

CSCE 574 ROBOTICS

Path Planning

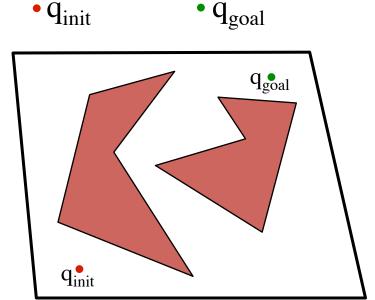
Outline

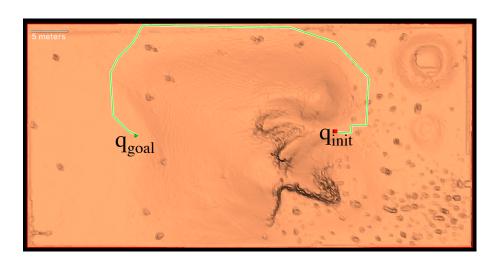
- Path Planning
 - Visibility Graph
 - Potential Fields
 - Bug Algorithms
 - Skeletons/Voronoi Graphs
 - C-Space



Motion Planning

- The ability to go from A to B
 - Known map Off-line planning
 - Unknown Environment –Online planning
 - Static/Dynamic Environment







World

Robot

Мар



World

- •Indoor/Outdoor
- •2D/2.5D/3D
- •Static/Dynamic
- •Known/Unknown
- Abstract (web)

Мар

Robot

World

Robot

Мар

- Mobile
 - ➤Indoor/Outdoor
 - ➤ Walking/Flying/Swimming
- Manipulator
- •Humanoid
- Abstract



World

Robot

Мар

- Topological
- Metric
- •Feature Based
- •1D,2D,2.5D,3D



World

- Indoor/Outdoor
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Robot

- Mobile
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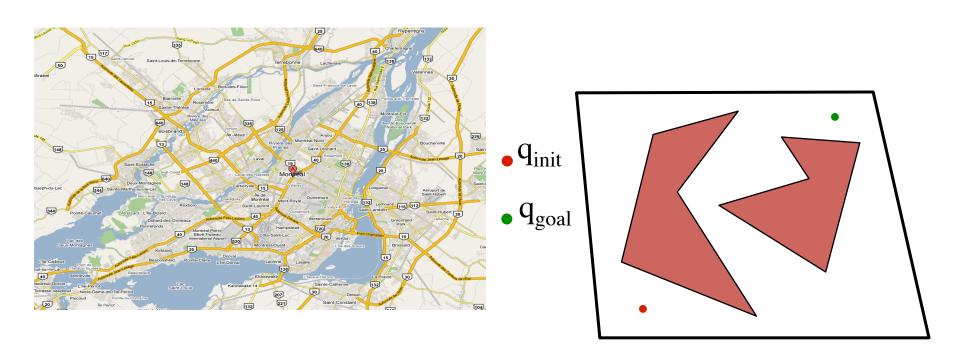
Map

- Topological
- Metric
- Feature Based
- •1D,2D,2.5D,3D



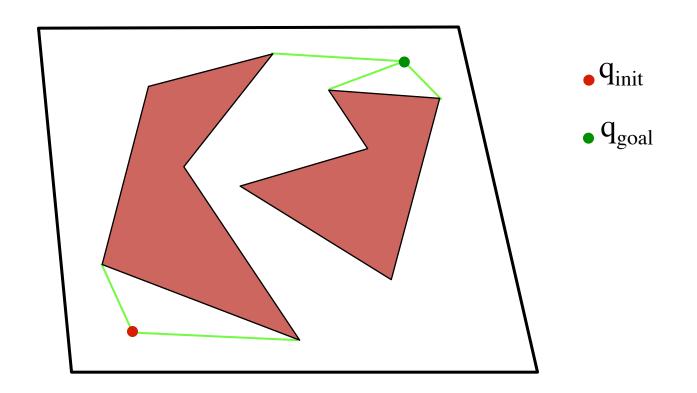
Path Planning: Assumptions

- Known Map
- Roadmaps (Graph representations)
- Polygonal Representation



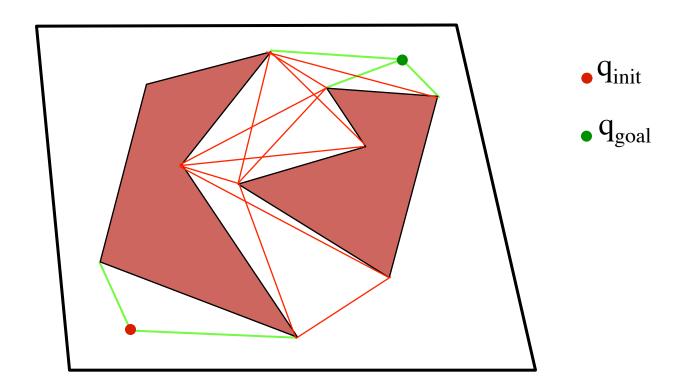


Connect Initial and goal locations with all the visible vertices



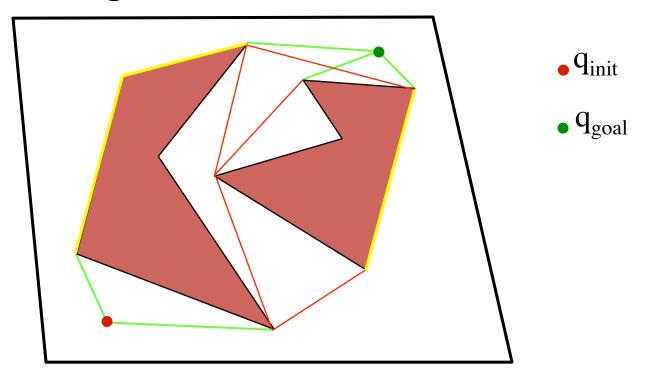


- Connect initial and goal locations with all the visible vertices
- Connect each obstacle vertex to every visible obstacle vertex





- Connect initial and goal locations with all the visible vertices
- Connect each obstacle vertex to every visible obstacle vertex
- Remove edges that intersect the interior of an obstacle

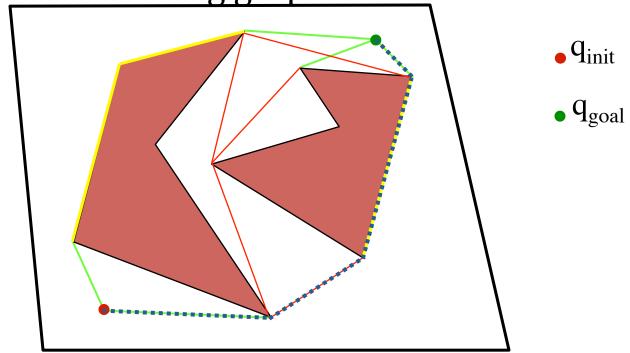




CSCE-574 Robotics

- Connect initial and goal locations with all the visible vertices
- Connect each obstacle vertex to every visible obstacle vertex
- Remove edges that intersect the interior of an obstacle

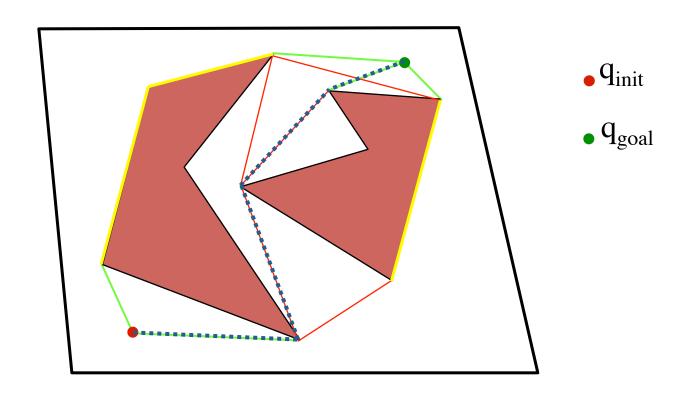
Plan on the resulting graph





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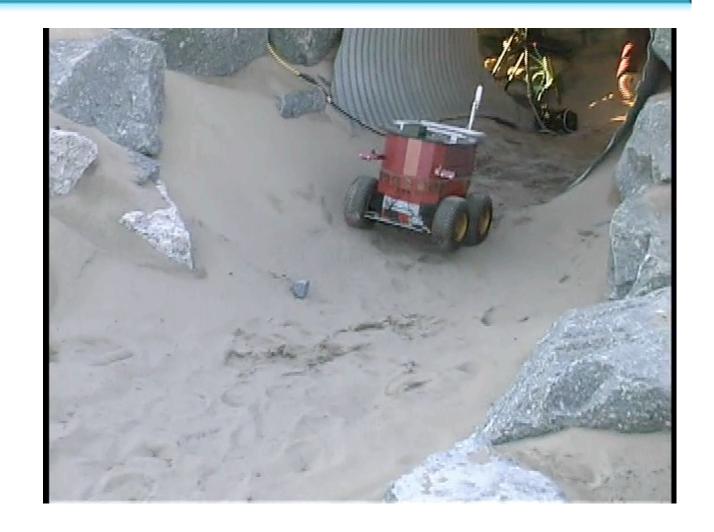
- An alternative path
- Alternative name: "Rubber band algorithm"





