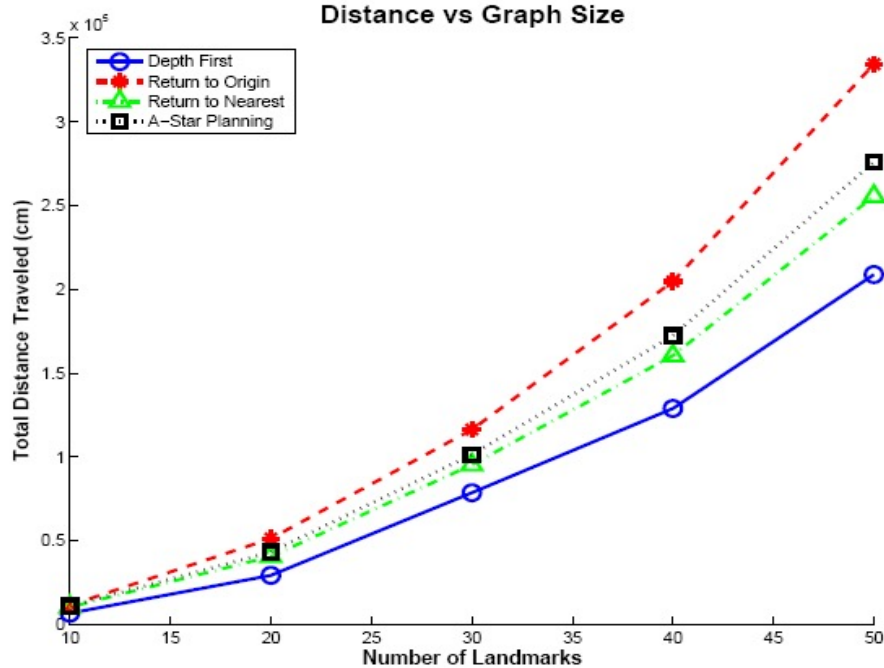
- Compared planners over many trials
- 3 realistic network types (2 shown)
- 3 methods for comparison:
  - Depth-first
  - Return to origin
  - Return to nearest explored