Major Fault

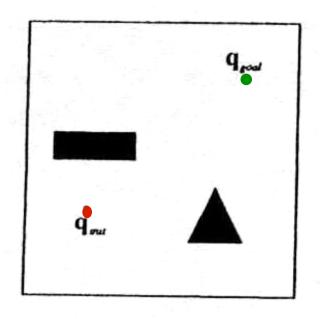
- Point robot
- Path planning like that guarantees to hit the obstacles

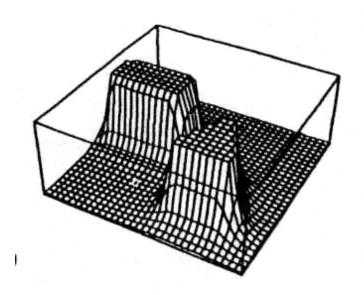




Potential Field methods

• compute a repulsive force away from obstacles



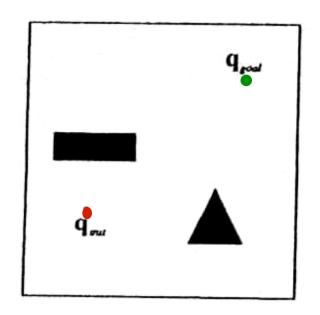


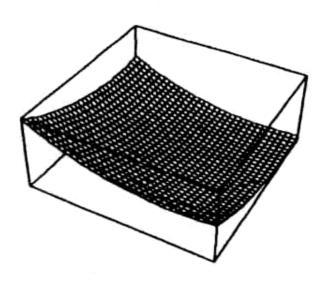


Local techniques

Potential Field methods

- compute a repulsive force away from obstacles
- compute an attractive force toward the goal



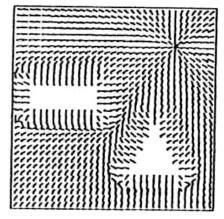


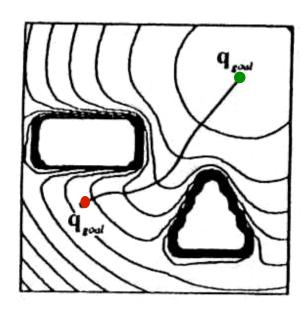


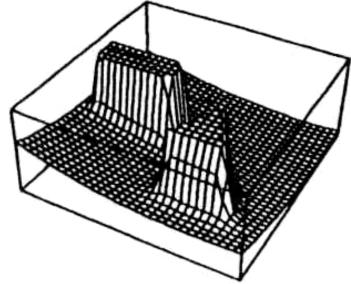
Local techniques

Potential Field methods

- compute a repulsive force away from obstacles
- compute an attractive force toward the goal
- → let the sum of the forces control the robot





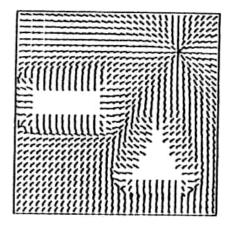


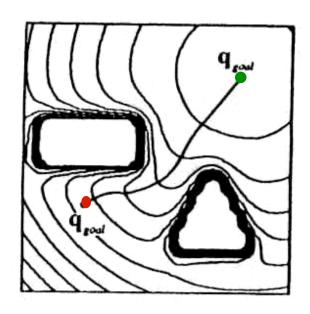


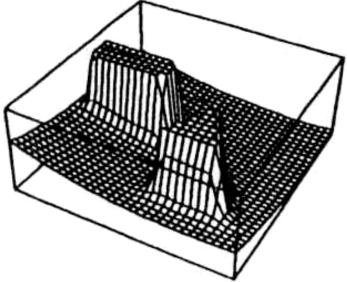
Local techniques

Potential Field methods

- compute a repulsive force away from obstacles
- compute an attractive force toward the goal
- → let the sum of the forces control the robot





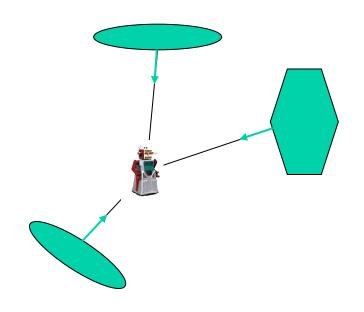




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To a large extent, this is 19 computable from sensor readings

Sensor Based Calculations

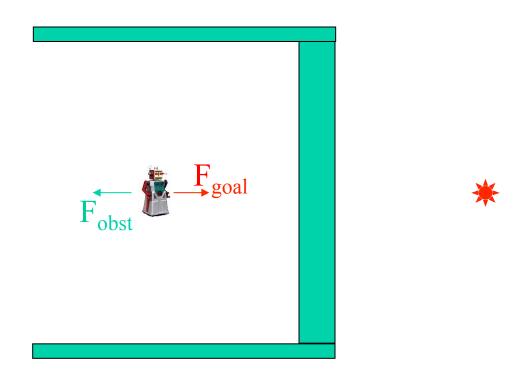




Major Problem?



Local Minima!





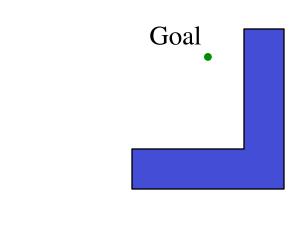
Simulated Annealing

• Every so often add some random force



Limited-knowledge path planning

- Path planning with limited knowledge
 - Insect-inspired "bug" algorithms



Start



- otherwise local sensing walls/obstacles encoders
- •"reasonable" world
- 1. finitely many obstacles in any finite disc
- 2. a line will intersect an obstacle finitely many times



Not truly modeling bugs...

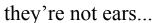
Insects do use several cues for navigation:



visual landmarks
polarized light
chemical sensing



neither are the current bugsized robots



Other animals use information from

magnetic fields

electric currents

temperature



CSCE-574 Robotics

bacteria

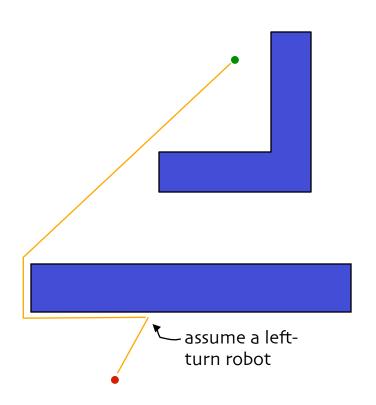


migrating bobolink



Bug Strategy

Insect-inspired "bug" algorithms



- known direction to goal
- otherwise only local sensing walls/obstacles encoders

"Bug 0" algorithm

- 1) head toward goal
- 2) follow obstacles until you can head toward the goal again
- 3) continue



Does It Work?

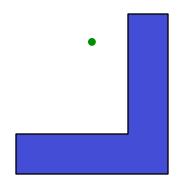


Bug 1

Insect-inspired "bug" algorithms

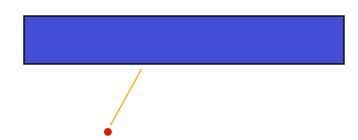


 otherwise only local sensing walls/obstacles encoders



"Bug 1" algorithm

1) head toward goal



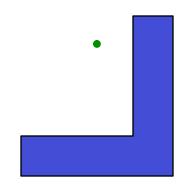


Bug 1

Insect-inspired "bug" algorithms



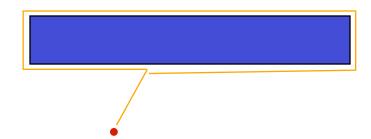
 otherwise only local sensing walls/obstacles encoders



"Bug 1" algorithm

1) head toward goal

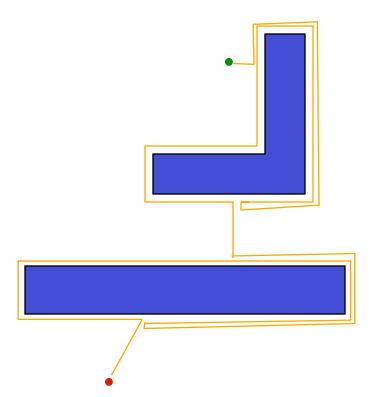
2) if an obstacle is encountered, circumnavigate it *and* remember how close you get to the goal





Bug 1

Insect-inspired "bug" algorithms



- known direction to goal
- otherwise only local sensing walls/obstacles encoders

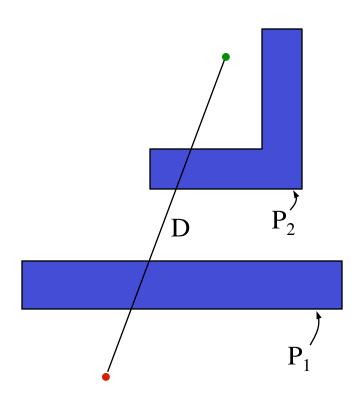
"Bug 1" algorithm

- 1) head toward goal
- 2) if an obstacle is encountered, circumnavigate it *and* remember how close you get to the goal
- 3) return to that closest point (by wall-following) and continue



Bug 1 analysis

Distance Traveled



What are bounds on the path length that the robot takes?

Available Information:

D = straight-line distance from start to goal

 P_i = perimeter of the *i*th obstacle

Lower and upper bounds?

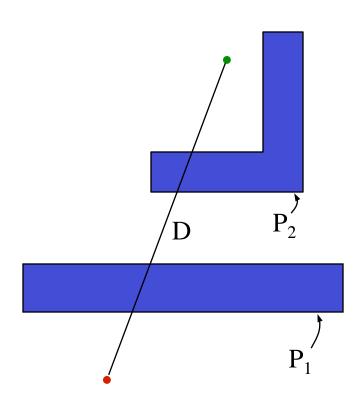
Lower bound:

Upper bound:



Bug 1 analysis

Distance Traveled



What are bounds on the path length that the robot takes?

Available Information:

D = straight-line distance from start to goal

 P_i = perimeter of the *i*th obstacle

Lower and upper bounds?

Lower bound: D

Upper bound:



Bug 1 analysis

Distance Traveled

What are bounds on the path length that the robot takes?

Available Information:

D = straight-line distance from start to goal

 P_i = perimeter of the *i*th obstacle

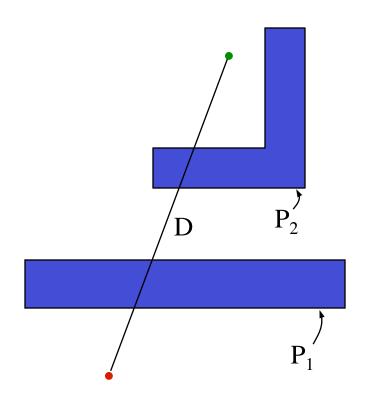
Lower and upper bounds?

Lower bound: D

Upper bound: $D + 1.5 \sum_{i} P_{i}$

How good a bound?

How good an algorithm?



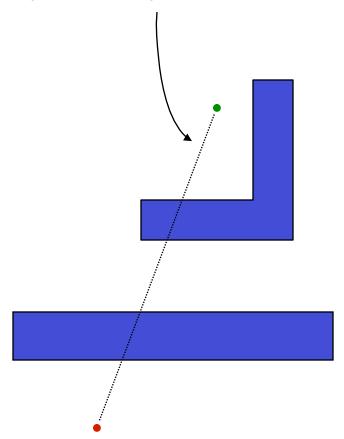
Bug Mapping





A better bug?

Call the line from the starting point to the goal the *s-line*

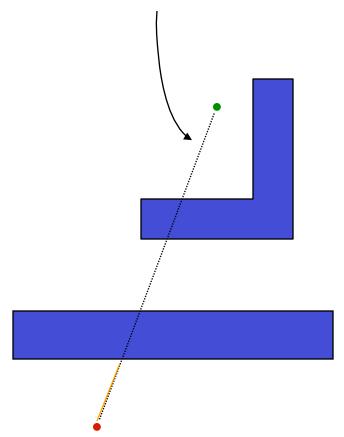


"Bug 2" algorithm



A better bug?

Call the line from the starting point to the goal the *s-line*



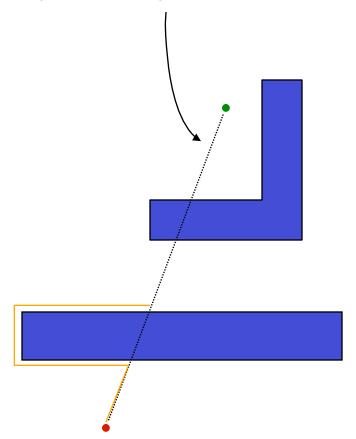
"Bug 2" algorithm

1) head toward goal on the *s-line*



A better bug?

Call the line from the starting point to the goal the *s-line*



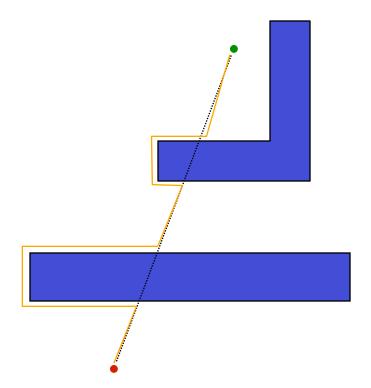
"Bug 2" algorithm

- 1) head toward goal on the *s-line*
- 2) if an obstacle is in the way, follow it until encountering the sline again.



A better bug?

s-line

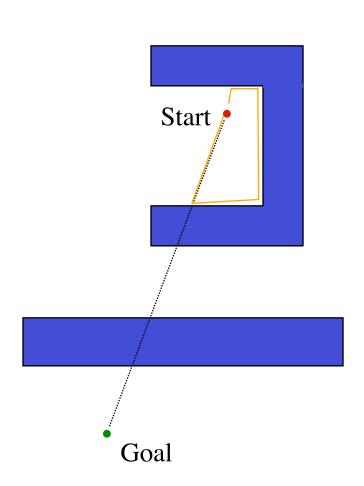


"Bug 2" algorithm

- 1) head toward goal on the *s-line*
- 2) if an obstacle is in the way, follow it until encountering the sline again.
- 3) Leave the obstacle and continue toward the goal



A better bug?

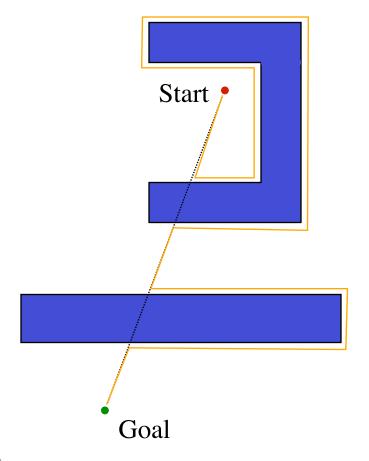


"Bug 2" algorithm

- 1) head toward goal on the *s-line*
- 2) if an obstacle is in the way, follow it until encountering the sline again *closer to the goal*.
- 3) Leave the obstacle and continue toward the goal



Distance Traveled



What are bounds on the path length that the robot takes?

Available Information:

D = straight-line distance from start to goal

 P_i = perimeter of the *i*th obstacle

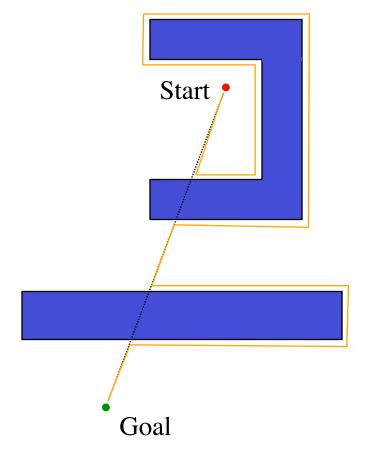
Lower and upper bounds?

Lower bound:

Upper bound:



Distance Traveled



What are bounds on the path length that the robot takes?

Available Information:

D = straight-line distance from start to goal

 P_i = perimeter of the *i*th obstacle

 N_i = number of s-line intersections with the ith obstacle

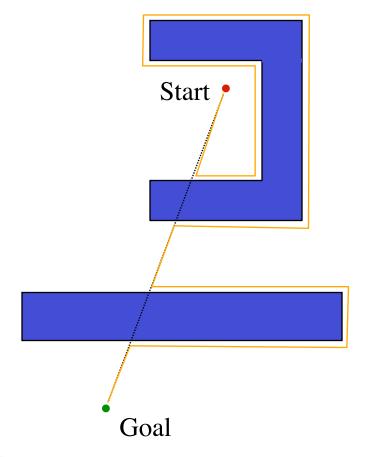
Lower and upper bounds?

Lower bound:

Upper bound:



Distance Traveled



What are bounds on the path length that the robot takes?

Available Information:

D = straight-line distance from start to goal

 P_i = perimeter of the *i*th obstacle

 N_i = number of s-line intersections with the i th obstacle

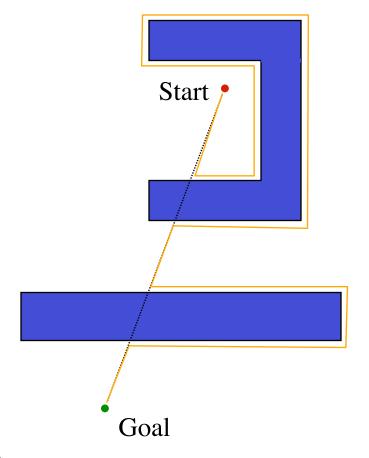
Lower and upper bounds?

Lower bound: D

Upper bound:



Distance Traveled



What are bounds on the path length that the robot takes?

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 P_i = perimeter of the *i*th obstacle

 N_i = number of s-line intersections with the i th obstacle

Lower and upper bounds?

Lower bound: D

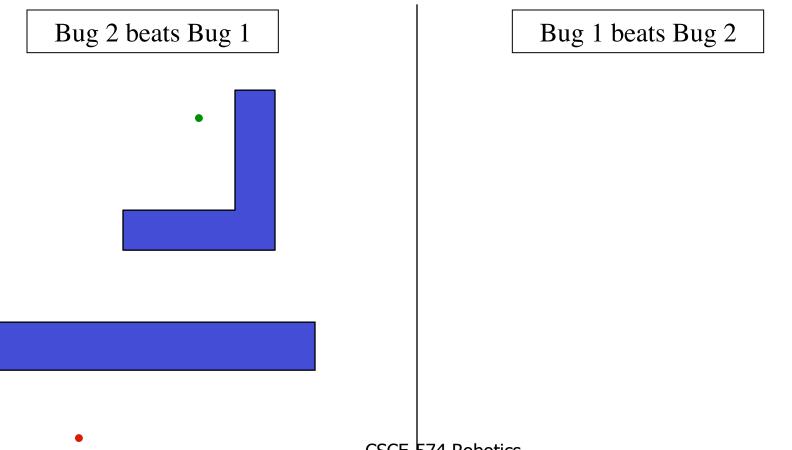
Upper bound: $D + 0.5 \sum_{i} N_i P_i$



head-to-head comparison

or thorax-to-thorax, perhaps

What are worlds in which Bug 2 does better than Bug 1 (and vice versa)?