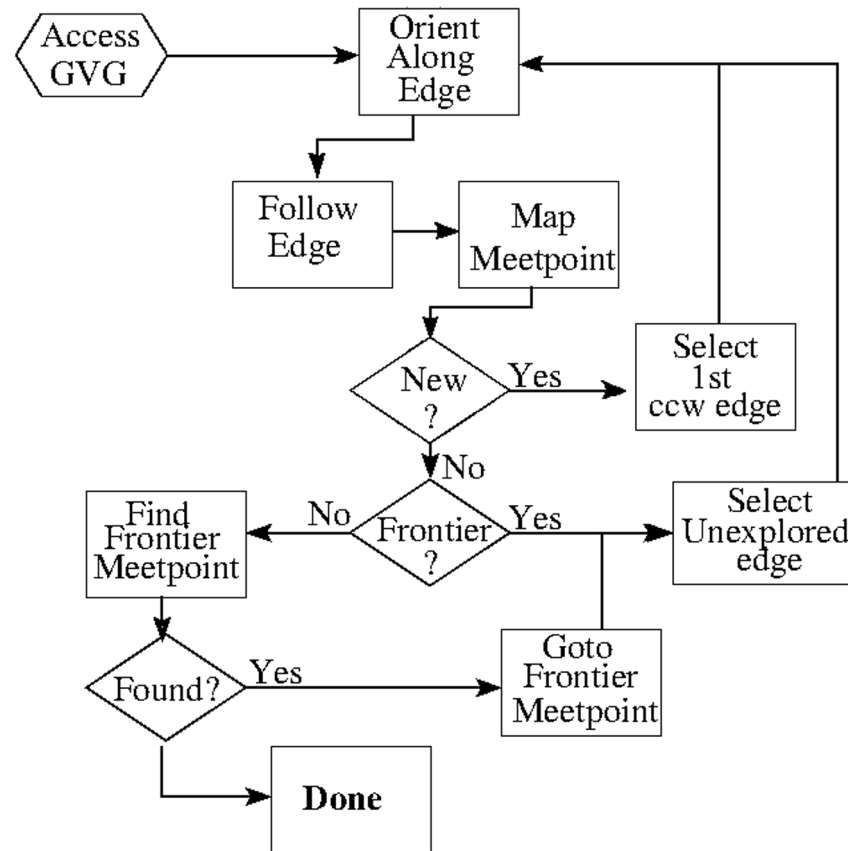
# Simulated Relocalization Results



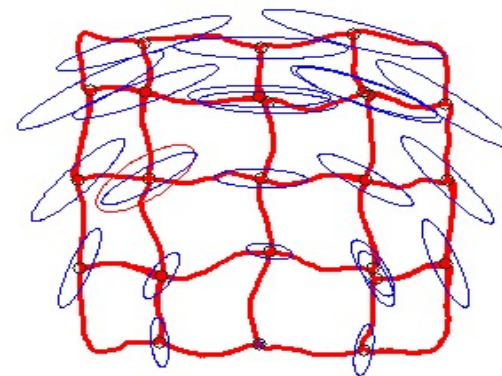
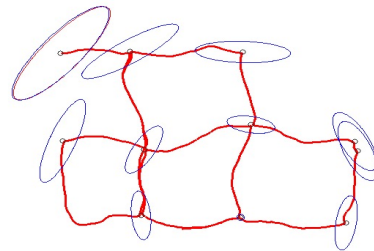
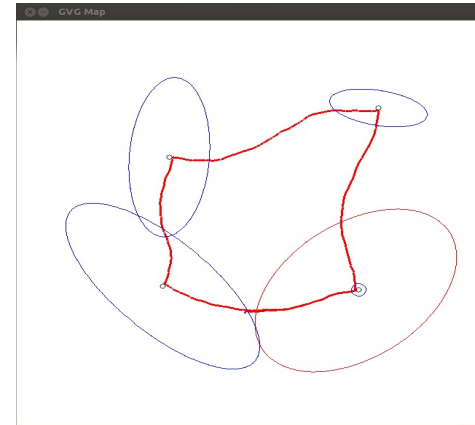
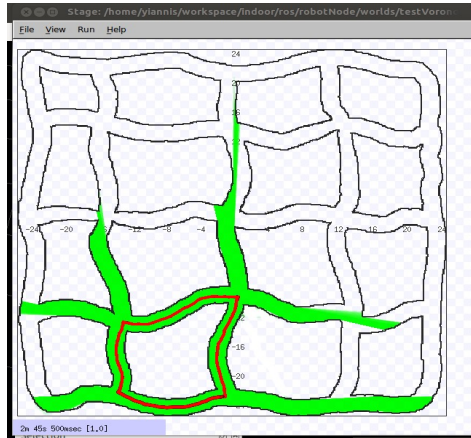
# Simulated Exploration Results