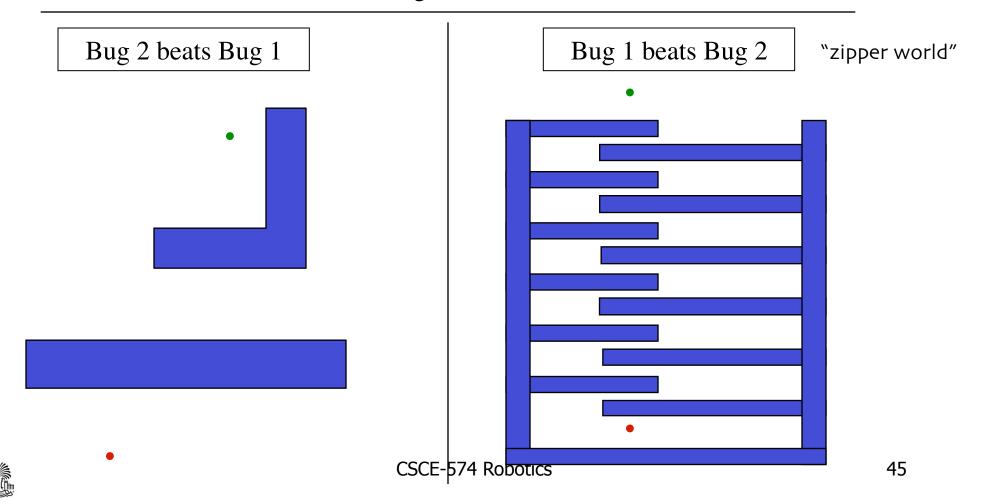




head-to-head comparison

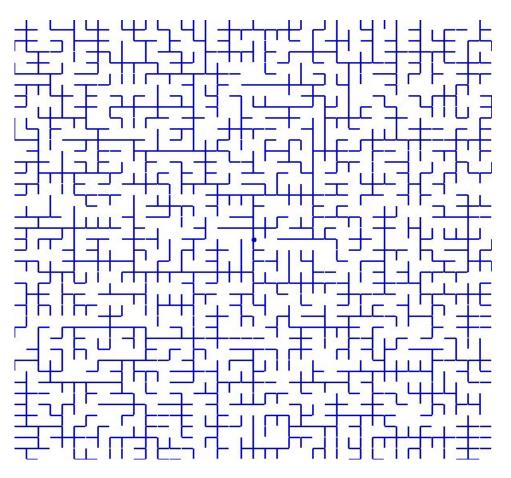
or thorax-to-thorax, perhaps

What are worlds in which Bug 2 does better than Bug 1 (and vice versa)?



Other bug-like algorithms

The Pledge maze-solving algorithm

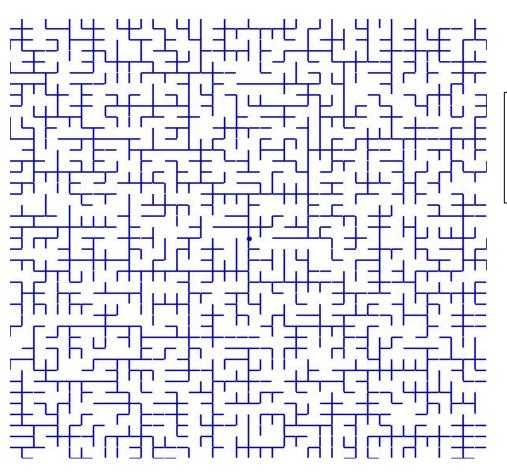


- 1. Go to a wall
- 2. Keep the wall on your right
- 3. Continue until out of the maze



Other bug-like algorithms

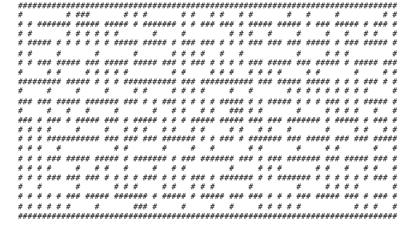
The Pledge maze-solving algorithm



- 1) Go to a wall
- 2) Keep the wall on your right
- 3) Continue until out of the maze

int a[1817]; main(z,p,q,r){for(p=80;q+p-80;p=2*a[p]) for(z=9;z--;)q=3&(r=time(0)+r*57)/7,q=q?q-1?q-2?1-p %79?-1:0:p%79-77?1:0:p<1659?79:0:p>158?-79:0,q?!a[p+q*2]?a[p+=a[p+=q]=q]=q:0:0;for(;q++-1817;)printf(q %79?"%c":"%c\n"," #"[!a[q-1]]);}

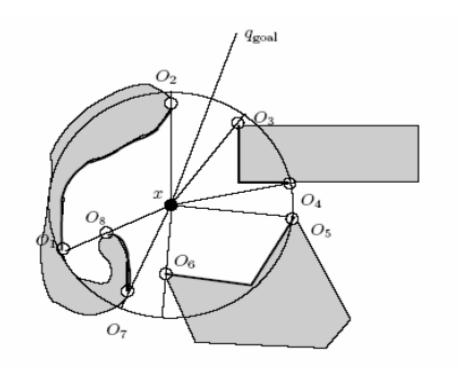
IOCCC random maze generator





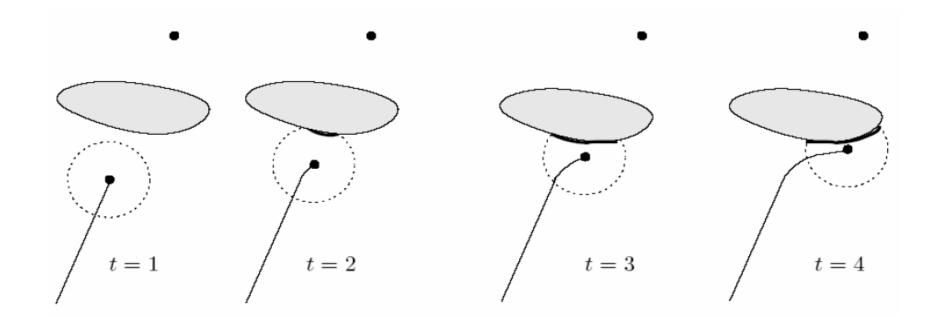
Tangent Bug

- Limited Range Sensor
- Tangent Bug relies on finding endpoints of finite, continues segments of the obstacles



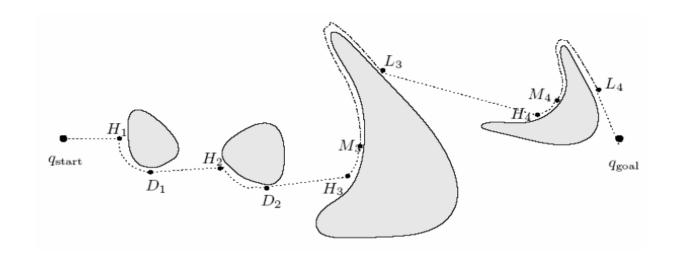


Tangent Bug





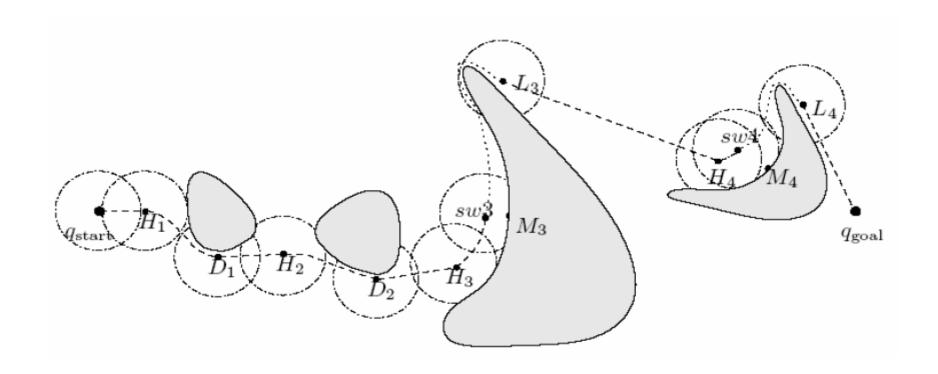
Contact Sensor Tangent Bug



- 1. Robot moves toward goal until it hits obstacle 1 at H1
- 2. Pretend there is an infinitely small sensor range and the direction which minimizes the heuristic is to the right
- 3. Keep following obstacle until robot can go toward obstacle again
- 4. Same situation with second obstacle
- 5. At third obstacle, the robot turned left until it could not increase heuristic
- 6. D_followed is distance between M3 and goal, d_reach is distance between robot and goal because sensing distance is zero

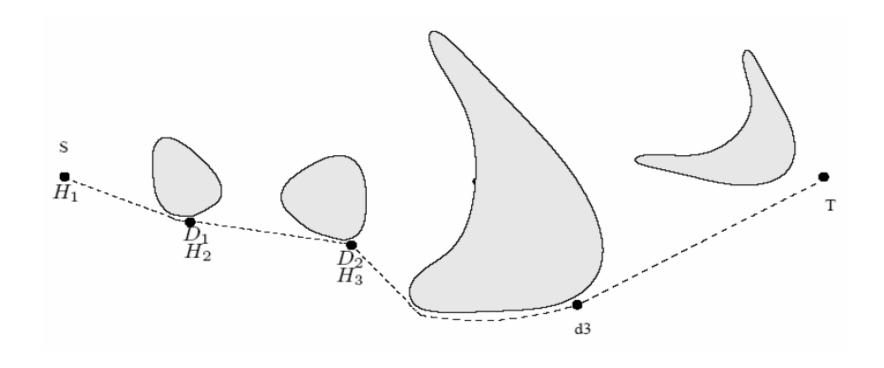


Limited Sensor Range Tangent-Bug





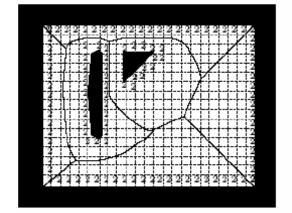
Infinite Sensor Range Tangent Bug

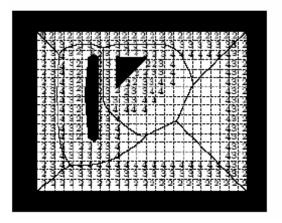


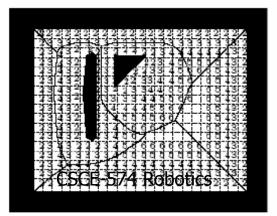


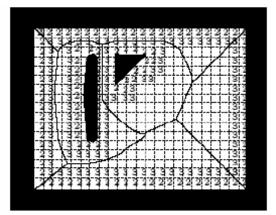
Known Map

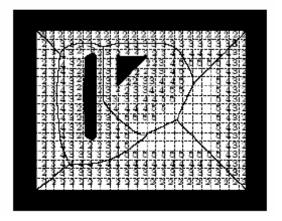
Brushfire Transform

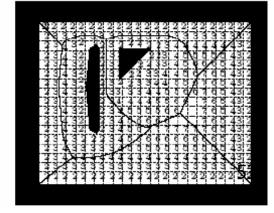






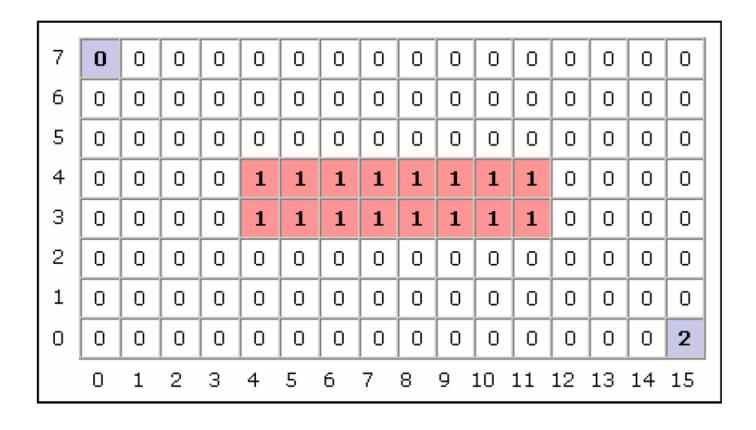








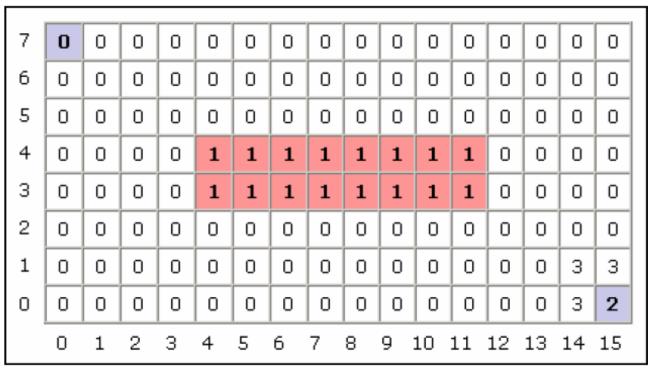
The Wavefront Planner: Setup





The Wavefront in Action (Part 1)

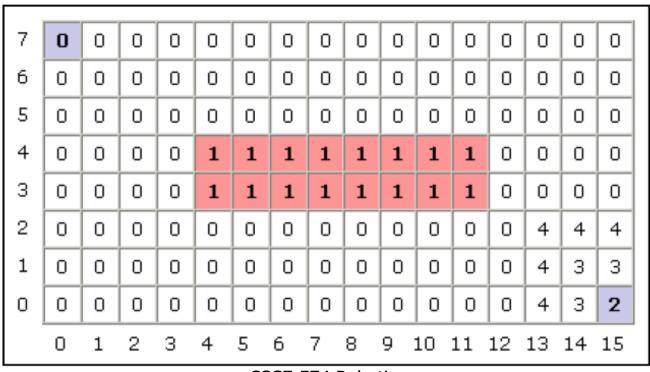
- Starting with the goal, set all adjacent cells with "0" to the current cell + 1
 - 4-Point Connectivity or 8-Point Connectivity?
 - Your Choice. We'll use 8-Point Connectivity in our example





The Wavefront in Action (Part 2)

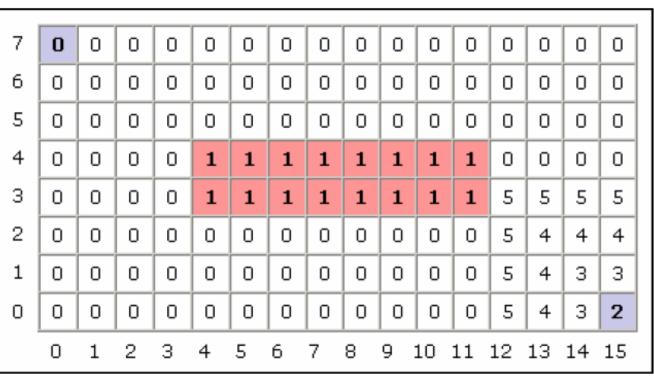
- Now repeat with the modified cells
 - This will be repeated until no 0's are adjacent to cells with values ≥ 2
- 0's will only remain when regions are unreachable





The Wavefront in Action (Part 3)

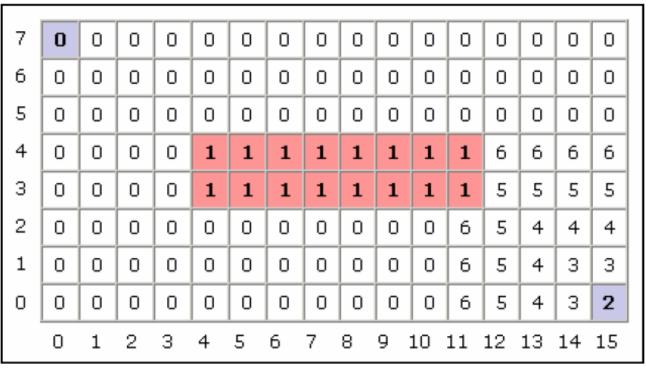
Repeat





The Wavefront in Action (Part 3)

Repeat





The Wavefront in Action (Part 3)

Until Done

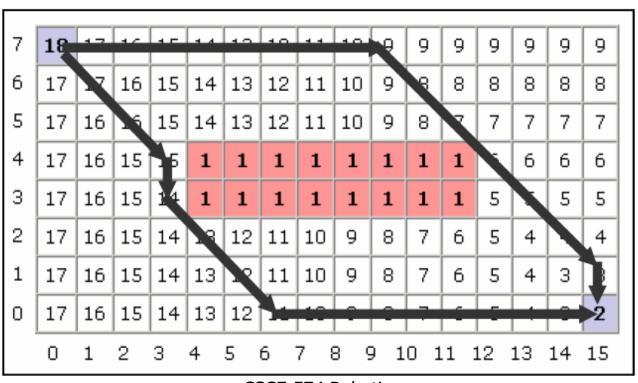
- 0's would only remain in the unreachable areas

7	18	17	16	15	14	13	12	11	10	9	9	9	9	9	9	9
6	17	17	16	15	14	13	12	11	10	9	8	8	8	8	8	8
5	17	16	16	15	14	13	12	11	10	9	8	7	7	7	7	7
4	17	16	15	15	1	1	1	1	1	1	1	1	6	6	6	6
3	17	16	15	14	1	1	1	1	1	1	1	1	5	5	5	5
2	17	16	15	14	13	12	11	10	9	8	7	6	5	4	4	4
1	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	3
0	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2
	0	1	2	3	4	5	6	7 8	3 9) 1	0 1	.1	12	13	14	15



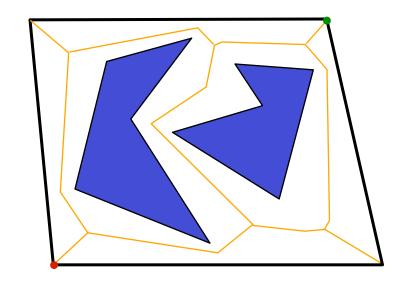
The Wavefront in Action

- To find the shortest path, according to your metric, simply always move toward a cell with a lower number
 - The numbers generated by the Wavefront planner are roughly proportional to their distance from the goal

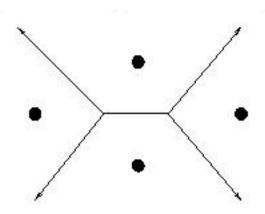




An alternative roadmap



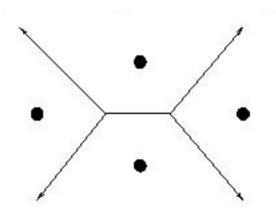




These line segments make up the **Voronoi diagram** for the four points shown here.