# Ear-Based Exploration Algorithm



# Exploration of the GVG

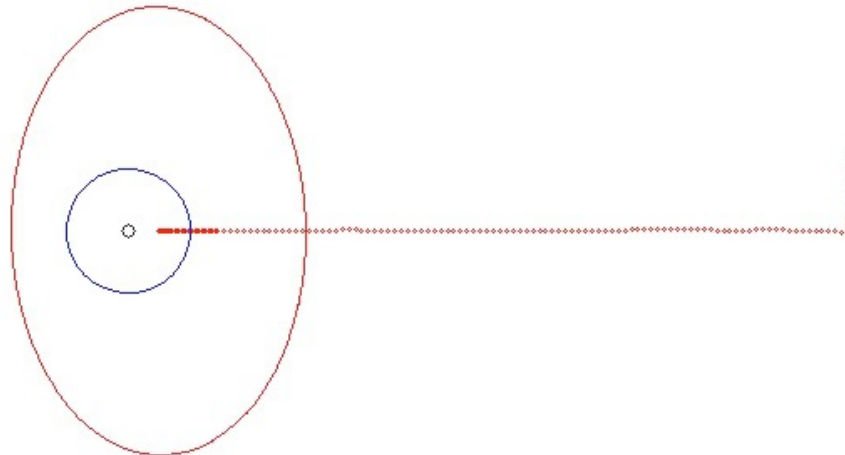


Simulation in StageRos

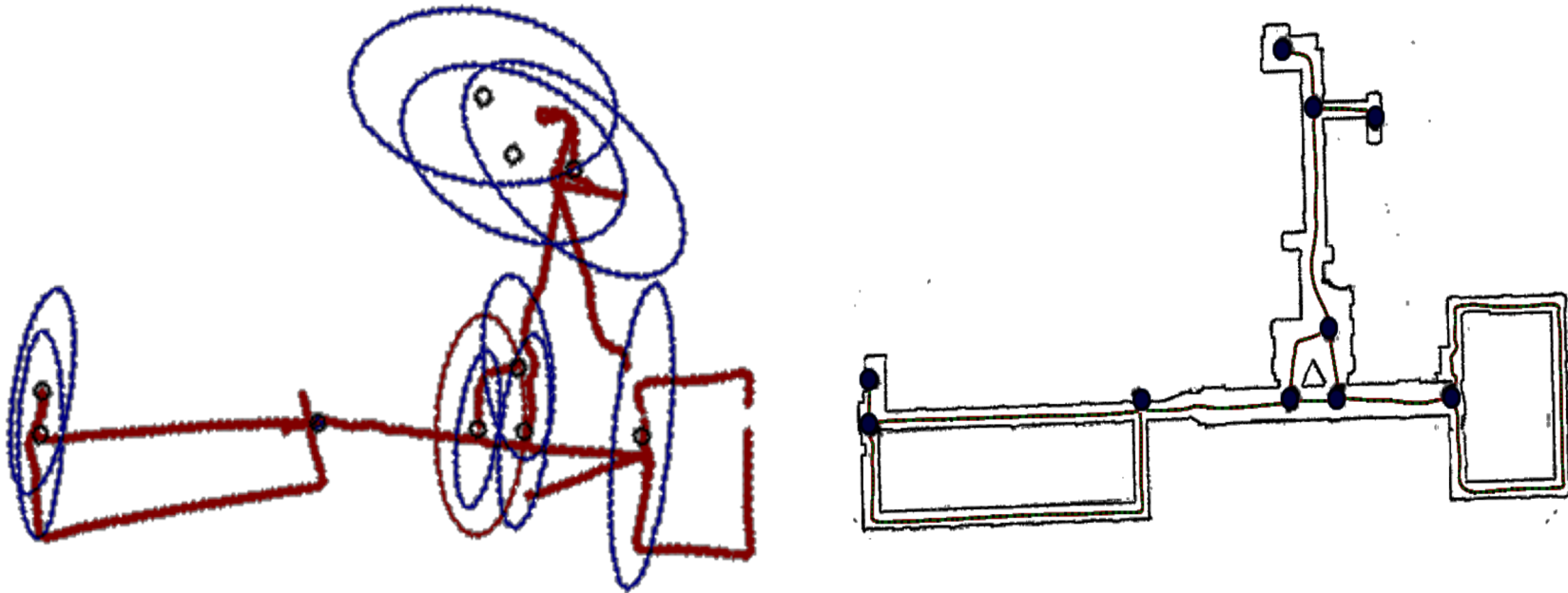


# Ear based exploration

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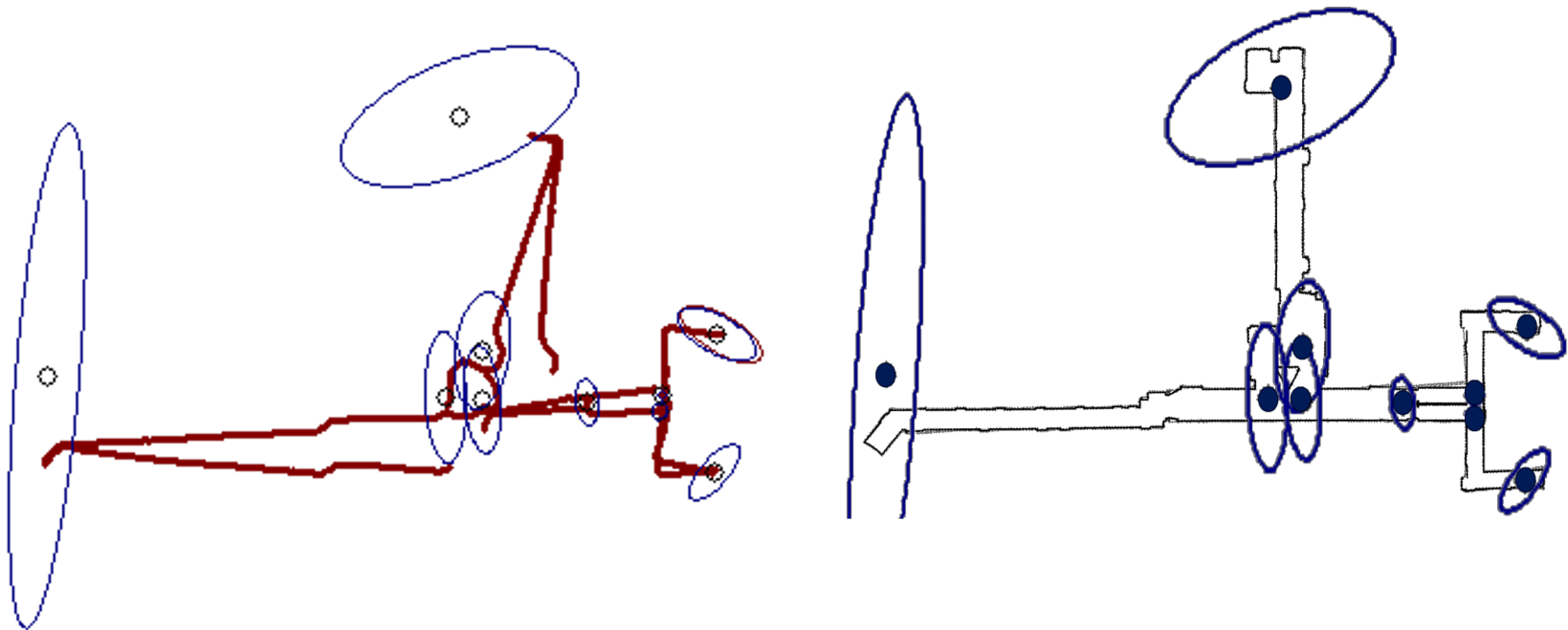
# Exploration of the GVG



Real environment, McConnell 4<sup>th</sup> floor



# Exploration of the GVG



Real environment, McConnell 3<sup>rd</sup> floor

# Video of the Ear-based Exploration

## Ear-based Exploration on Hybrid Metric/Topological Maps

Q. Zhang, D. Whitney, F. Shkurti, and I. Rekleitis  
School of Computer Science, McGill University



# Exploration Key Points

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- Mapping requires exploration
- Exploration strategies depend on the representation
- Topological representations are the most convenient for exploration
- Two objectives:
  - Explore new territory
  - Improve the accuracy by relocalization