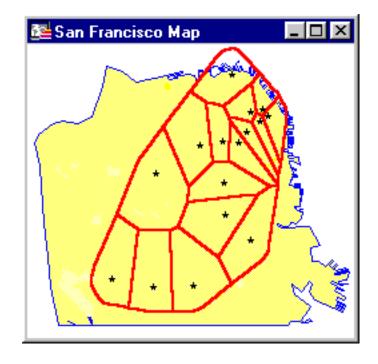
Solves the "Post Office Problem"





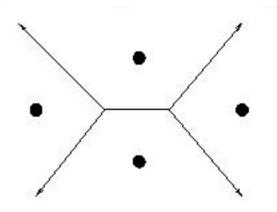
These line segments make up the **Voronoi diagram** for the four points shown here.

Solves the "Post Office Problem"

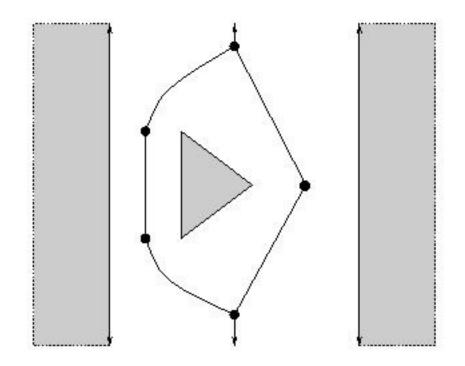


or, perhaps, more important problems...





"true" Voronoi diagram (isolates a set of points)

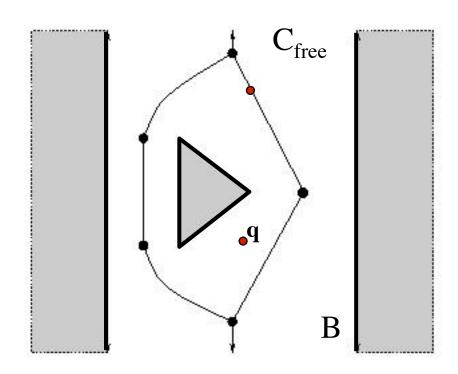


generalized Voronoi diagram What is it?



Let B =the boundary of C_{free} .

Let \mathbf{q} be a point in C_{free} . (•)





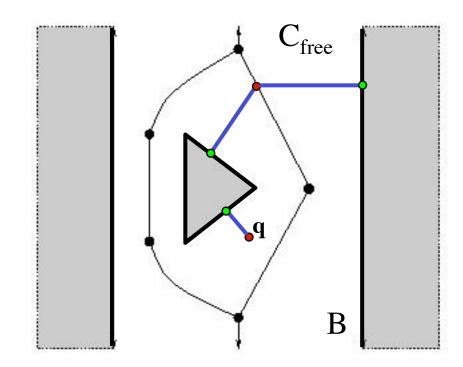
Cfree

Let B =the boundary of C_{free} .

Let \mathbf{q} be a point in C_{free} .

Define *clearance*(q) = min $\{ | q - p | \}$, for all $p \in B$





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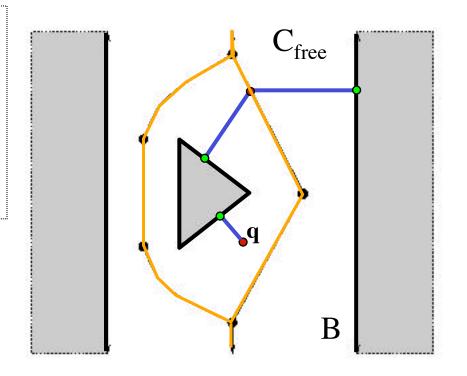
Define $near(q) = \{ p \in B \text{ such that } | q - p | = clearance(q) \}$



Evaluation

- + maximizes distance from obstacles
- + reduces to graph search
- + can be used in higher-dimensions
- nonoptimal
- real diagrams tend to be noisy

Let B = the boundary of C_{free} . Let q be a point in C_{free} .

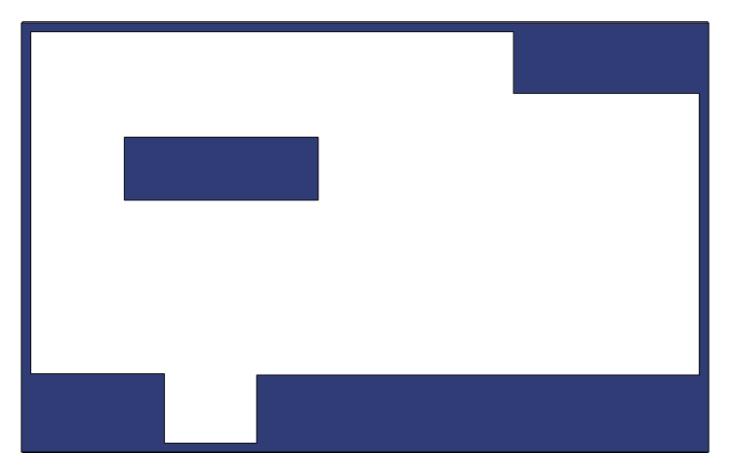


Define
$$clearance(q) = min \{ | q - p | \}, for all p \in B$$

Define
$$near(q) = \{ p \in B \text{ such that } | q - p | = clearance(q) \}$$

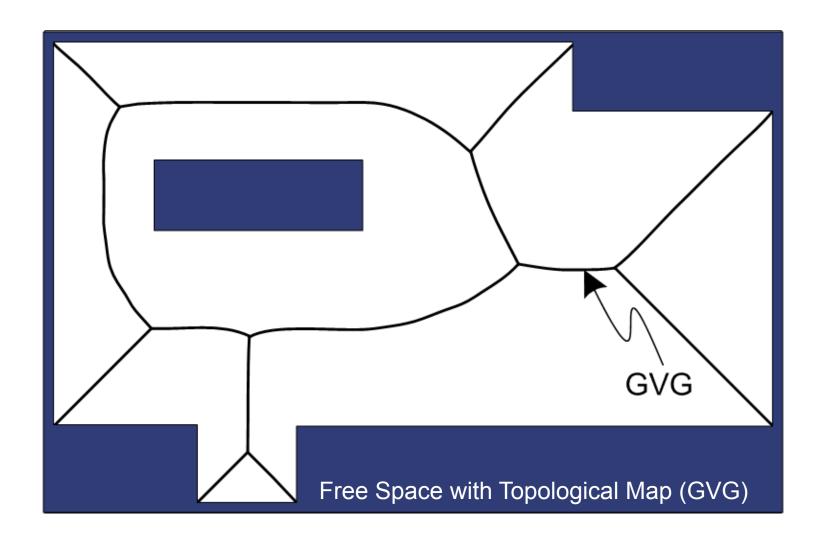
q is in the *Voronoi diagram* of C_{free} if |near(q)| > 1CSCE-574 Robotics

Generalized Voronoi Graph (GVG)



CSCE-574 Robotics

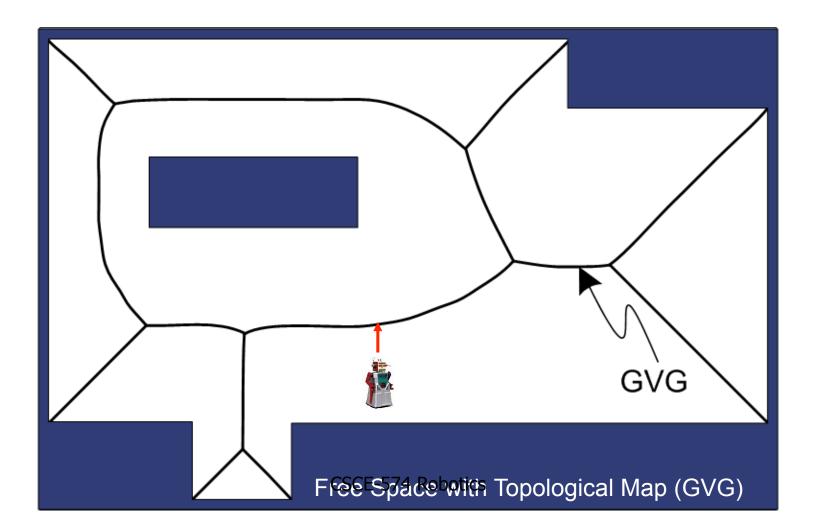
Generalized Voronoi Graph (GVG)





Generalized Voronoi Graph (GVG)

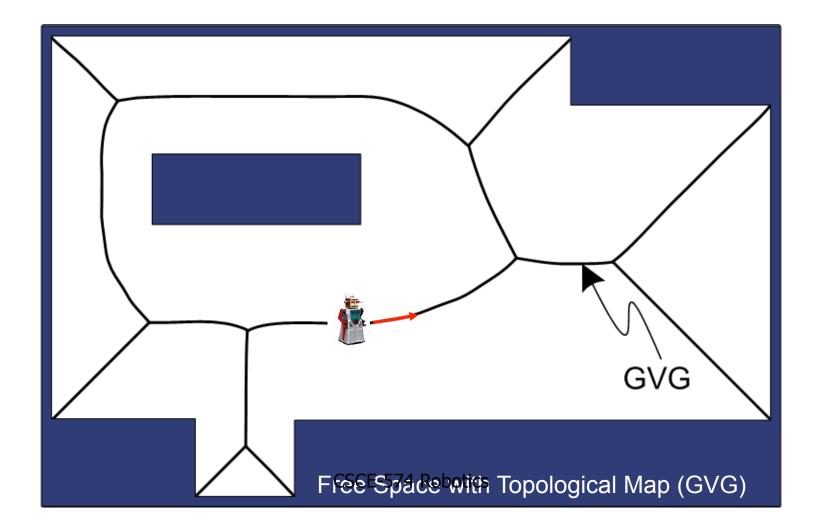
Access GVG





Generalized Voronoi Graph (GVG)

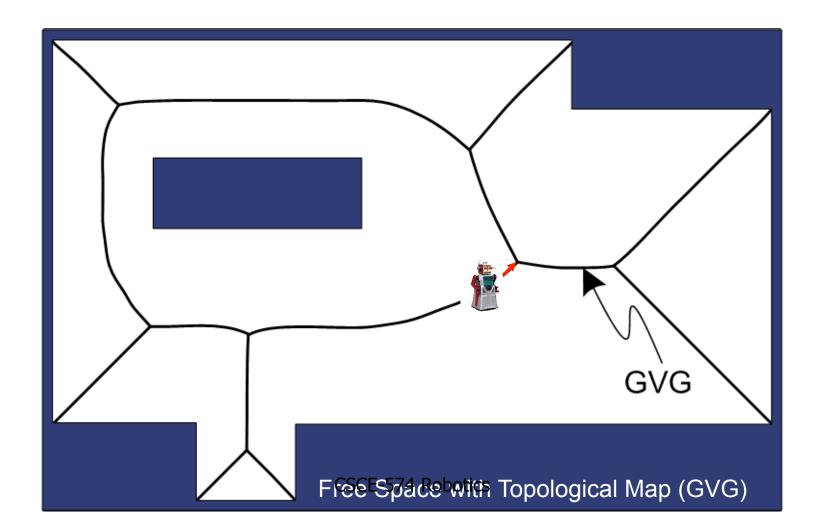
- Access GVG
- •Follow Edge





Generalized Voronoi Graph (GVG)

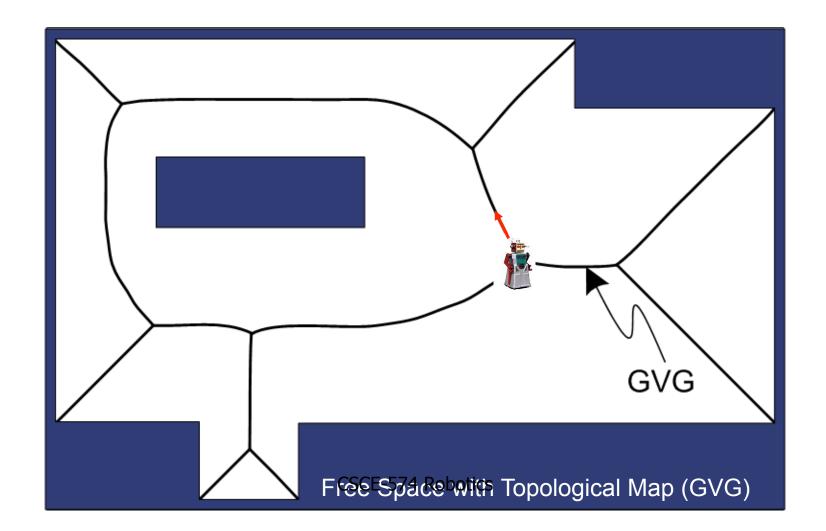
- •Access GVG •Home to the MeetPoint
- •Follow Edge





Generalized Voronoi Graph (GVG)

- •Access GVG •Home to the MeetPoint
- •Follow Edge •Select Edge





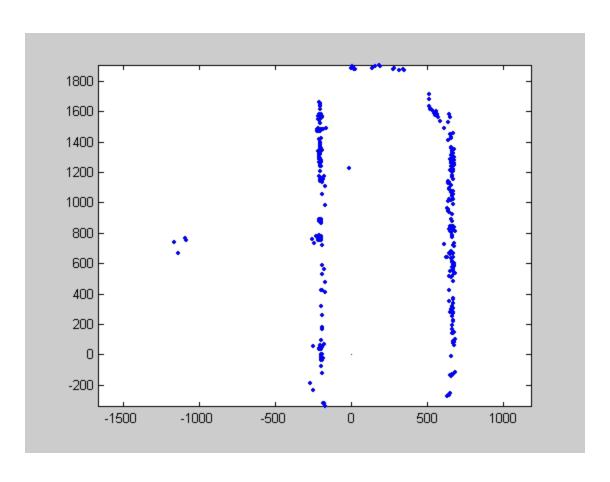
GVG construction using sonar



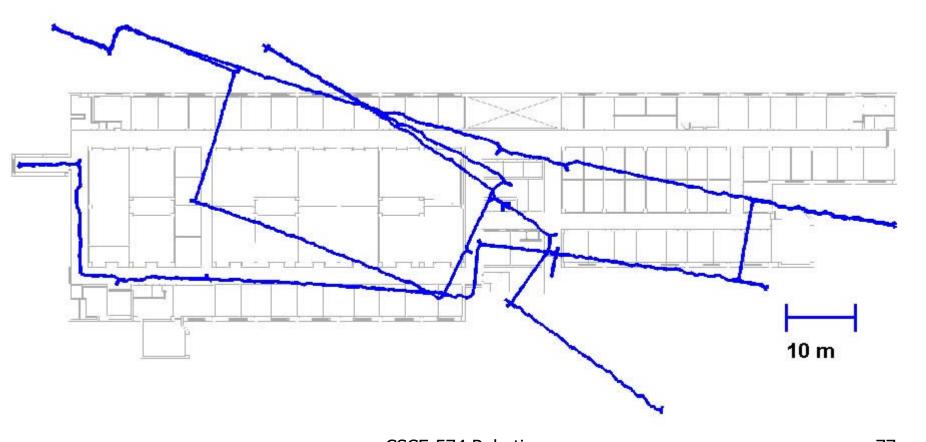
- Nomadic Scout
- Sonar (GVG navigation)
- Camera with omni-directional mirror (feature detection)
- Onboard 1.2 GHz processor



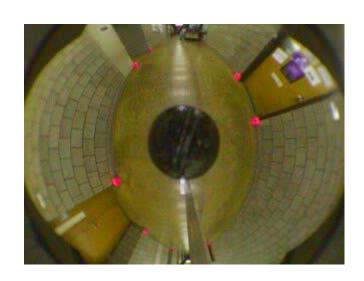
GVG construction using sonar



GVG construction using sonar



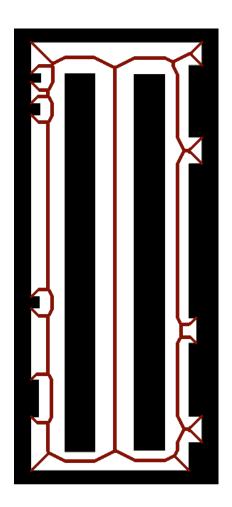
Slammer in Action

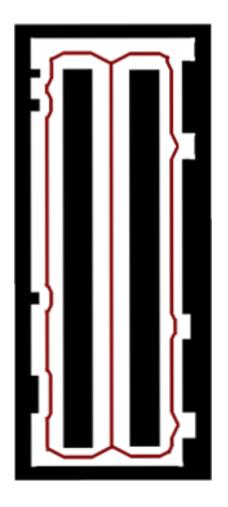






Removing Edges



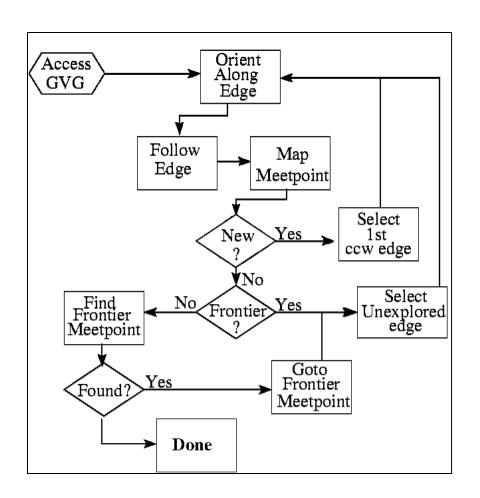


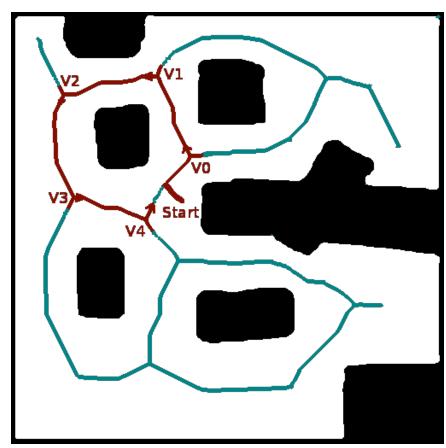


Meetpoint Detection

- 3σ uncertainty ellipse of explored meetpoints
- Meetpoint degree (branching factor)
- Distances to local obstacles
- Relative angle bearings
- Edge signature
 - Edge length
 - Edge Curvature
- Vertex signal

Ear-based Exploration

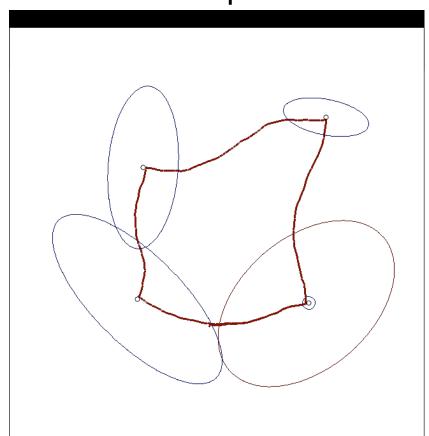




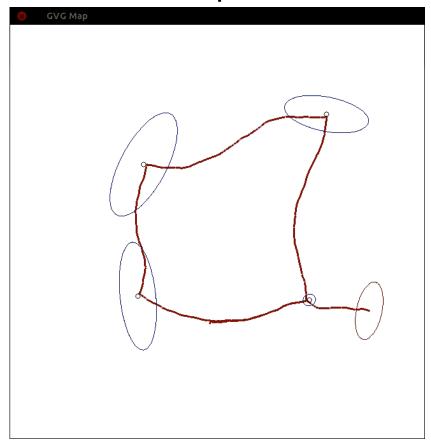


Uncertainty Reduction

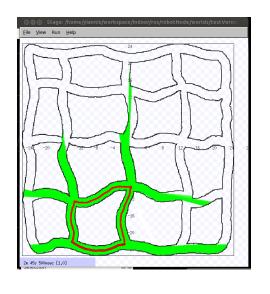
Before Loop-closure

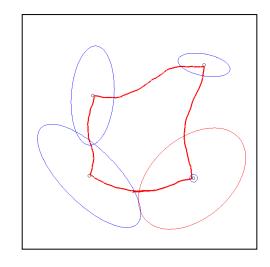


After Loop-closure

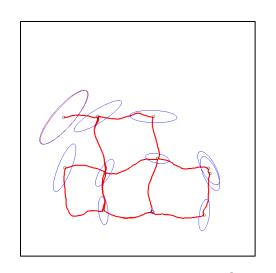


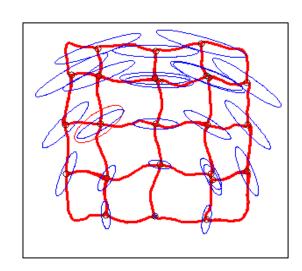






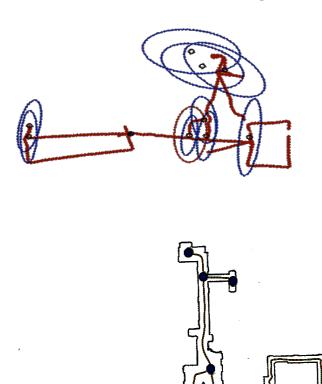
Simulation

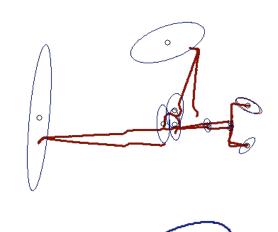


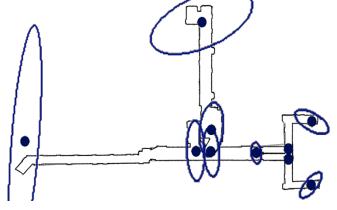




Real Environment

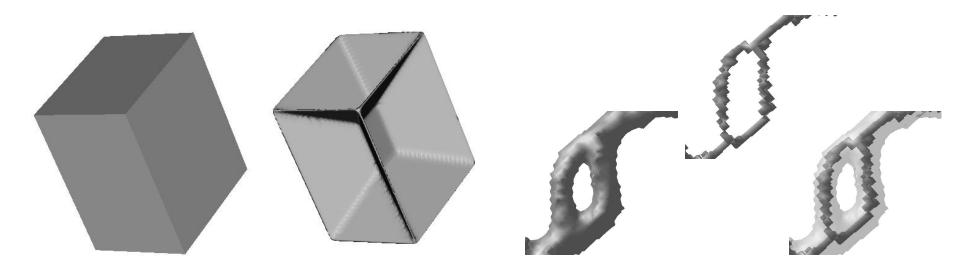




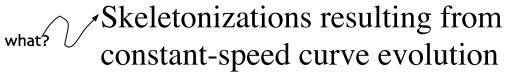




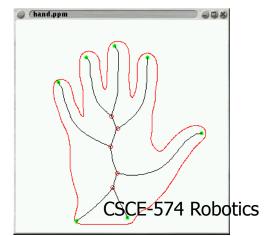
Voronoi applications



A retraction of a 3d object == "medial surface"





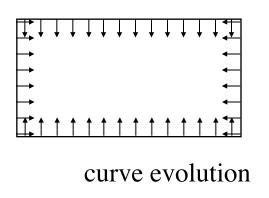


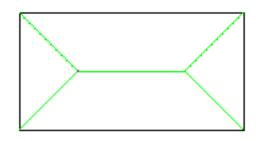


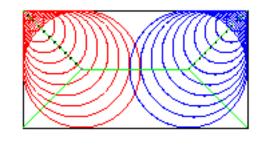
in 2d, it's called a medial axis



skeleton → shape







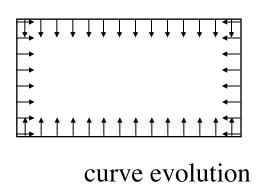
where wavefronts collide

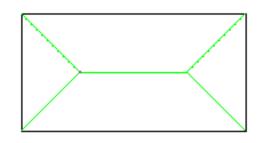
centers of maximal disks

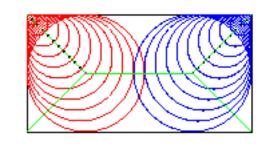
again reduces a 2d (or higher) problem to a question about graphs...



skeleton → shape





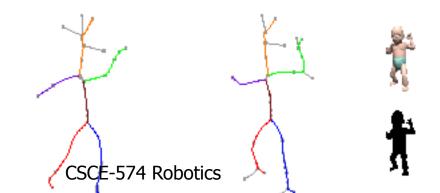


where wavefronts collide

centers of maximal disks

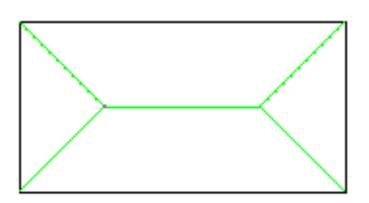
again reduces a 2d (or higher) problem to a question about graphs...

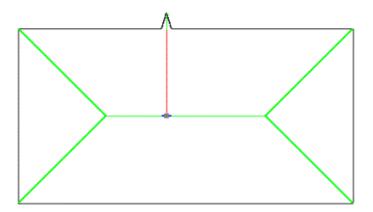






Problems



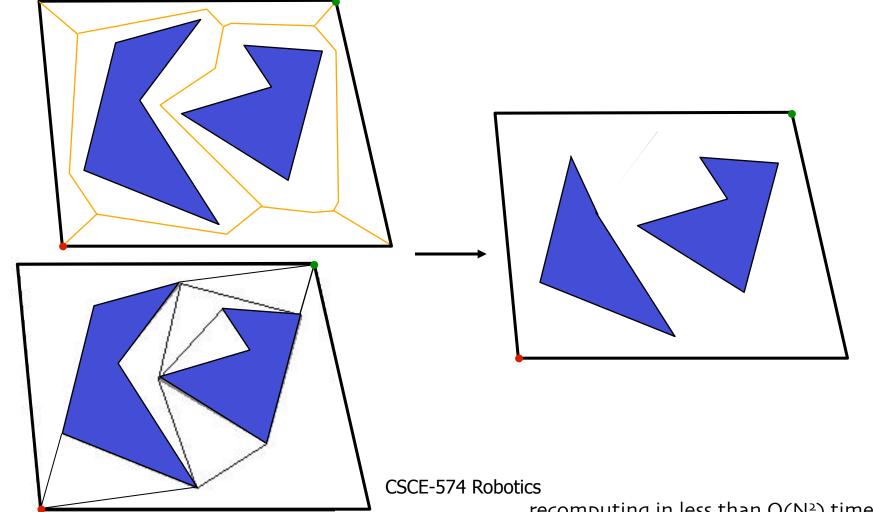


The skeleton is sensitive to small changes in the object's boundary.



Roadmap problems

If an obstacle decides to roll away... (or wasn't there to begin with)



89